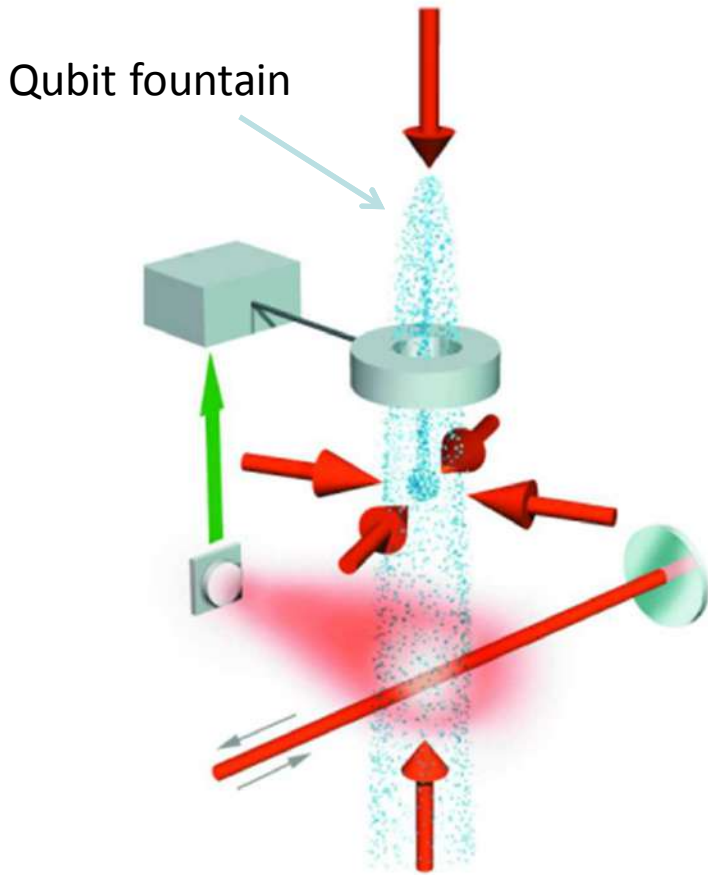


# Sensing with neutral atoms

Grant Biedermann

# Quantum-Coherence



Atomic fountain principle

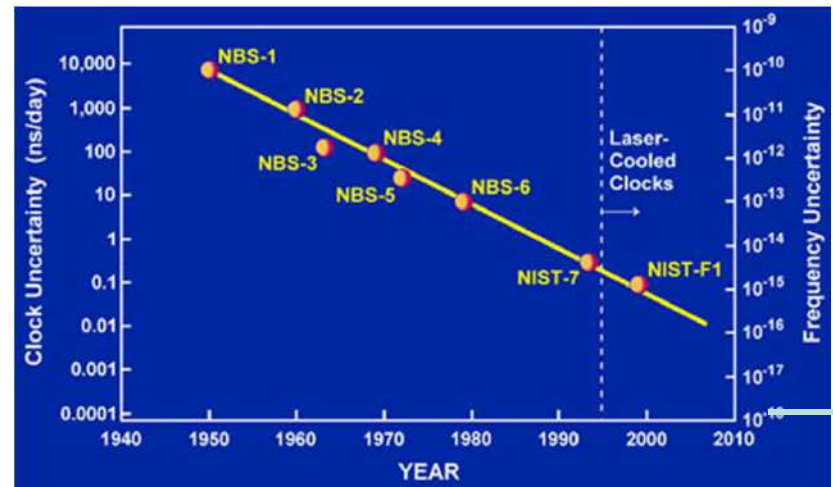
[http://smc.cnes.fr/PHARAO/GP\\_instrument.htm](http://smc.cnes.fr/PHARAO/GP_instrument.htm)

Outstanding quantum coherence in neutral atoms enables precision metrology and quantum information

- Example: atomic clocks

$$|6^2 S_{1/2}; F = 3, M_F = 0\rangle \leftrightarrow |6^2 S_{1/2}; F = 4, M_F = 0\rangle$$

$$|0\rangle \leftrightarrow |1\rangle$$

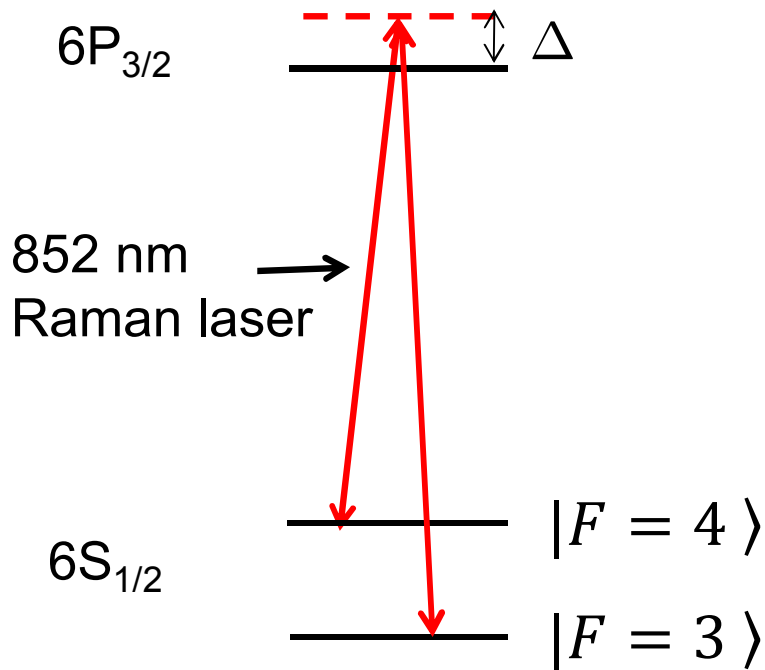


<http://www.nist.gov>

Optical  
clocks

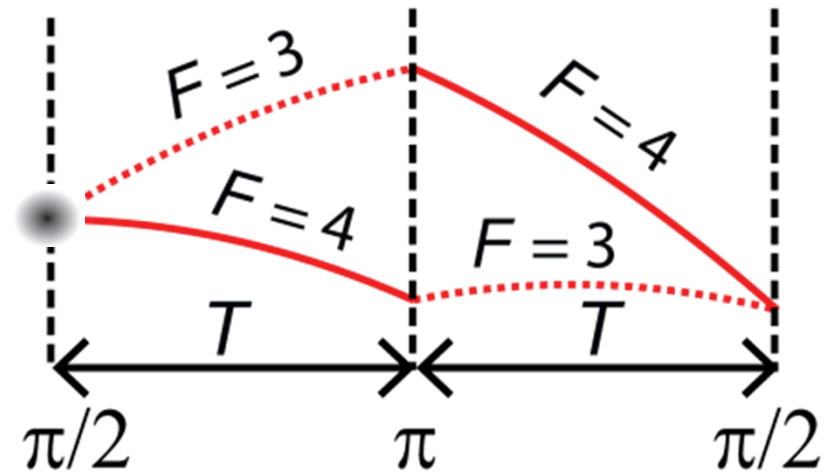
Typical accuracy now better than one part in  $10^{15}$

# Light-pulse atom interferometry



## stimulated Raman transition

## wavepacket trajectory

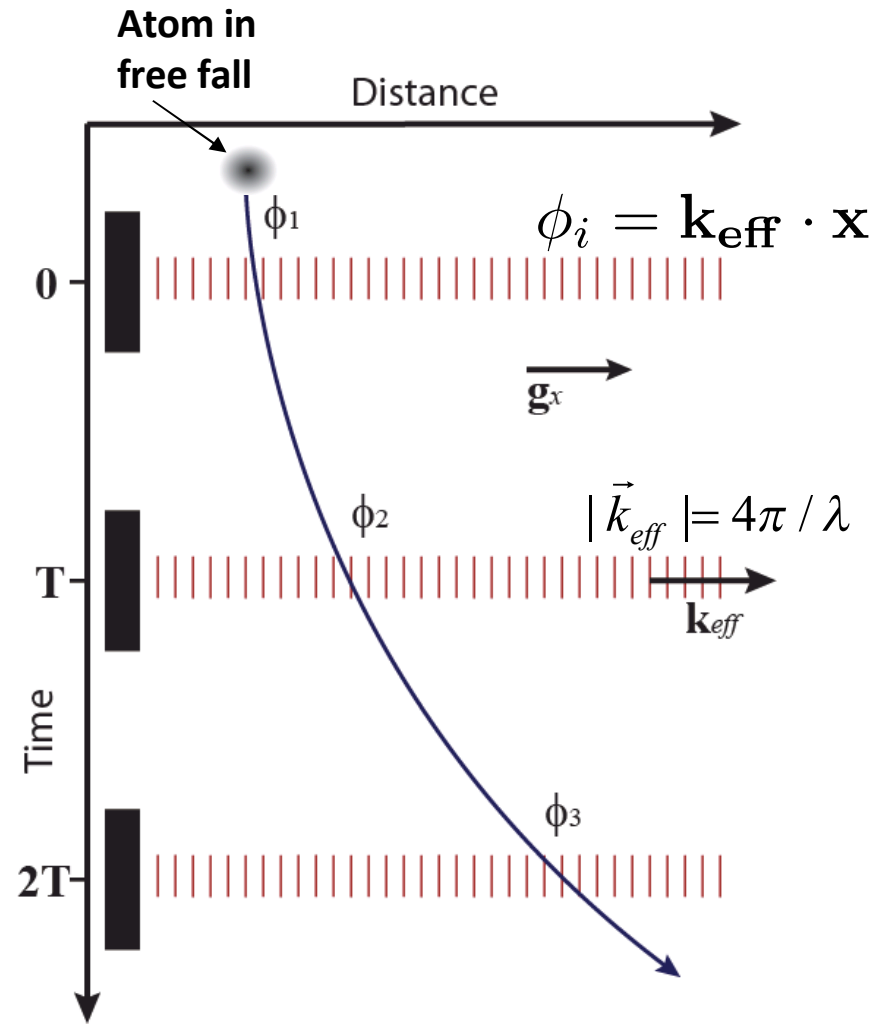
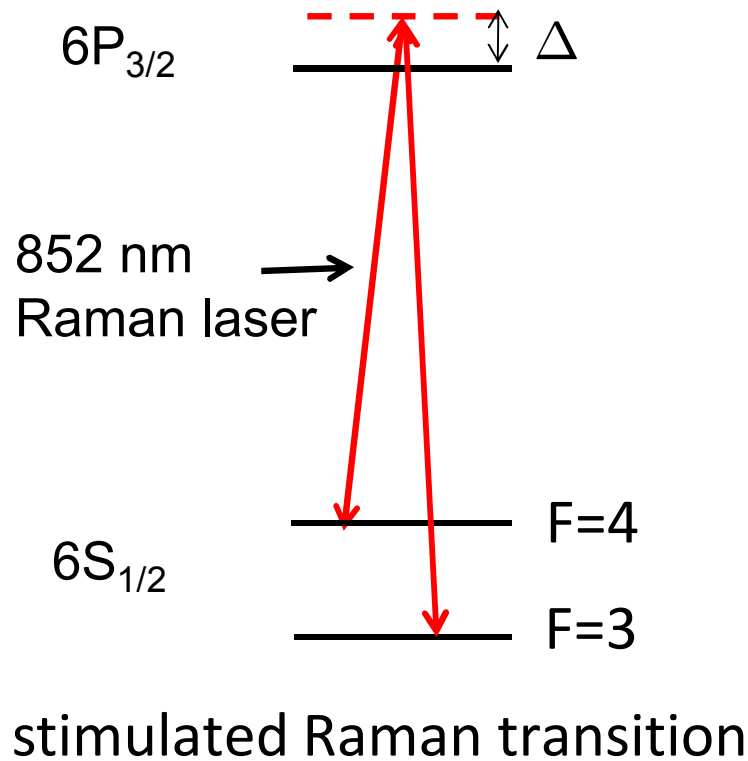


- Exceptional accelerometers and gyroscopes nrad/vHz, ng/vHz to pg/vHz
- Large commercial and govt. interest in fielding this technology

Kasevich, and Chu, Phys. Rev. Lett. 67, 181–184 (1991)

Gustavson, Landragin, and Kasevich, Class. Quantum. Grav 17, 2385–2398 (2000).

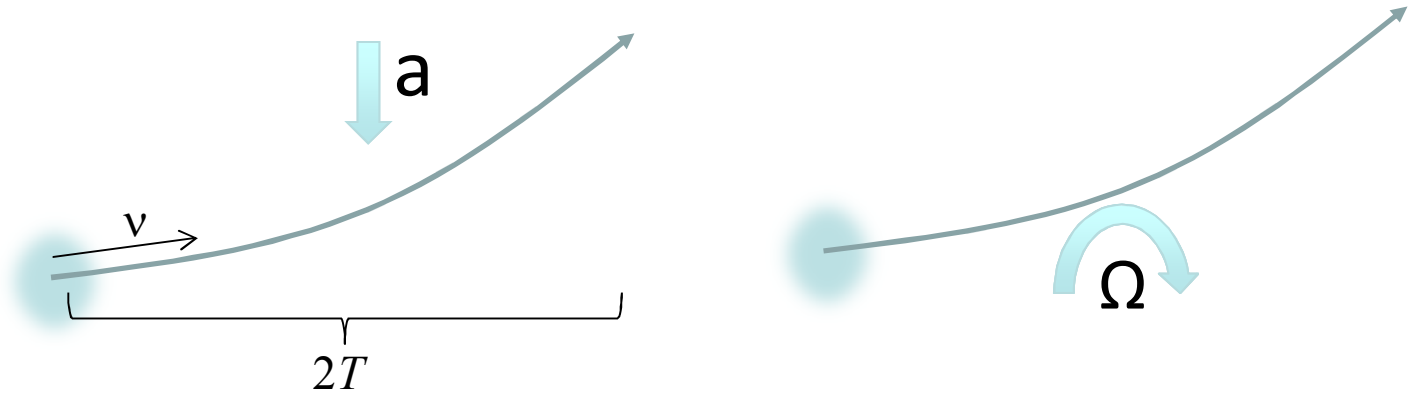
# Light-pulse atom interferometry



For an atom starting in F=3:  $P_{F=4} = \frac{1}{2} (\cos \Delta\phi)$  &  $\Delta\phi = \phi_1 - 2\phi_2 + \phi_3$

# Measuring acceleration and rotation with a particle in free-fall

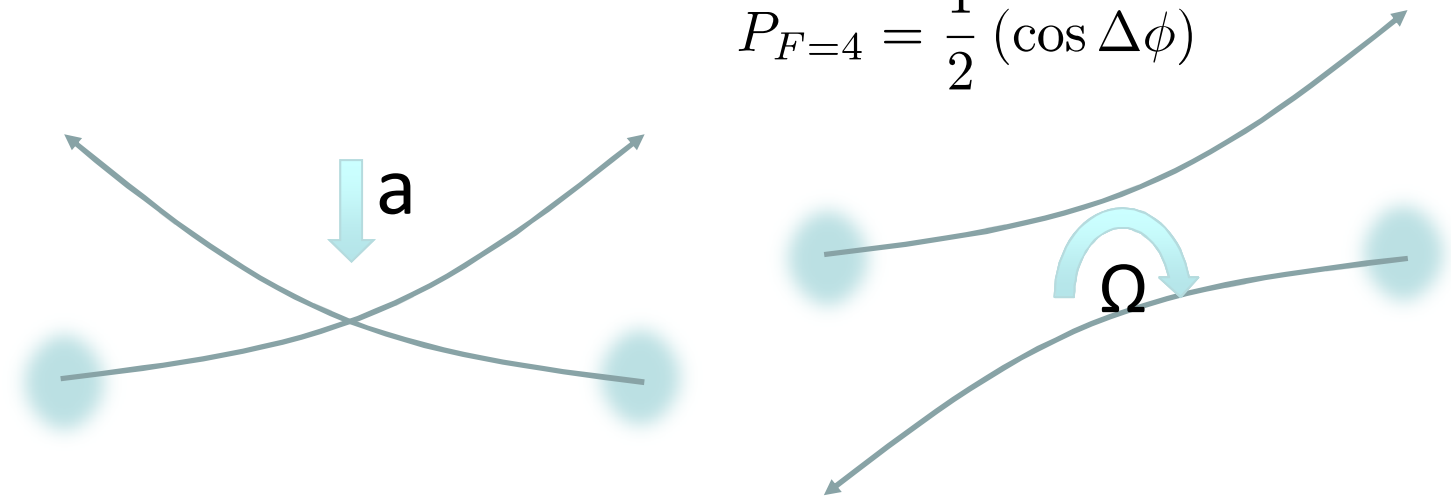
1-particle



Interferometer phase shift:  $\Delta\phi = \vec{k}_{eff} \cdot \left( \vec{a}T^2 - 2(\vec{v} \times \vec{\Omega})T^2 \right)$

$$P_{F=4} = \frac{1}{2} (\cos \Delta\phi)$$

2-particles


 Sensitivity increases with  $T^2$

# Launch and recapture

Steady state atom number:

$$N_s = \frac{\alpha\eta T_c}{\beta T_c + (1 - r_0)}$$

Base recapture efficiency  $r_0 = 96\%$

## Benefits

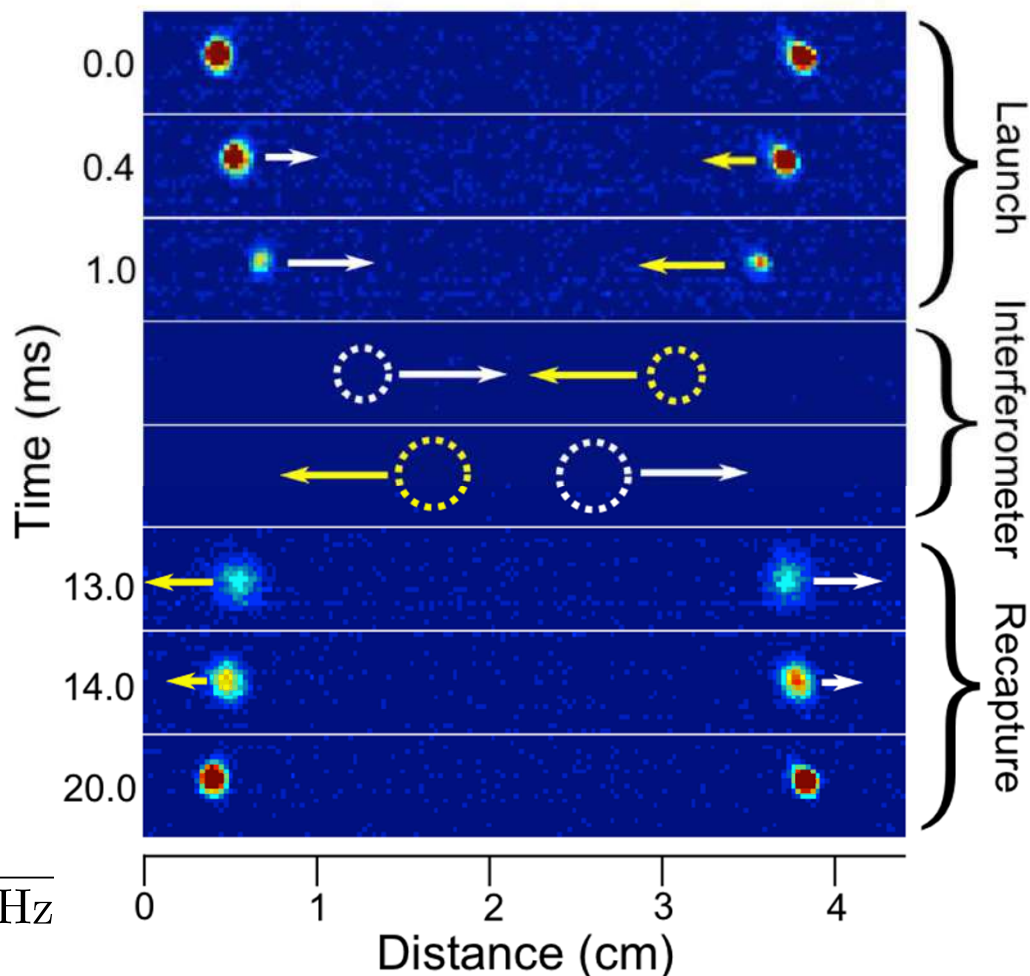
- Increases signal by 10x
- Data rates > 50 Hz
- **Minimizes** cycle dead time
- Reduced complexity
- Sufficient for:

$33 \text{ ng}/\sqrt{\text{Hz}}$  &  $70 \text{ nrad/s}/\sqrt{\text{Hz}}$

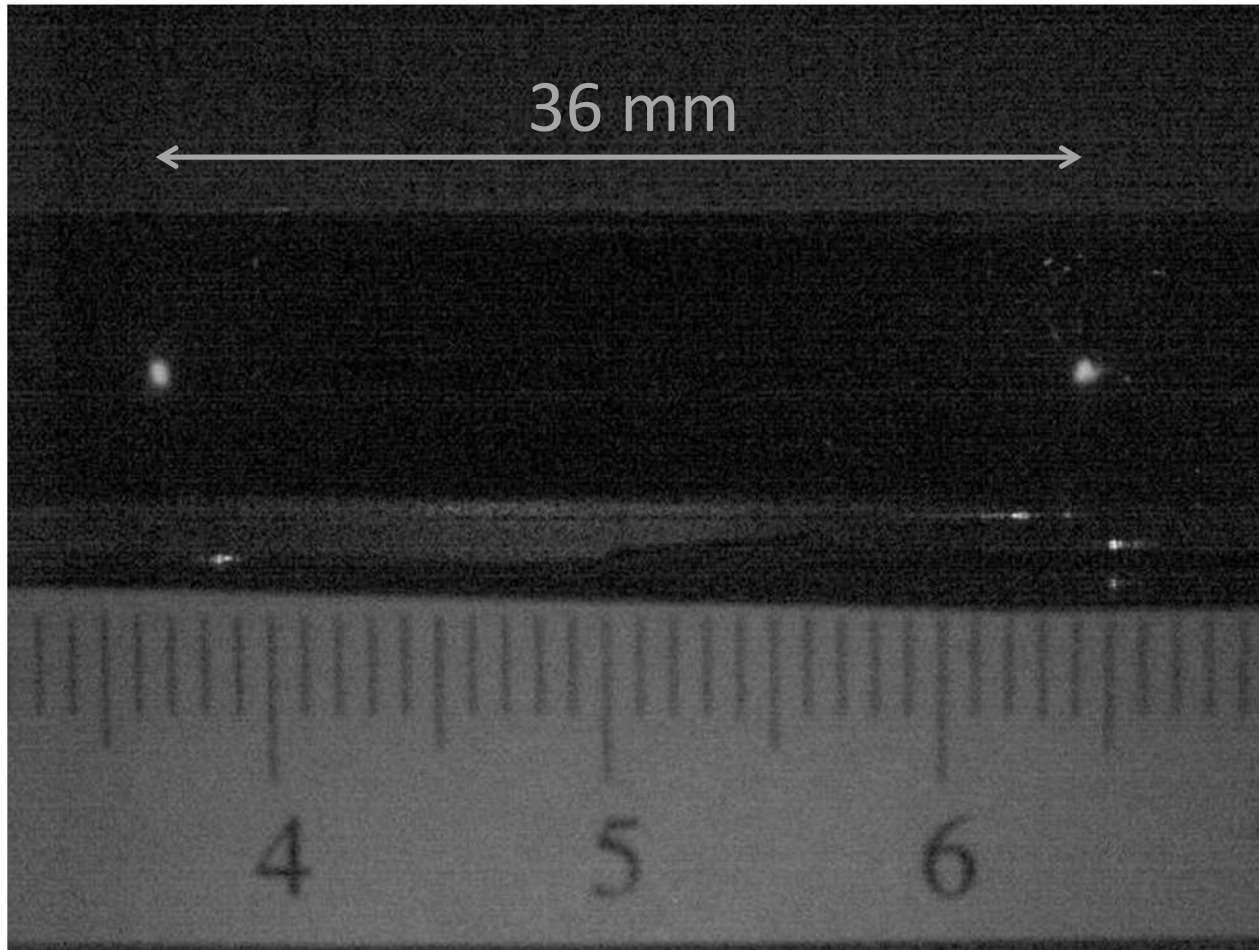
- Demonstrated:

$900 \text{ ng}/\sqrt{\text{Hz}}$  &  $1100 \text{ nrad/s}/\sqrt{\text{Hz}}$

CCD images of ensemble exchange

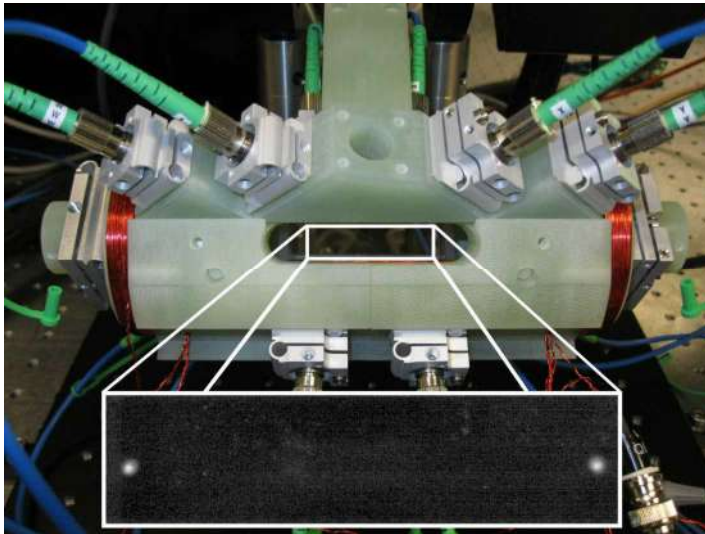


# Launch and recapture

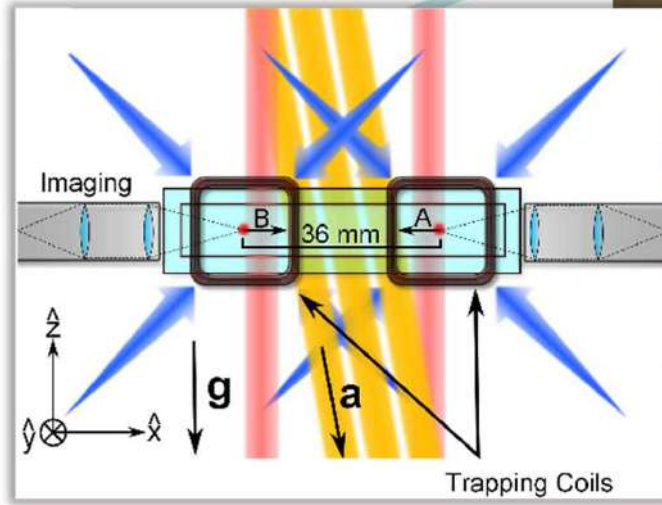
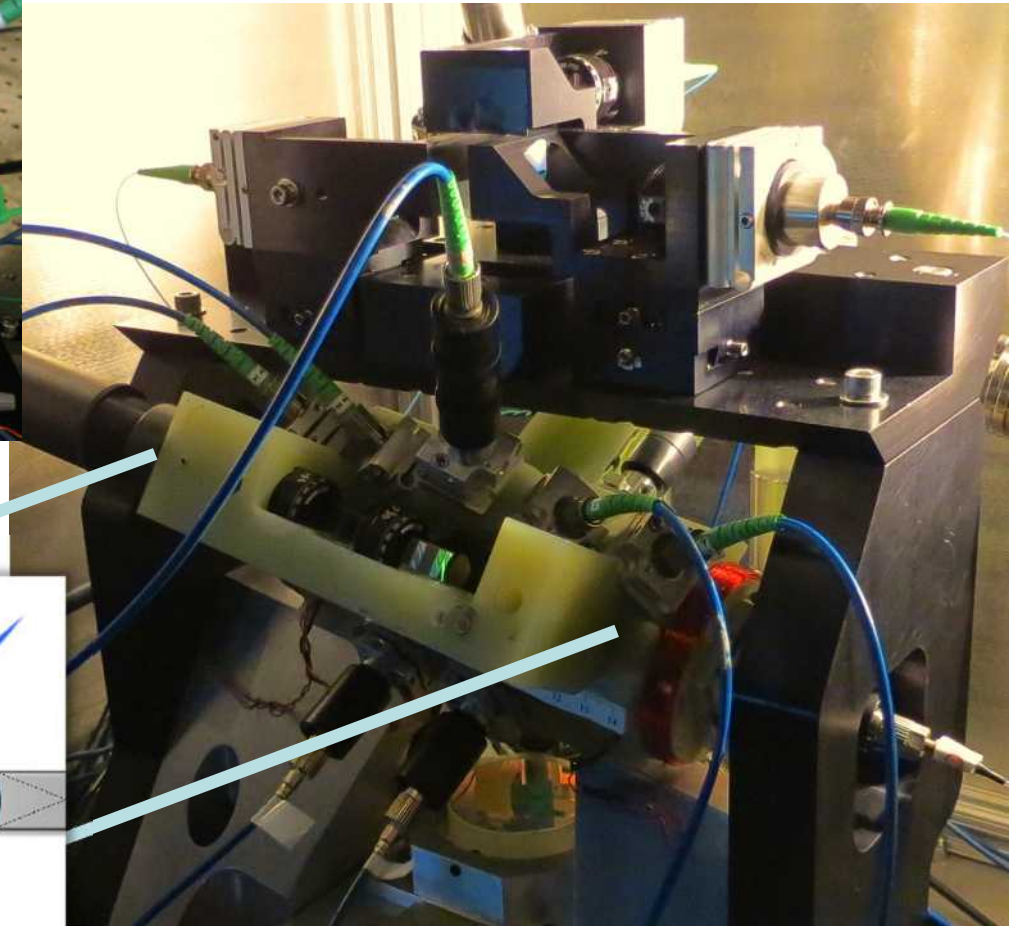


- Repeats at  $\approx 60$  measurements per second

# Experiment platform



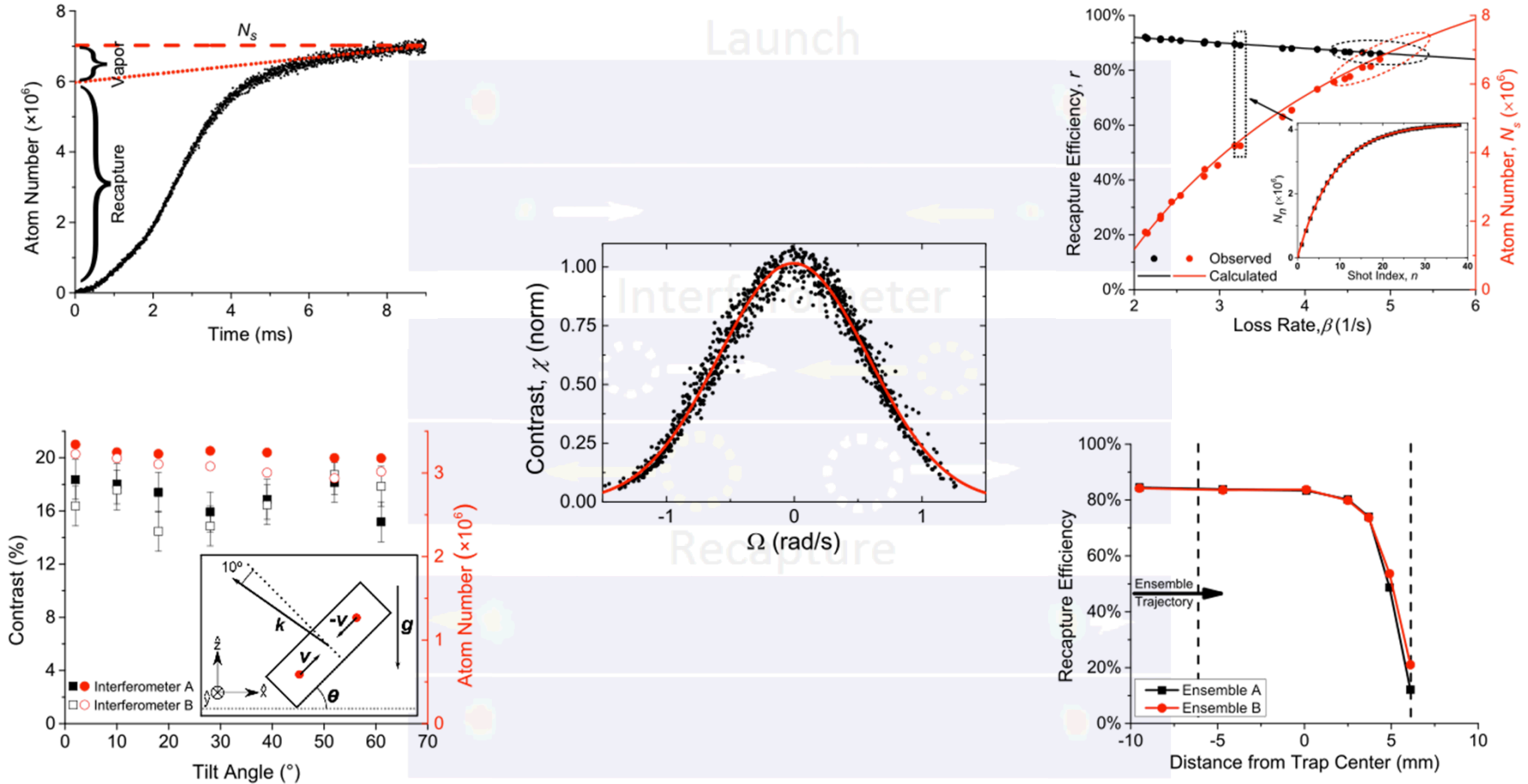
Picture of interferometer sensor





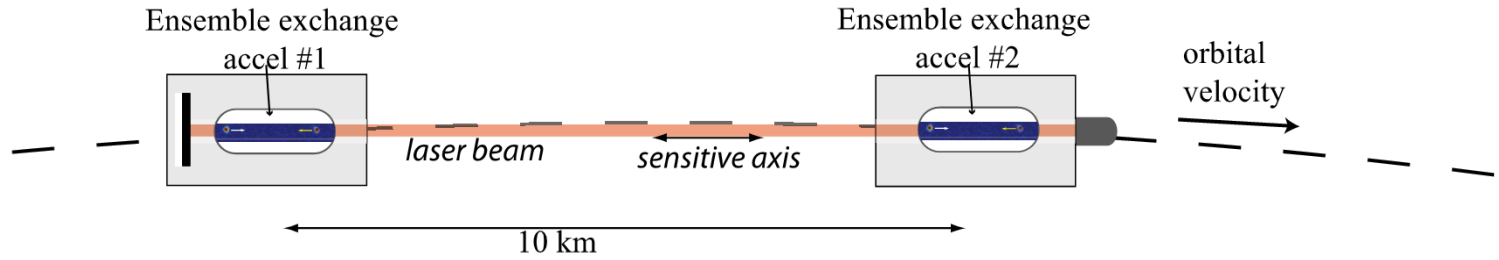
# Characterizing ensemble exchange

- Dynamic aspects of Ensemble Exchange characterized
- Robust to rotations, tilts and displacements



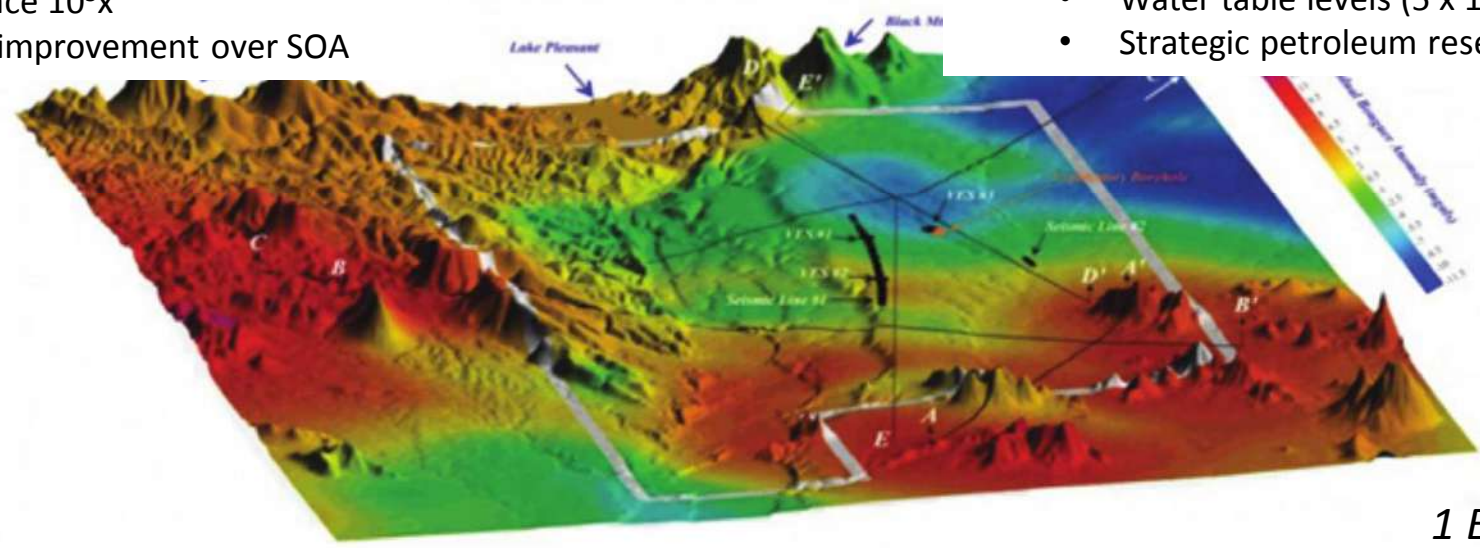
# Gradiometer survey—path finder

Simultaneous opposed gradiometers—bias rejection



- $10^4$  s stability—multiple orbital passes (SOA < 1 s)
- $10^{-3}$  E per shot with ground based performance—likely to improve in space  $10^3$ x
- $10^4$  x improvement over SOA

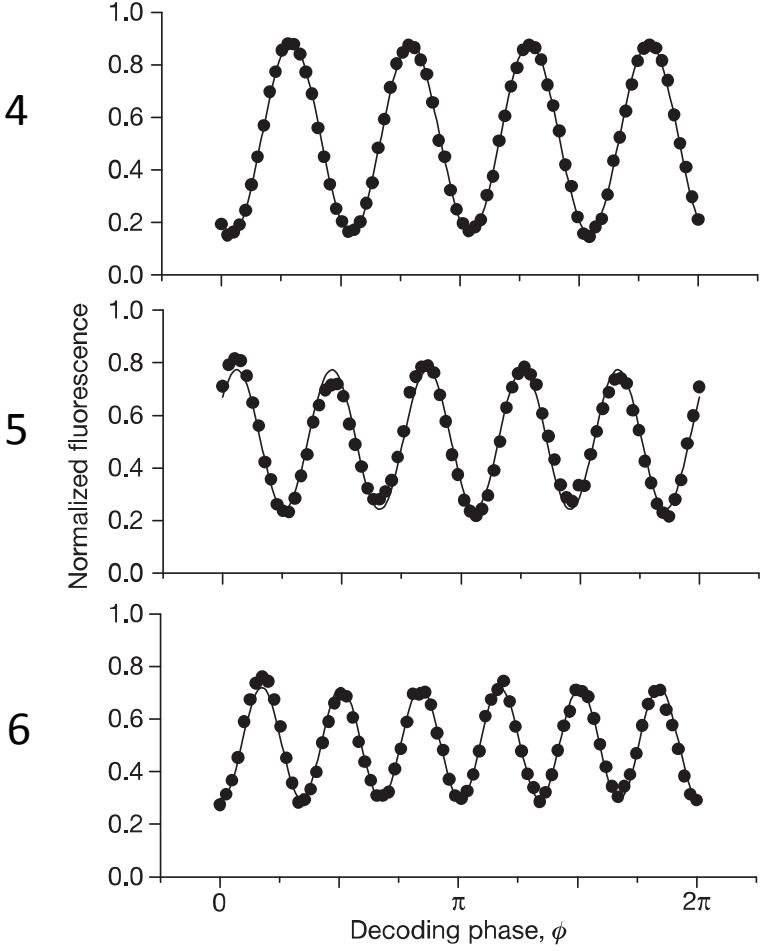
- Improved gravity maps in contested areas for GPS-denied navigation
- Other targets
  - Soil erosion ( $10^{-3}$  E)
  - Water table levels ( $5 \times 10^{-3}$  E)
  - Strategic petroleum reserves ( $10^{-6}$ E)



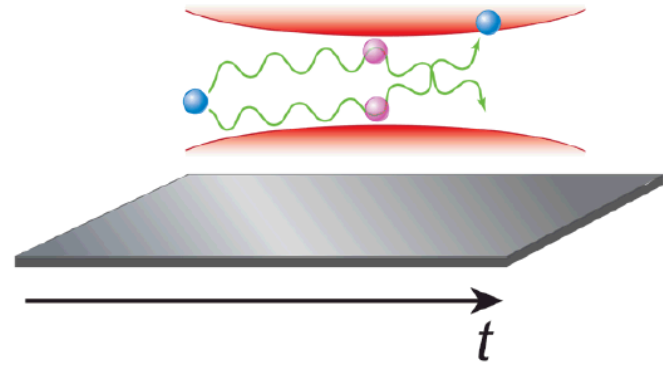
$$1 E = 10^{-9} /s^2$$

# Entangled states for metrology

Cat states with ions [1]



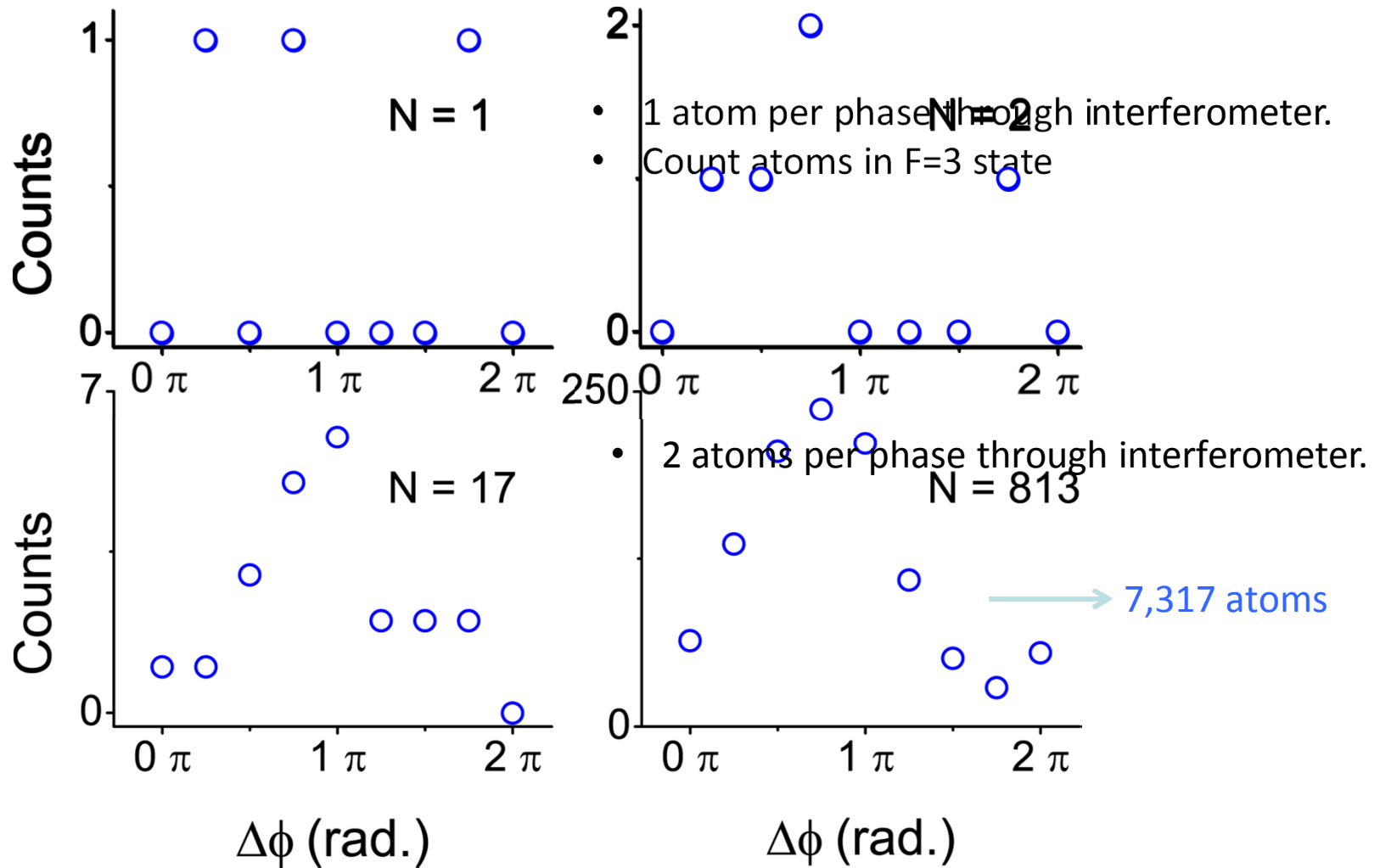
Atom interferometer with single atoms



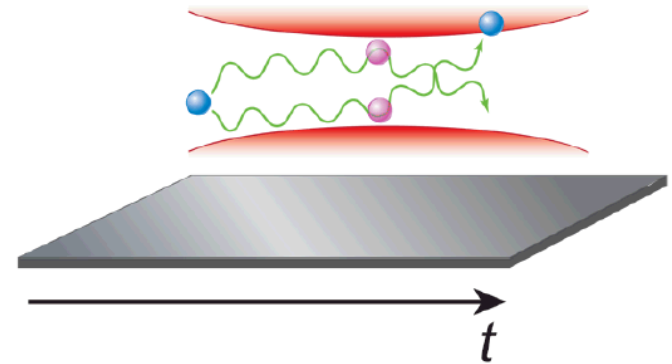
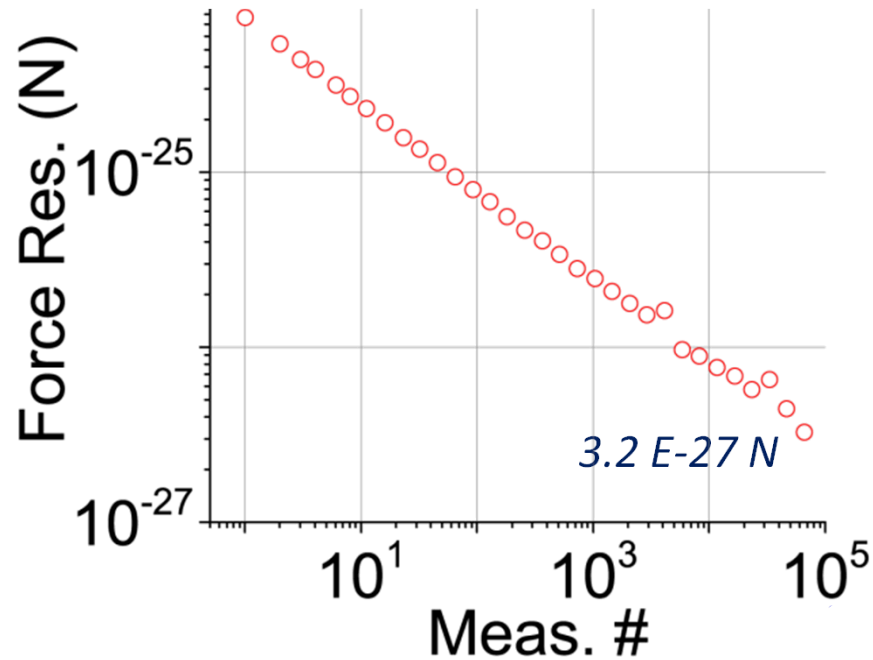
E. Rasel, Physics 5, 135 (2012)

[1] Leibfried, et al., "Creation of a six-atom 'Schrödinger cat' state", *Nature* 438, 639 (2005)

# Building a fringe, one atom at a time



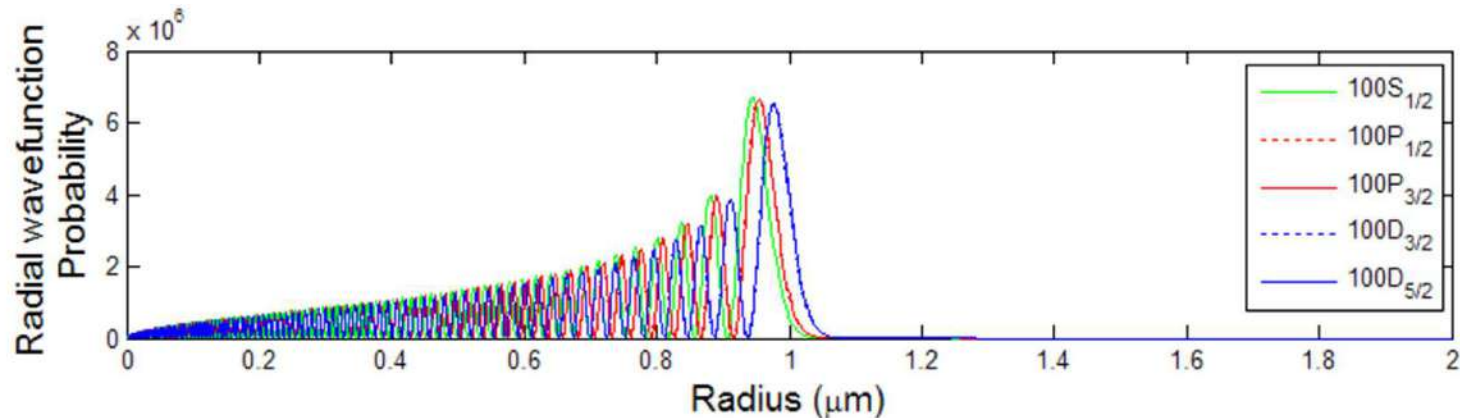
# Single atom interferometry



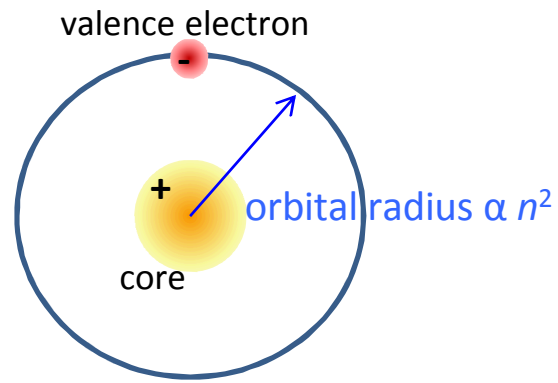
- We showed one can use single atoms
- Single atom control: gateway to harnessing quantum control in sensing
- $10^{-27}$  N  $\approx$  mg for a cesium atom

# Rydberg state mediated interaction

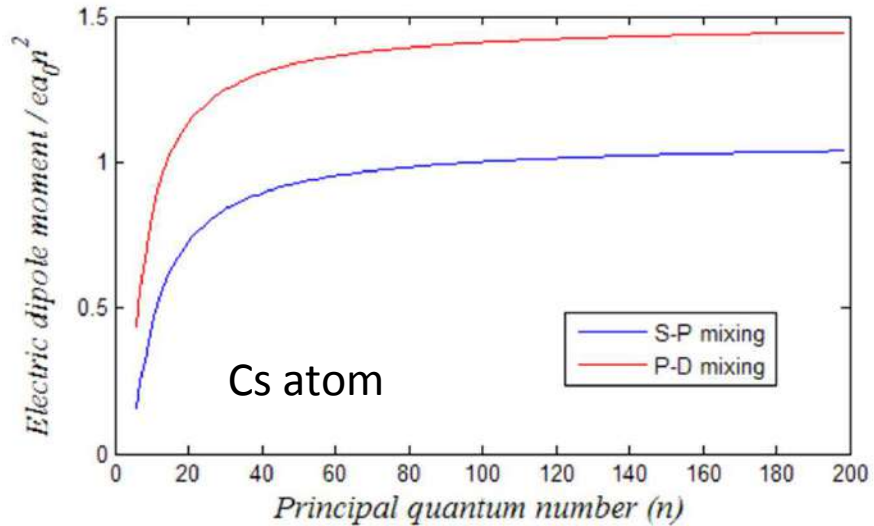
An example of the radial wavefunctions of a Cs atom at  $n = 100$ :



A Rydberg atom can have a strong electric dipole moment.

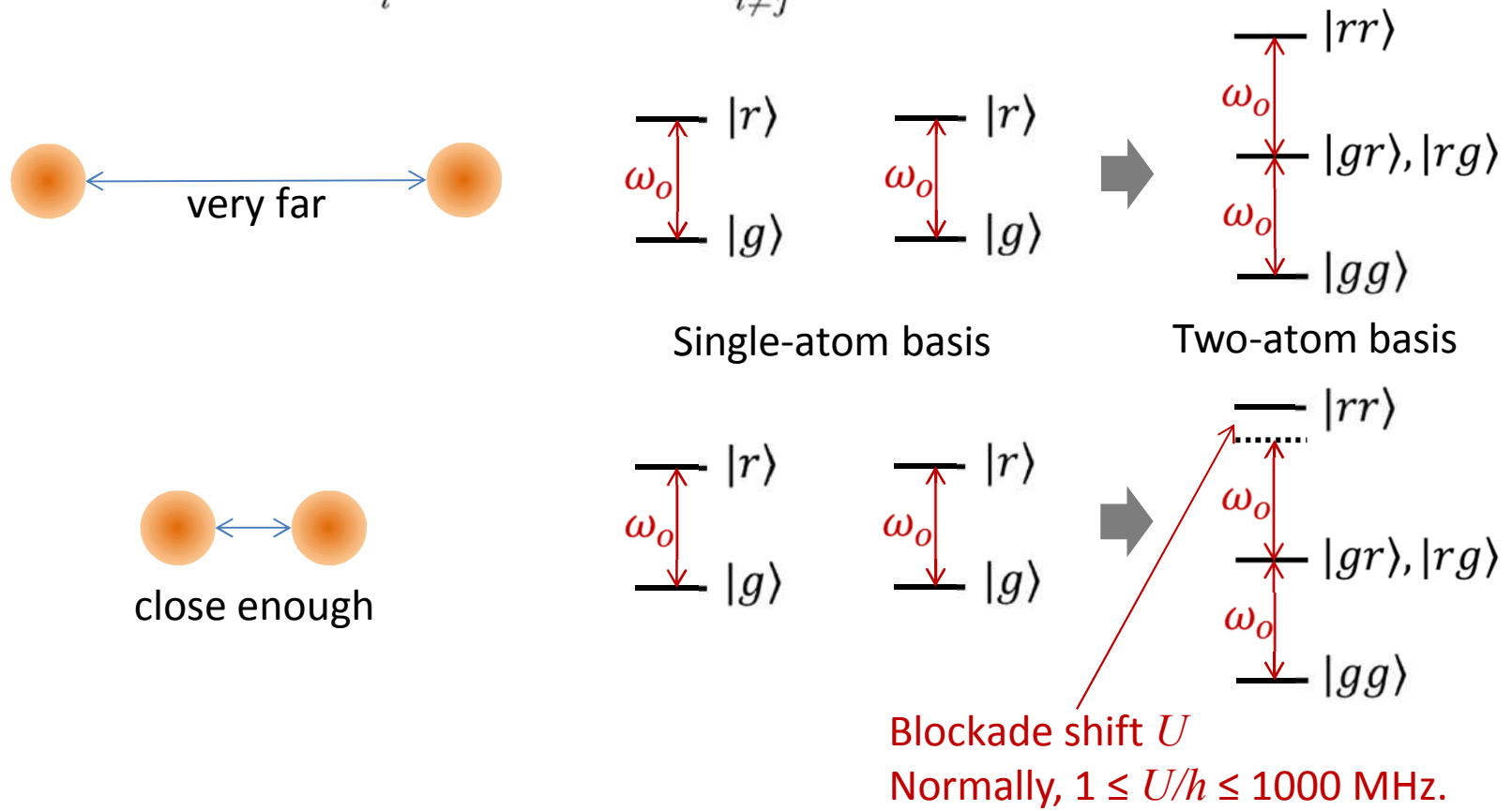


A classical picture of an atom



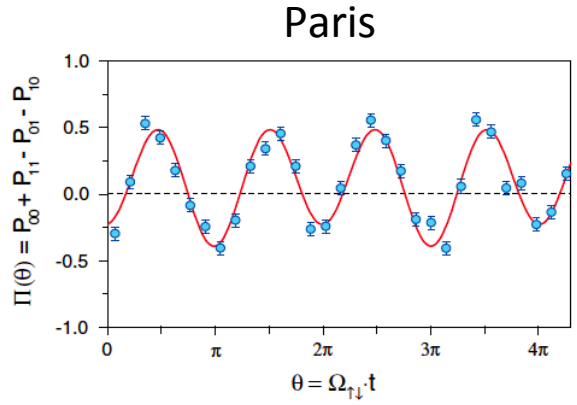
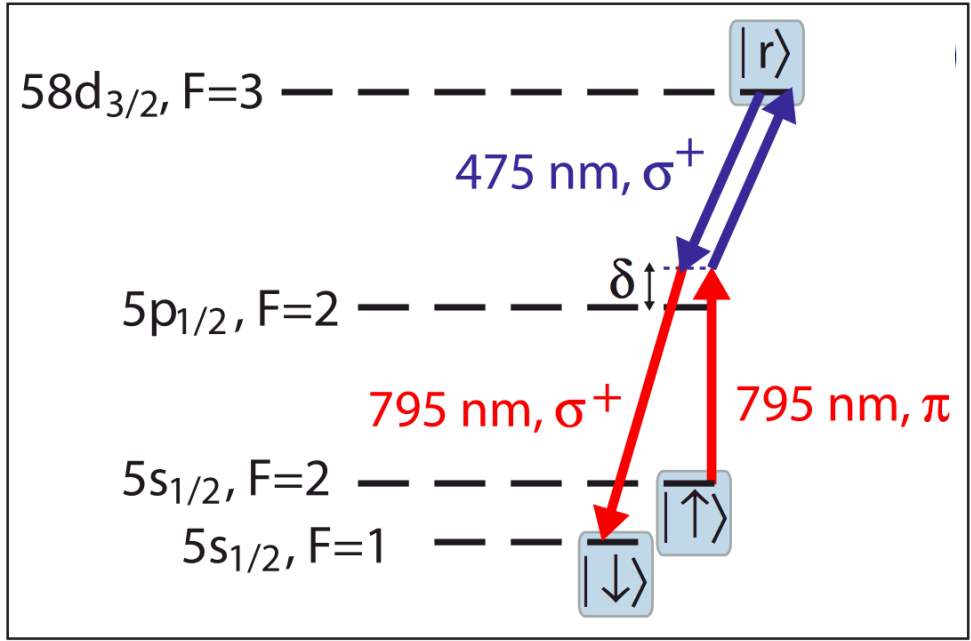
# Blockade & electric dipole-dipole interaction

$$H_{\text{atoms}} = \sum_i H_0^{(i)} + \frac{1}{4\pi\epsilon_0 r^3} \sum_{i \neq j} (\mathbf{D}^{(i)} \cdot \mathbf{D}^{(j)} - 3\mathbf{D}^{(i)} \cdot \hat{\mathbf{r}}\hat{\mathbf{r}} \cdot \mathbf{D}^{(j)})$$



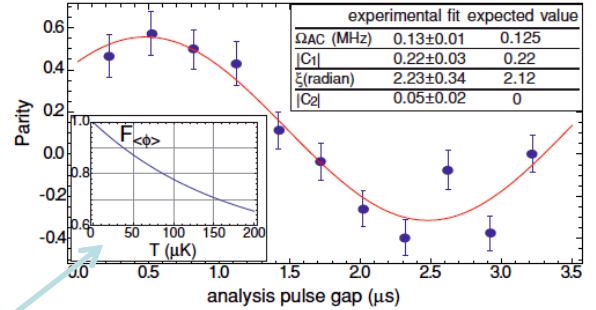
# On-demand interactions

## Two-atom entanglement using Rydberg blockade

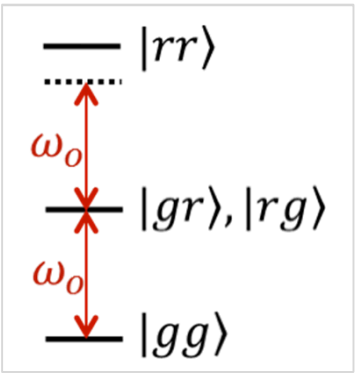


Wilk et al., PRL 104, 010502 (2010)

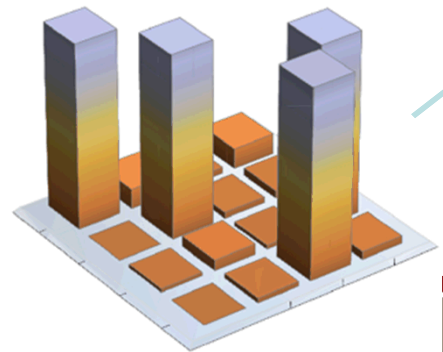
## Wisconsin



Zhang et al., PRA 82, 030306(R) (2010)

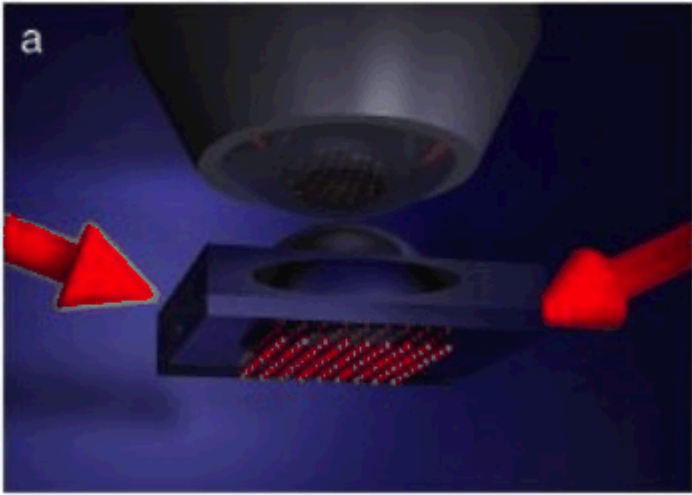


CNOT gate

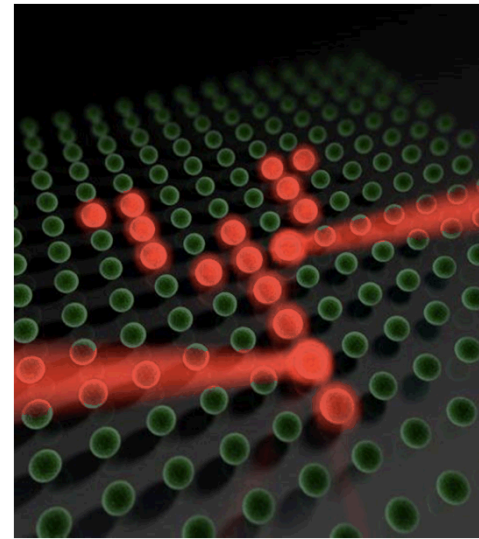




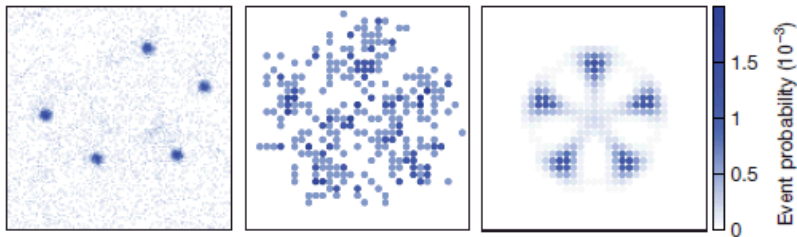
# Many body systems



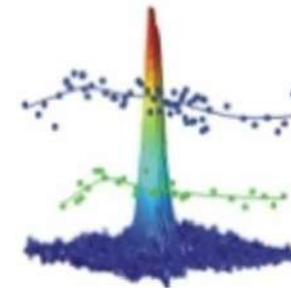
“Quantum Gas Microscope” Nature 462,74 (2009)



“Quantum simulation”, Nature Physics 8, 267 (2012)



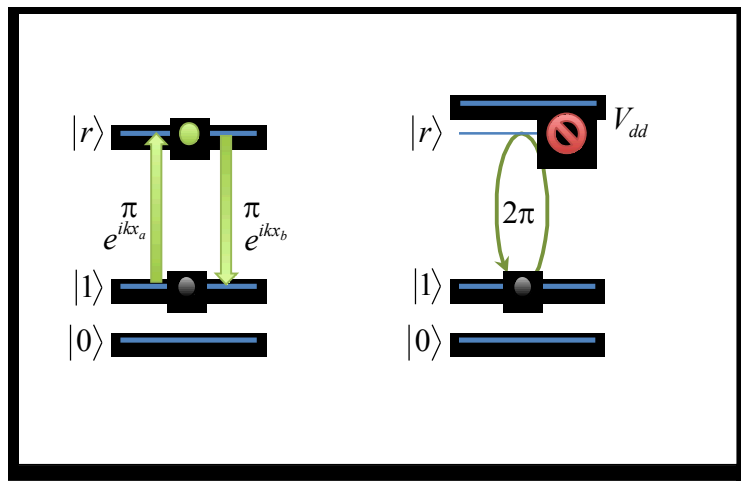
“Rydberg interactions in a lattice”, Nature 491, 87 (2012)



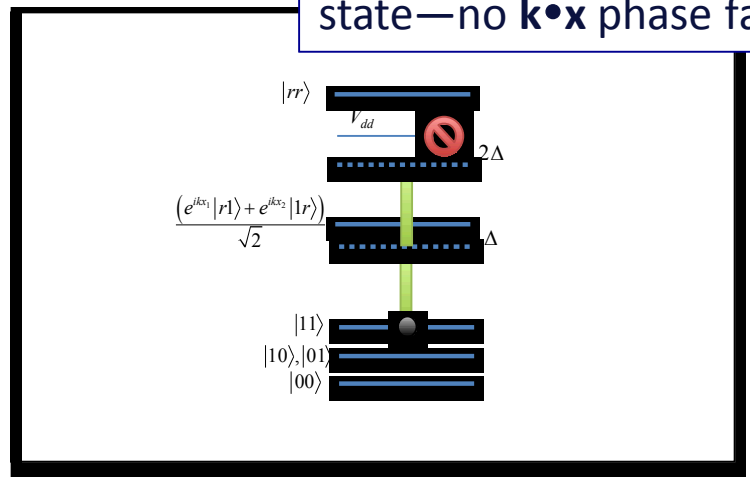
“Rydberg excitations in a BEC”, PRL 100, 033601 (2008)

# New options for Rydberg-state-mediated interactions

## Comparison of methods



Direct excitation

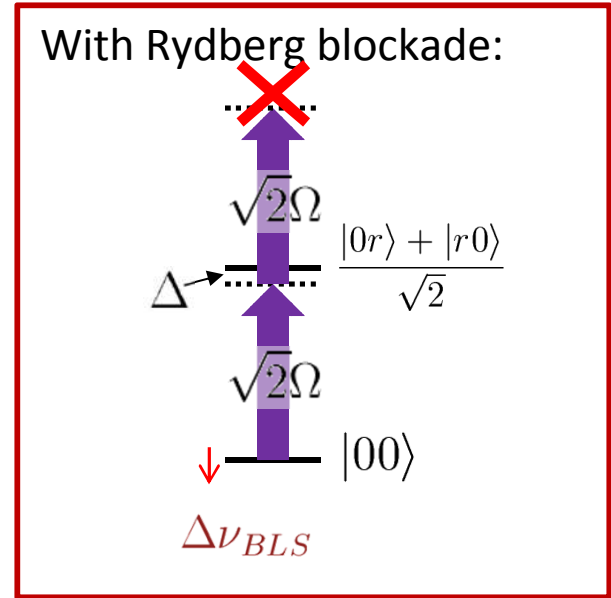
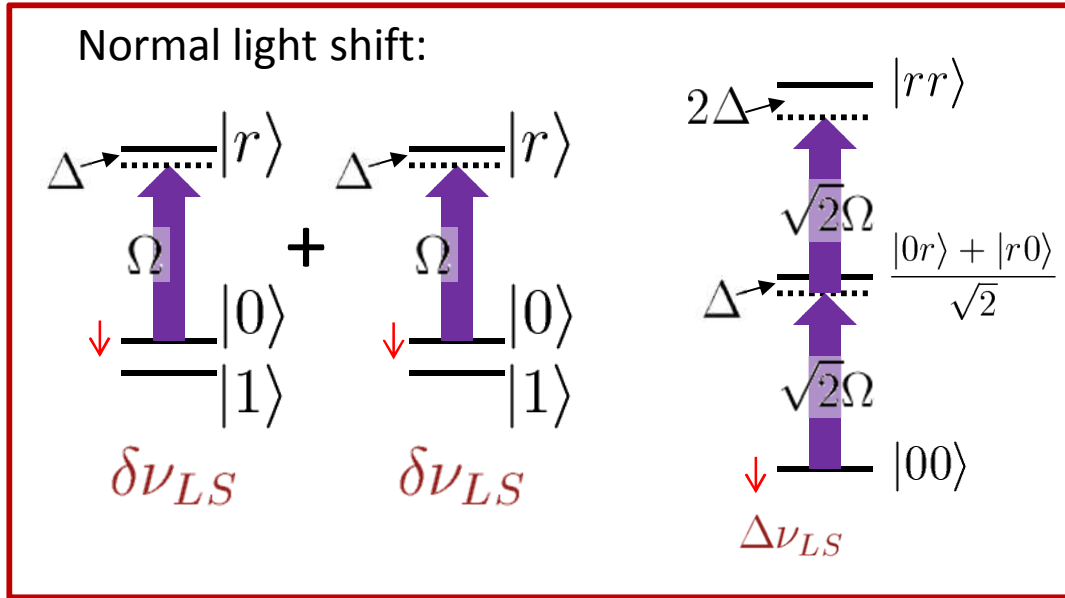


Rydberg dressed

"Elaborate theoretical proposals for the realization of various complex phases and applications in quantum simulation exist. Also a simple model has been already developed that describes the basic idea of Rydberg dressing in a two-atom basis. However, an experimental realization has been elusive so far."

T. Pfau's group, Stuttgart, Germany  
 J. B. Balewski, *et al.*, *N. J. Phys.* 16, 063012 (2014)

# Interaction between two Rydberg-dressed atoms



$$H_{BLS} = H_{LS} + H_{int} = \begin{bmatrix} 2\delta\nu_{LS} & 0 & 0 & 0 \\ 0 & \delta\nu_{LS} & 0 & 0 \\ 0 & 0 & \delta\nu_{LS} & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} + \begin{bmatrix} J & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \text{ for } \begin{bmatrix} |00\rangle \\ |01\rangle \\ |10\rangle \\ |11\rangle \end{bmatrix}$$

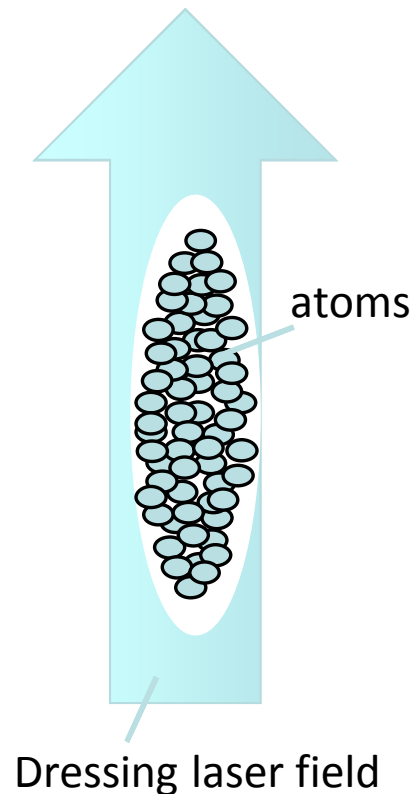
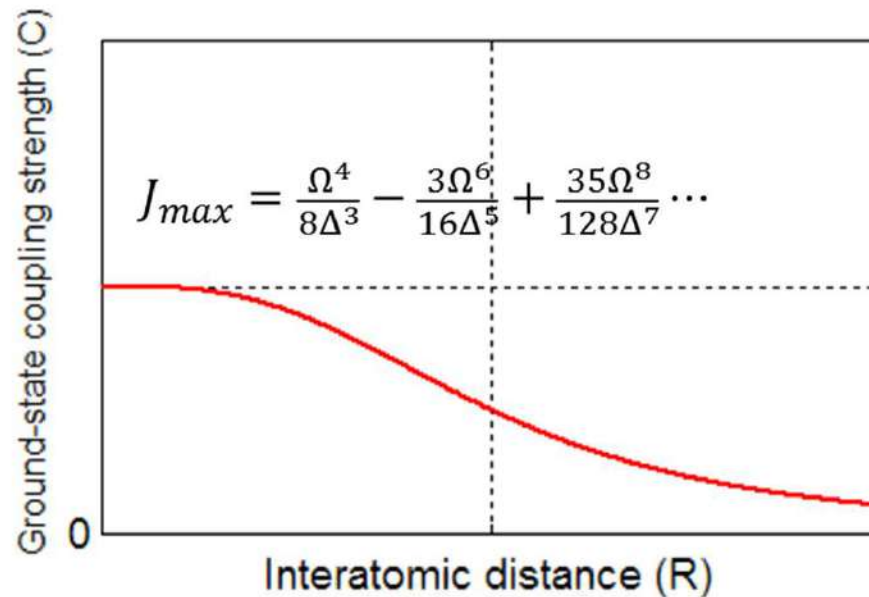
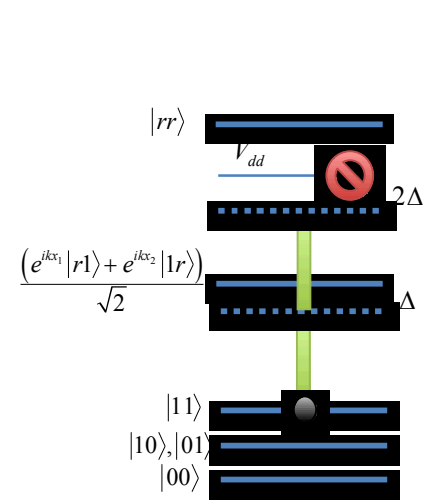
$$J = \Delta\nu_{BLS} - \Delta\nu_{LS} = \frac{\Omega^4}{8\Delta^3} - \frac{3\Omega^6}{16\Delta^5} + \frac{35\Omega^8}{128\Delta^7} - \dots$$

$$H_{int} = \frac{J}{4} (\sigma_z^{(1)} + 1)(\sigma_z^{(2)} + 1)$$

# Rydberg-dressed interactions

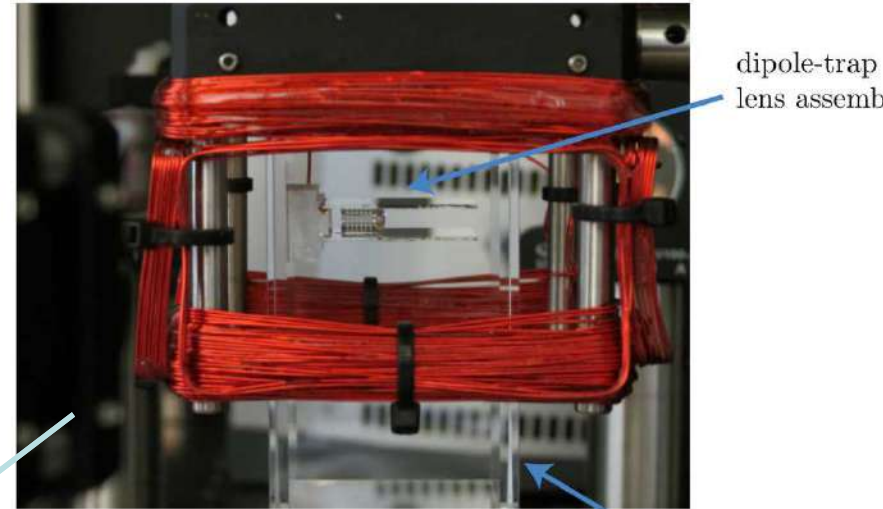
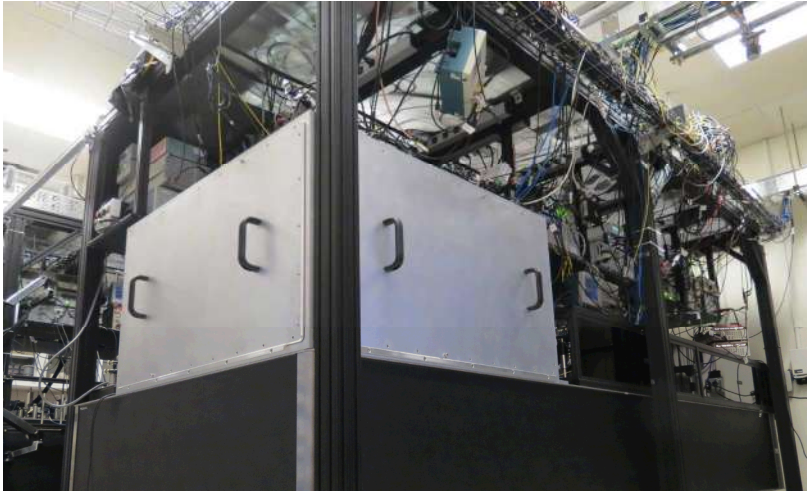
Tunable interaction strength ( $J$ ), low sensitivity to atom motion, and effectively strong ground-state interactions.

$$H_{int} = \sum_{ij} \frac{J_{ij}}{4} (\sigma_z^{(i)} + 1)(\sigma_z^{(j)} + 1)$$

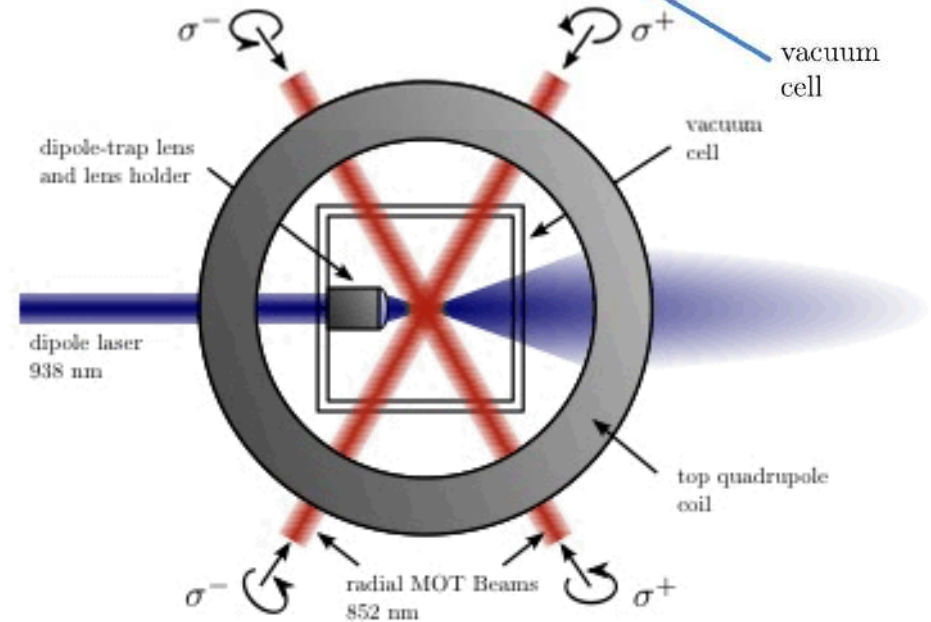
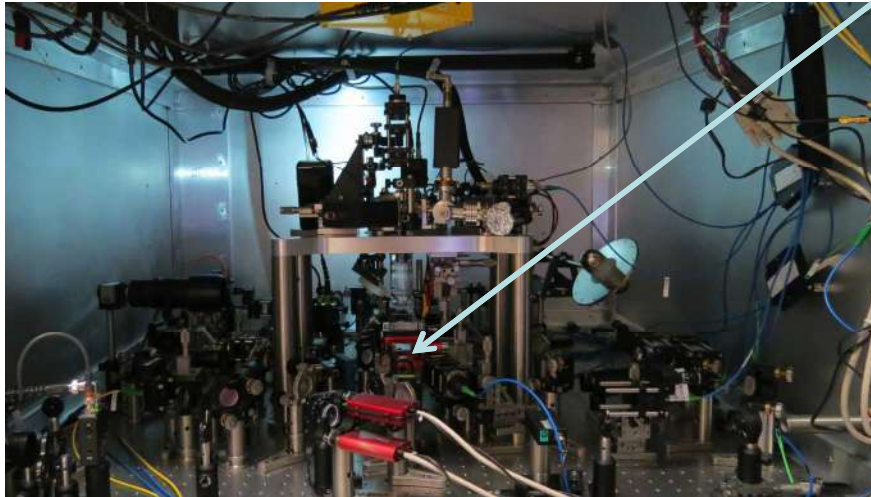


- I. Bouchoule, K. Mølmer, Phys. Rev. A 65, 041803 (2002).  
 J. Johnson, S. Rolston, Phys. Rev. A 82, 033412 (2010).

# Apparatus



dipole-trap lens assembly



vacuum cell

dipole-trap lens and lens holder

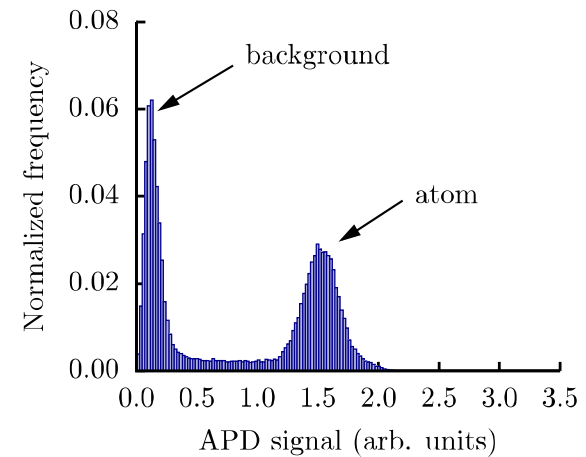
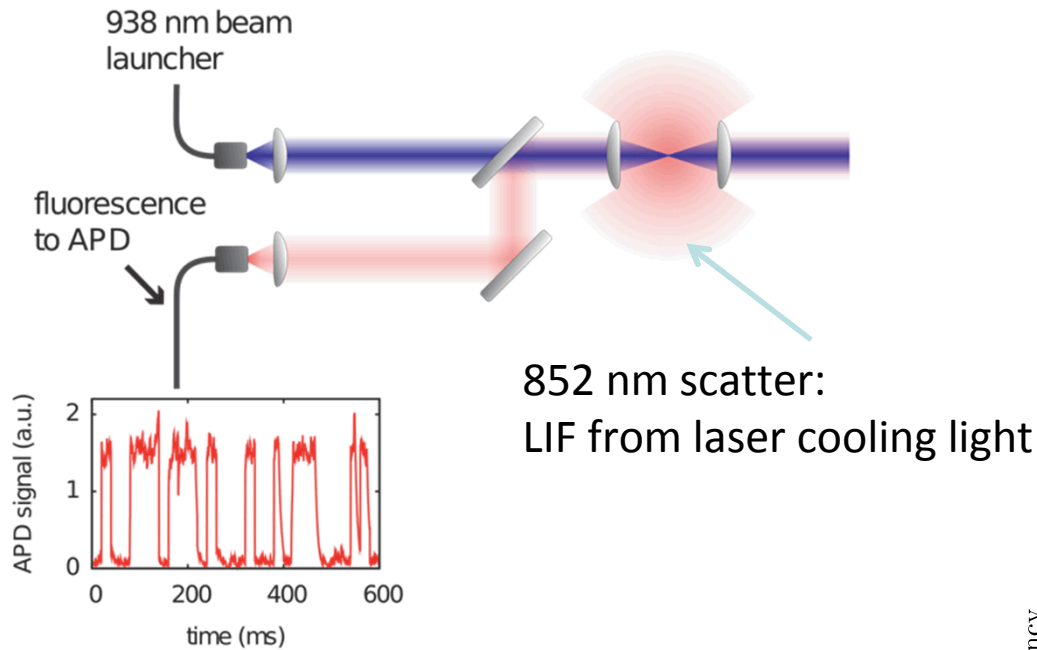
dipole laser 938 nm

vacuum cell

top quadrupole coil

radial MOT Beams 852 nm

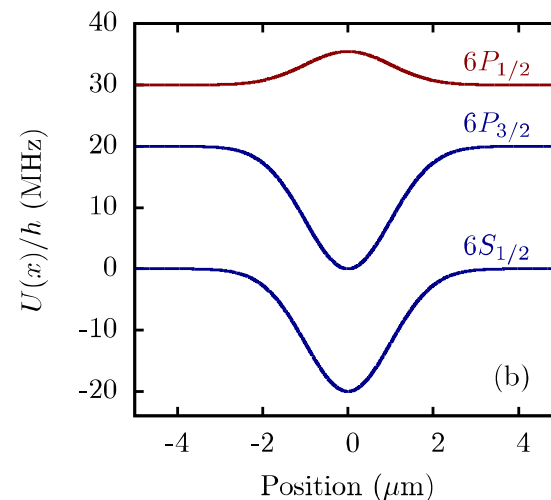
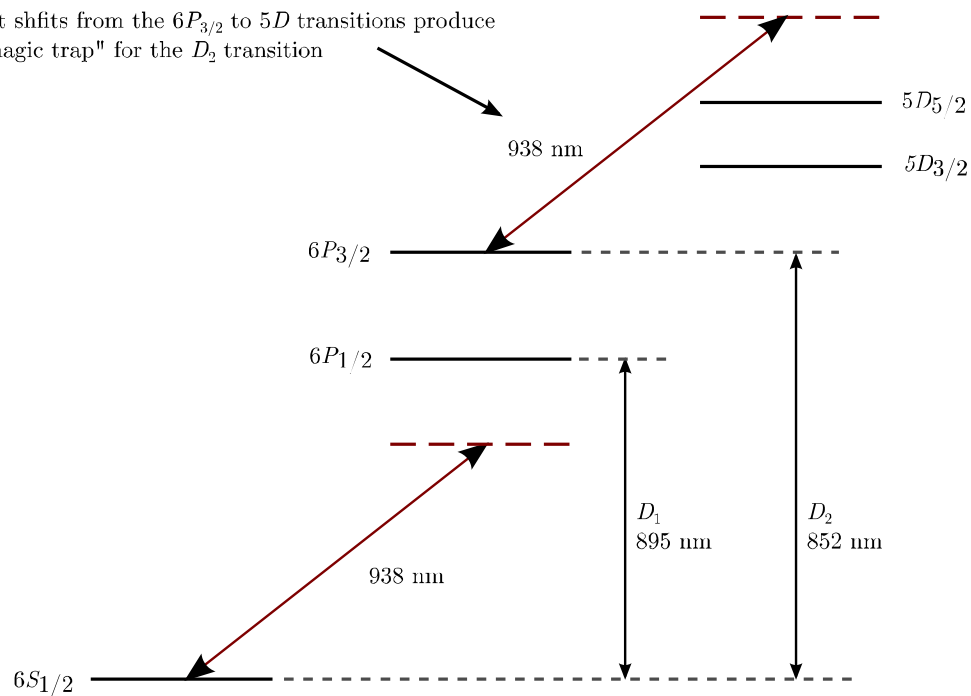
# Single atom control



Spot size  $\approx 1 \mu\text{m}$ —collisional blockade

# Single atom control

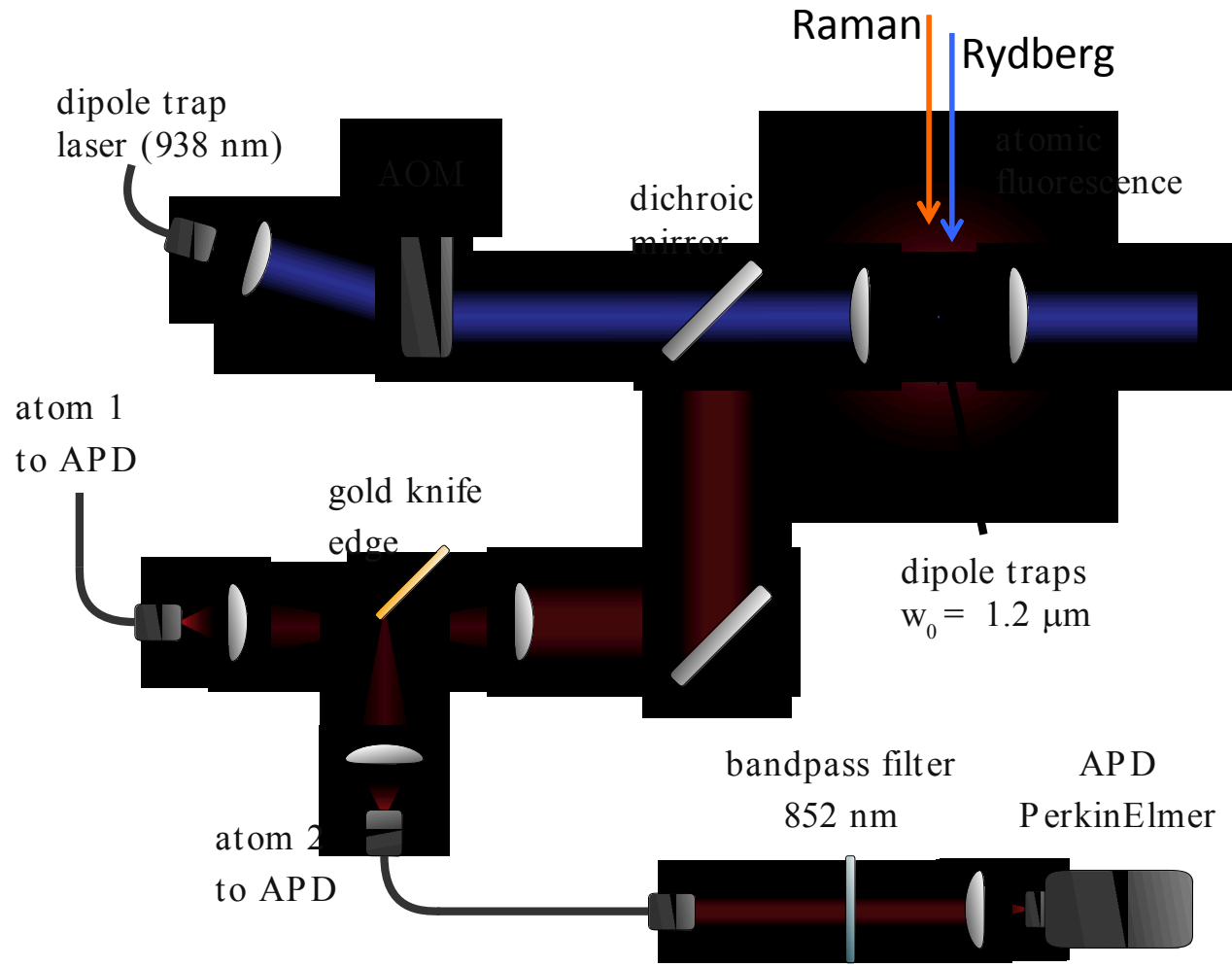
Light shifts from the  $6P_{3/2}$  to  $5D$  transitions produce a "magic trap" for the  $D_2$  transition



Why 938 nm? It's magic for the cooling transition.

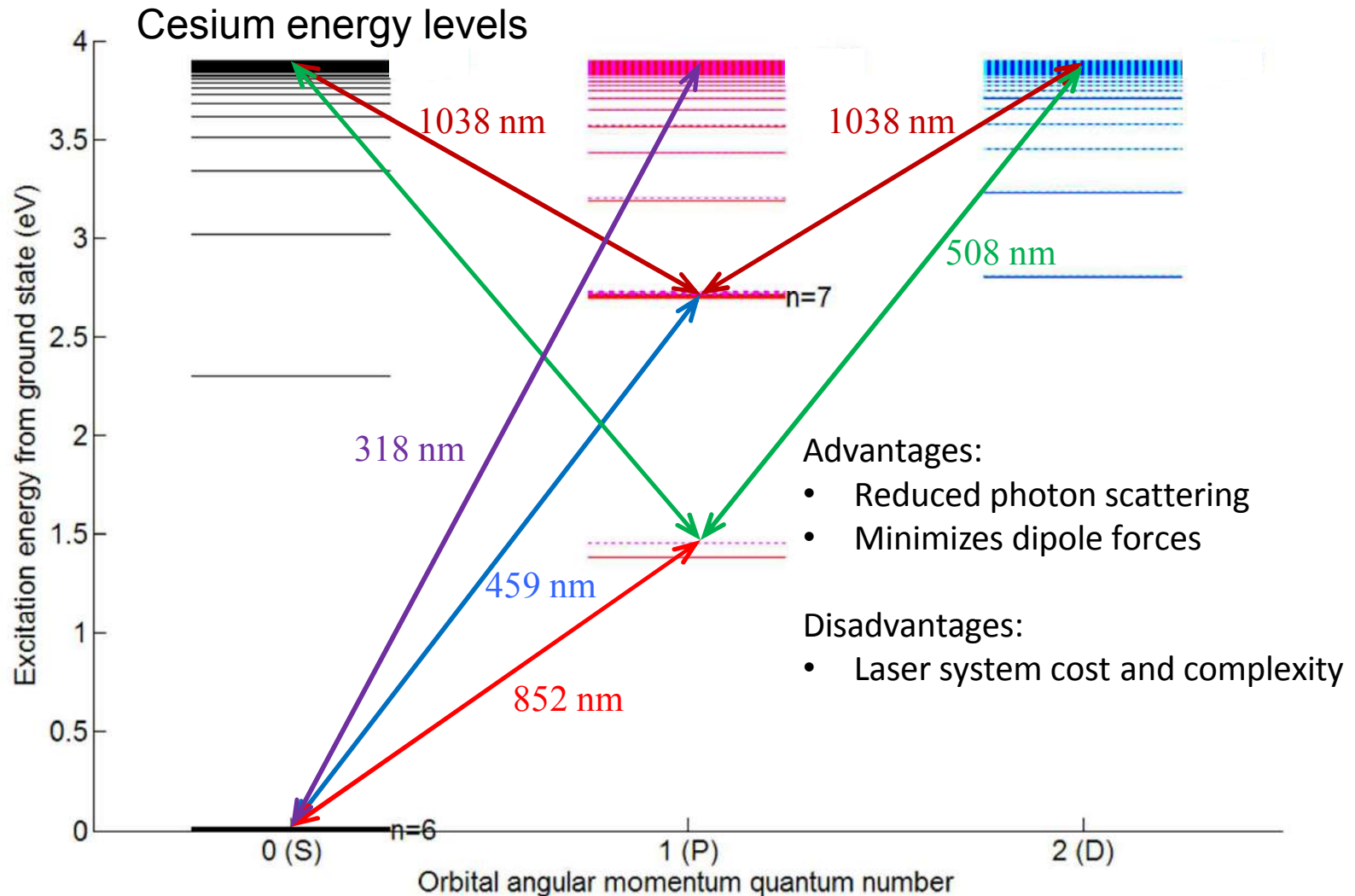
- $\approx 5$  mW, 43 nm red
- focused to  $\approx 1$   $\mu\text{m}$
- gives  $\approx 20$  MHz or  $\approx 1$  mK

# Experiment schematic

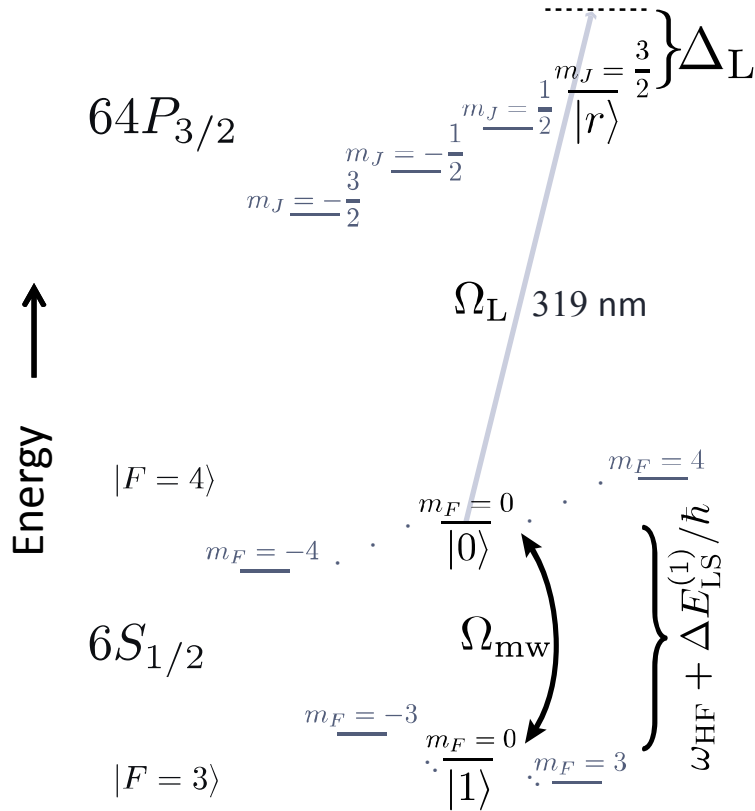




# Optimizing for long-term relationships



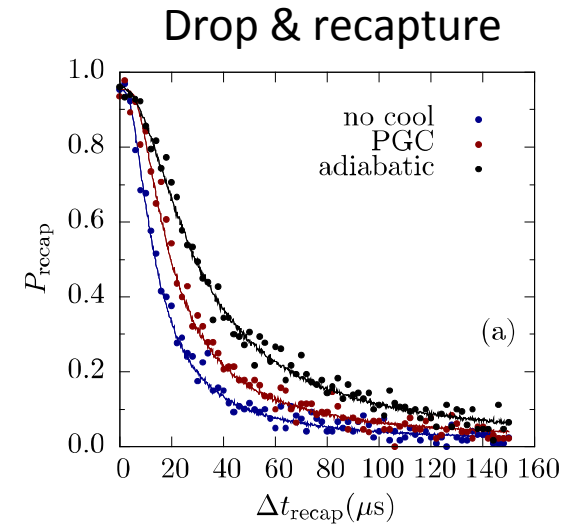
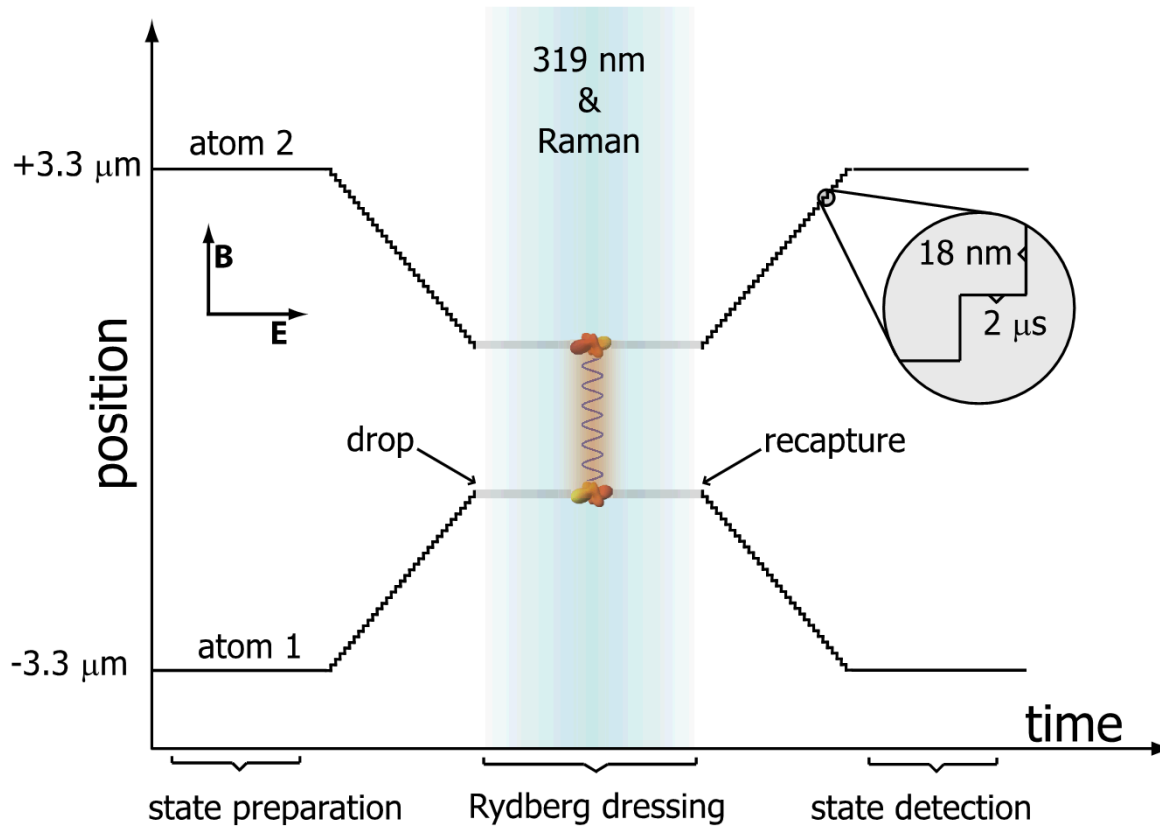
# Rydberg-dressed ground state interaction



Single atom picture

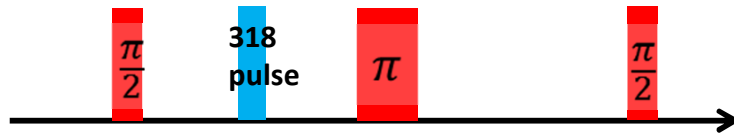
- Interaction range **increases** as principal quantum number  $n$  increases
- However, oscillator strength **decreases** as  $n$  increases—making  $\Omega_L$  smaller and thus  $J$
- Target smallest  $n$  that your optical resolution can accommodate
- Solution—*dynamic postioning*

# Dynamic atom positioning

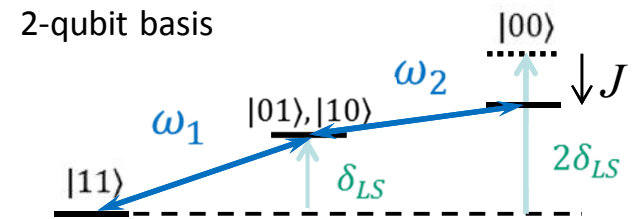
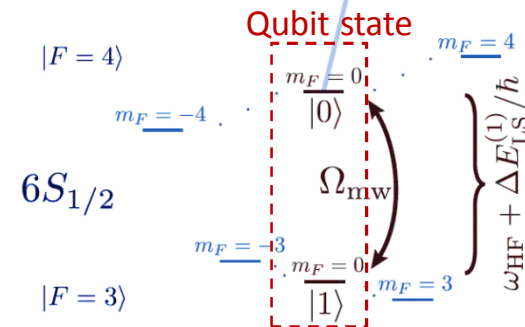
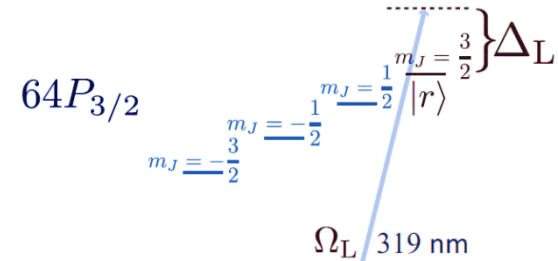
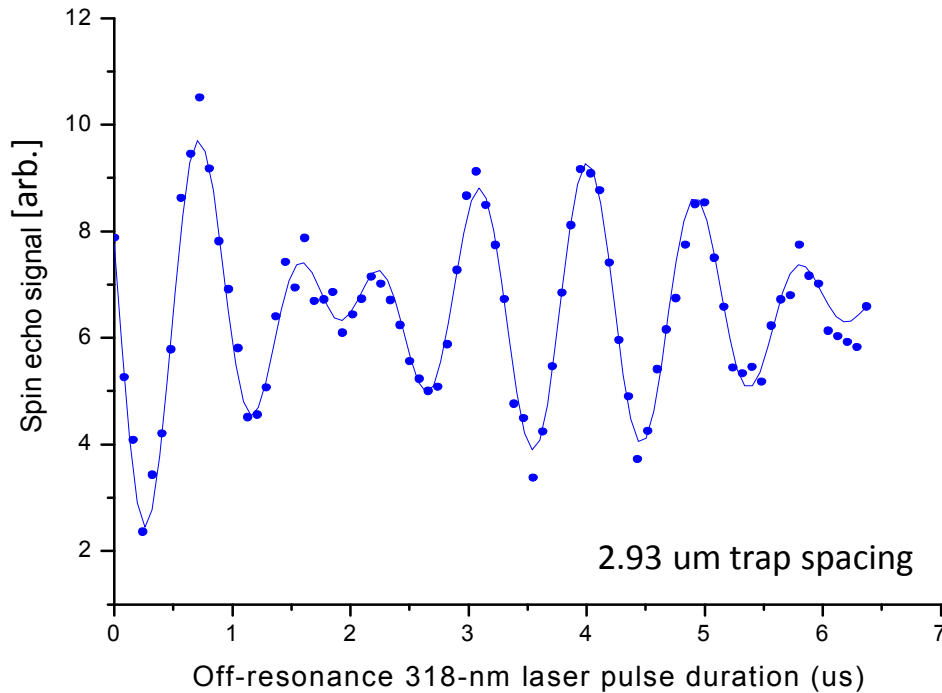


# First evidence of Rydberg-dressed interaction

Microwave transition is via Raman laser

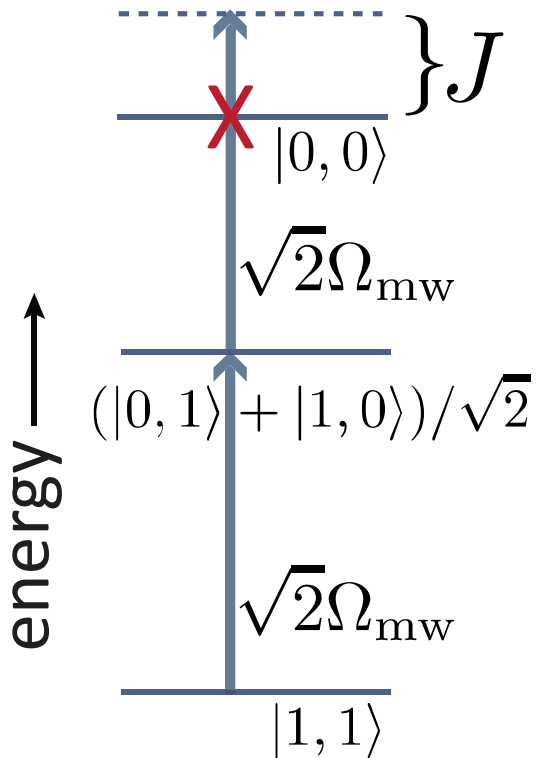


318-nm laser dressed spin echo sequence

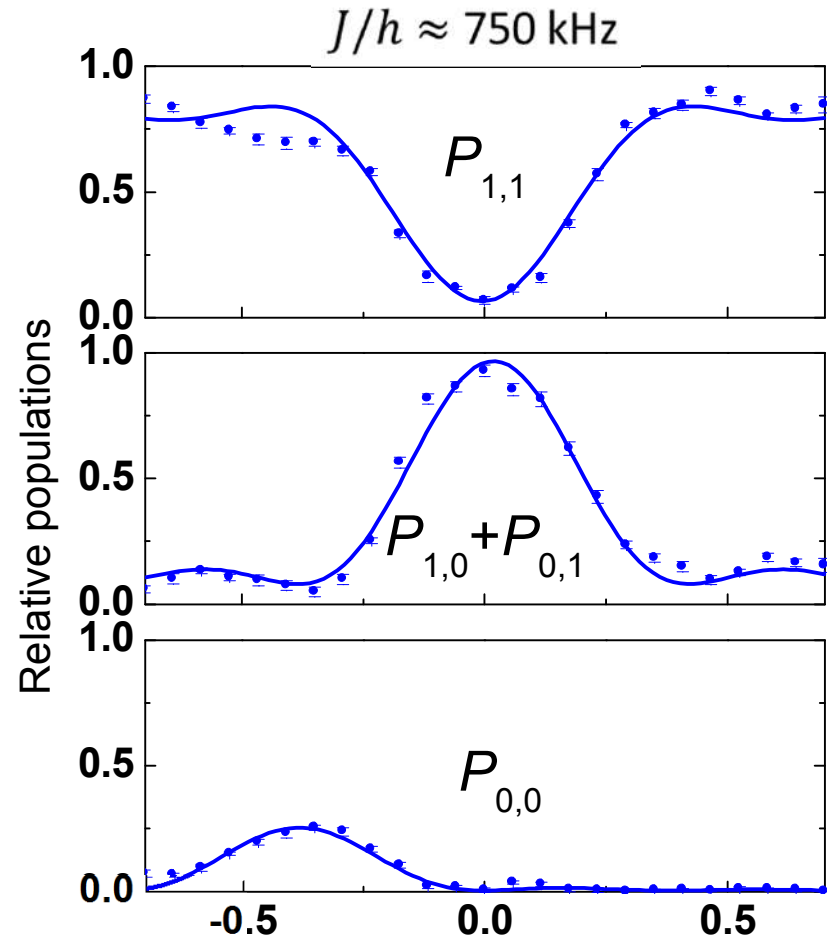


A frequency beat note is generated if  $\omega_1 \neq \omega_2$

# Two-qubit microwave resonances



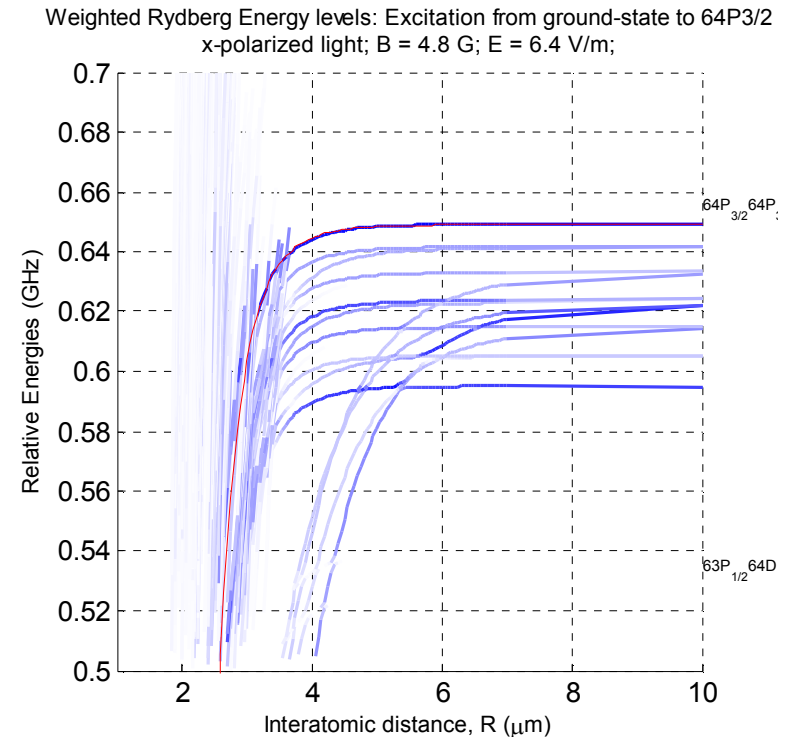
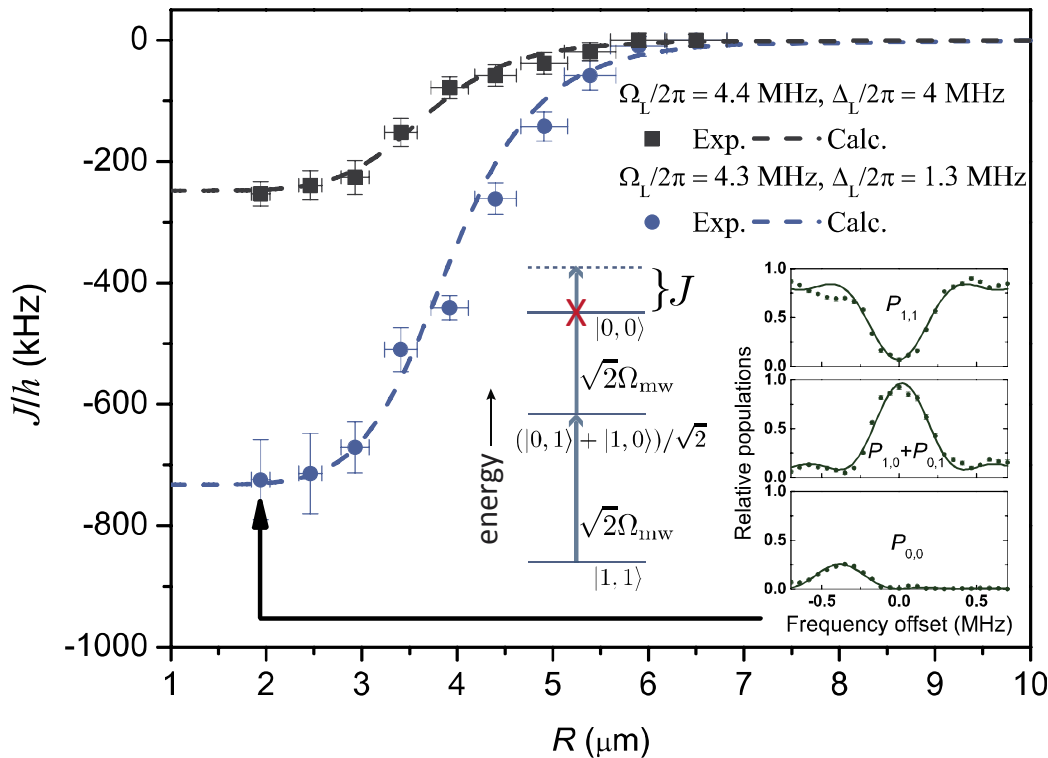
$P_{1,1}$ ,  $P_{1,0}$ ,  $P_{0,1}$ , and  $P_{0,0}$  denote relative populations of state  $|1,1\rangle$ ,  $|1,0\rangle$ ,  $|0,1\rangle$ , and  $|0,0\rangle$ .



Frequency offset (MHz)

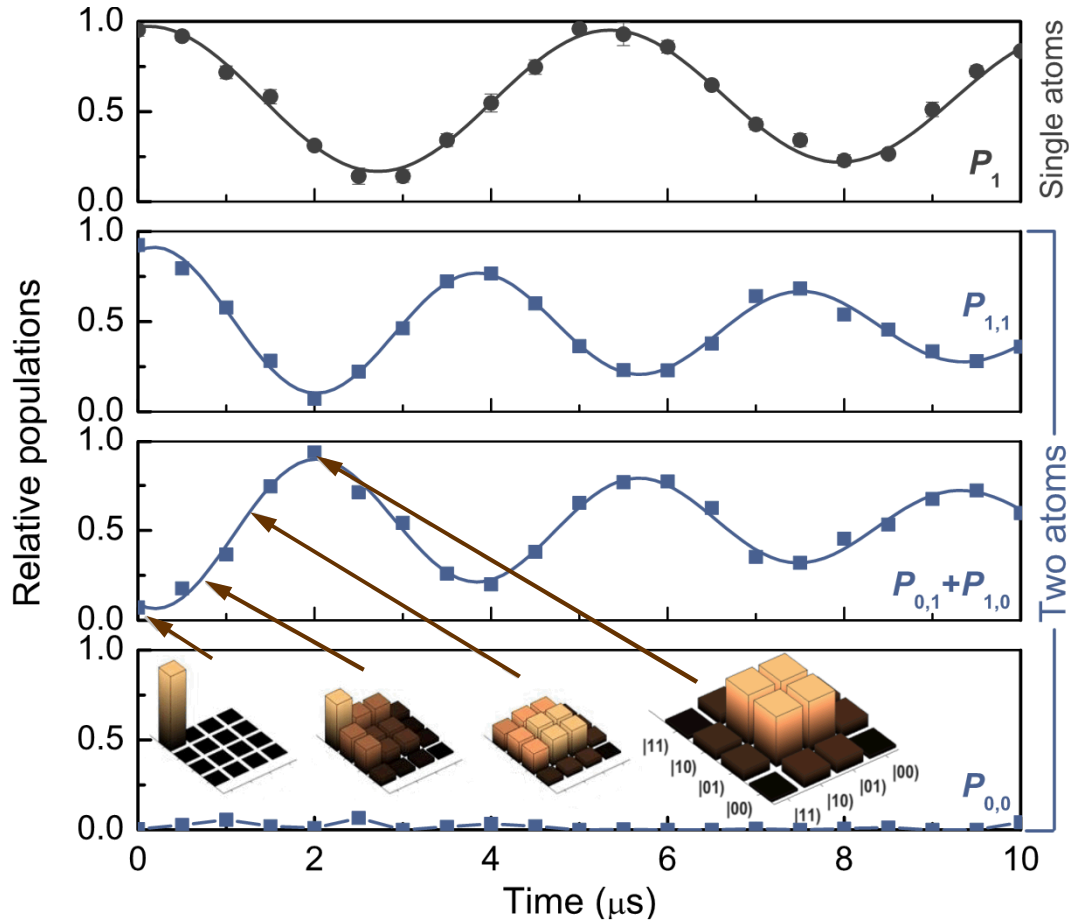
# $J$ vs. $R$ , no longer elusive

Direct measurement of two-qubit interaction strength  $J$  as a function of two-atom separation with two conditions.



# Producing Bell-state entanglement

Initial state is  $|1\rangle$  or  $|11\rangle$ , then apply 318-nm and Raman lasers  
 Experimental data with  $J/h \approx 750$  kHz



Single-atom Rabi oscillation:  $|1\rangle \leftrightarrow |0\rangle$

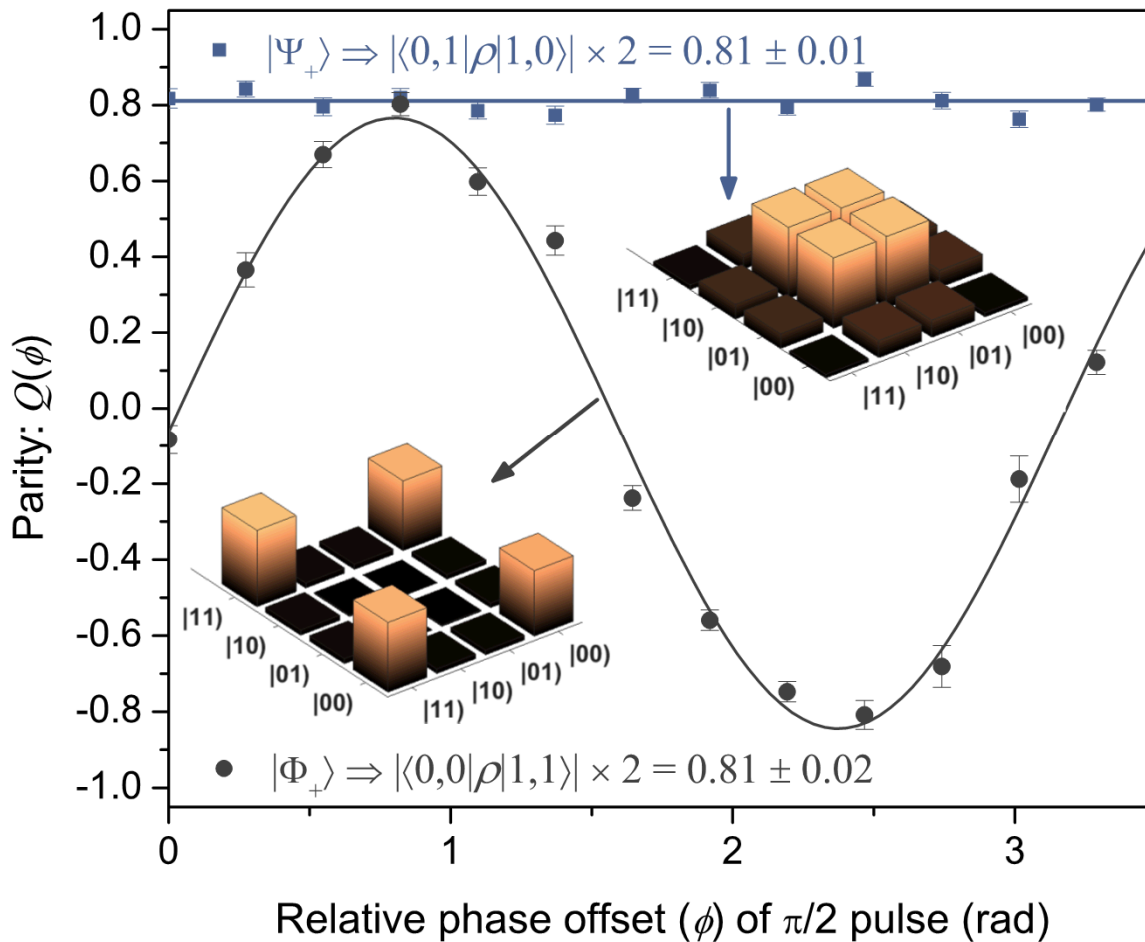
Two-atom Rabi oscillation:  $|11\rangle \leftrightarrow (|10\rangle + |01\rangle)/\sqrt{2}$

- $\sqrt{2}$  times faster
- No significant population being transferred to  $|00\rangle$
- Bell state  $|\Psi_+\rangle$  is produced at  $t = \pi/\sqrt{2}\Omega_{mw}$

Process occurs entirely and directly in the ground state

# Entanglement Fidelity $\geq 81\%$

Verify the entanglement via parity measurements



Prepare two Cs atoms in Bell state  $|\Psi_+\rangle$  or  $|\Phi_+\rangle$

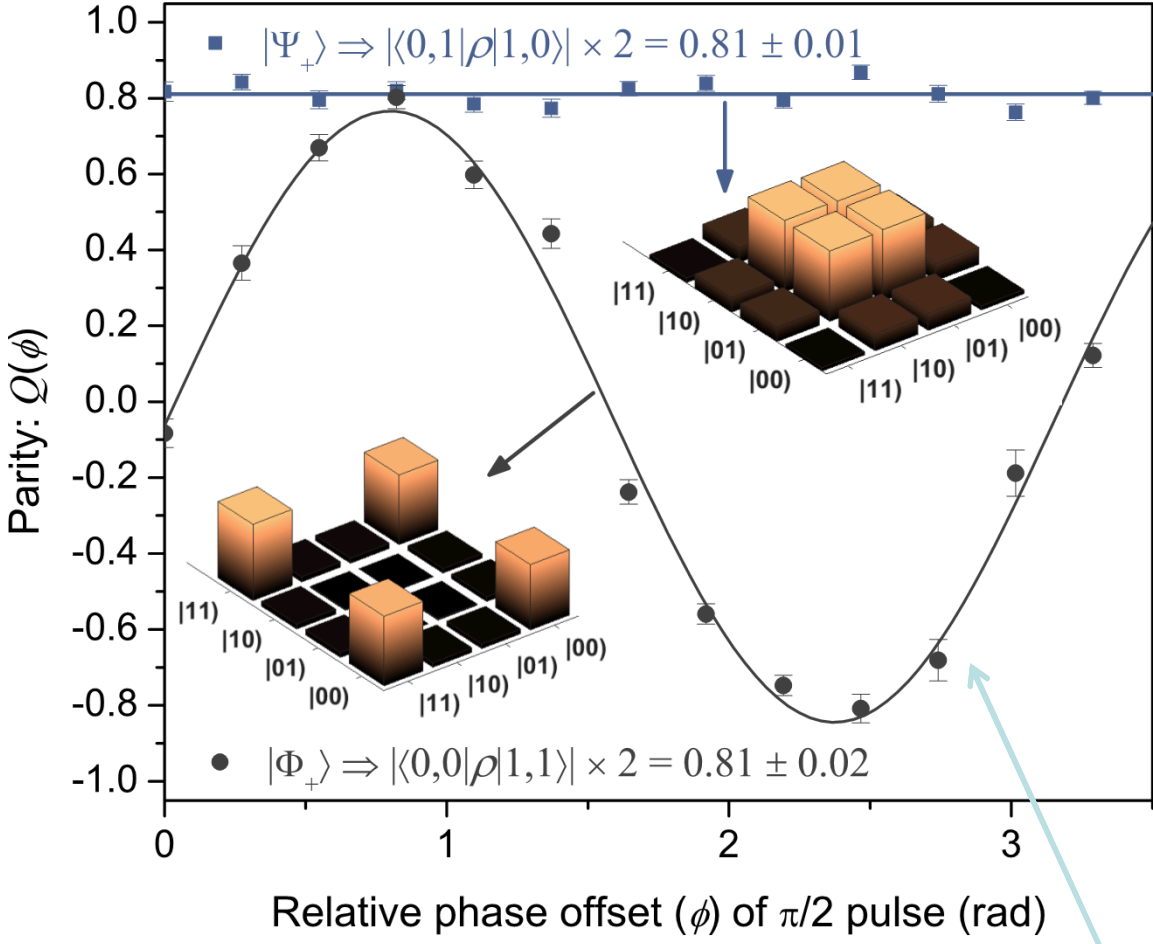
Apply a global  $\pi/2$  rotation with a given phase

Perform parity measurement  $Q = P_{11} + P_{00} - (P_{01} + P_{10})$

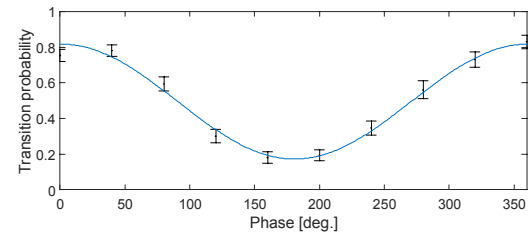
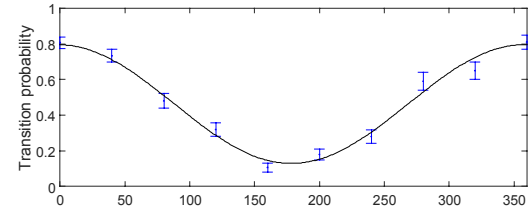
Obtain the two-qubit entanglement fidelity  $F$ , where  $Q \leq F \leq 1$ .



# Application to metrology

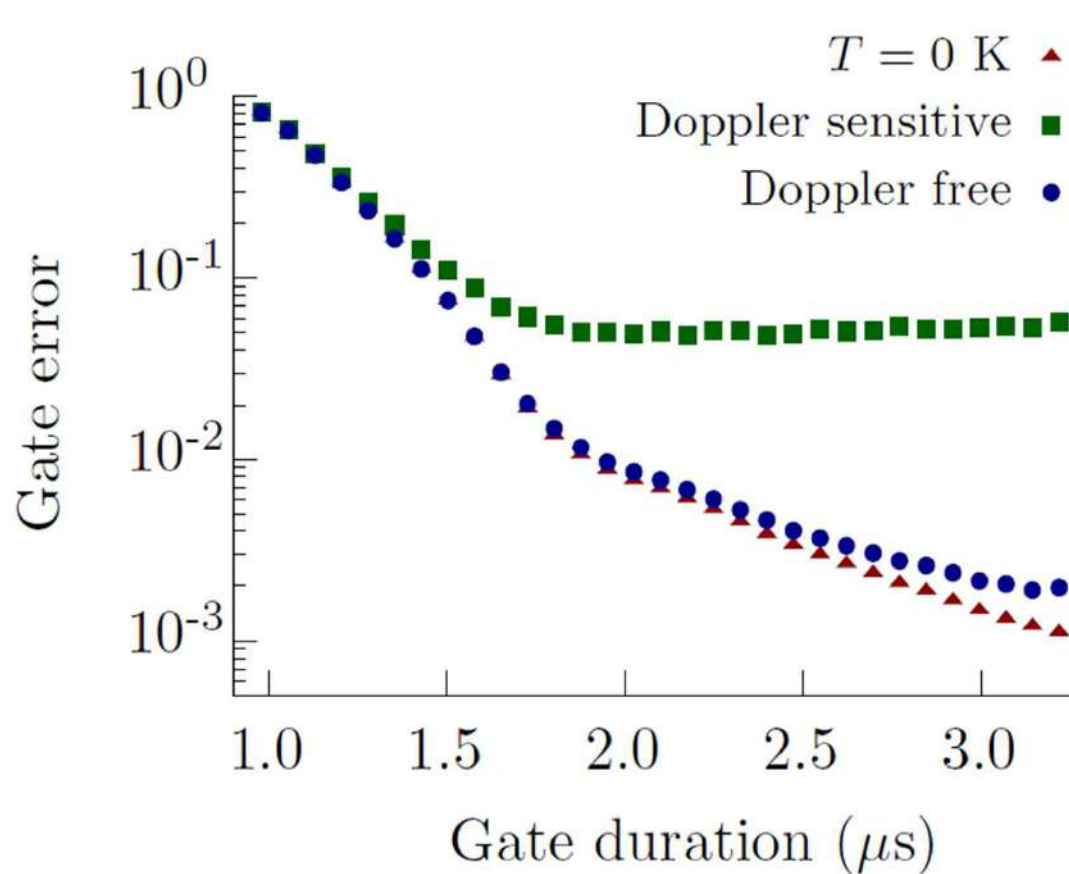


## 2-atom interferometer



Cat state 2x response to phase

# Simulated CPHASE gate fidelities



$\Omega = 0 \rightarrow 3 \text{ MHz}$   
 $\Delta/2\pi = 6 \rightarrow 0 \text{ MHz}$   
 $\Gamma = 3.7 \text{ kHz}$   
 $T = 16 \mu\text{K}$

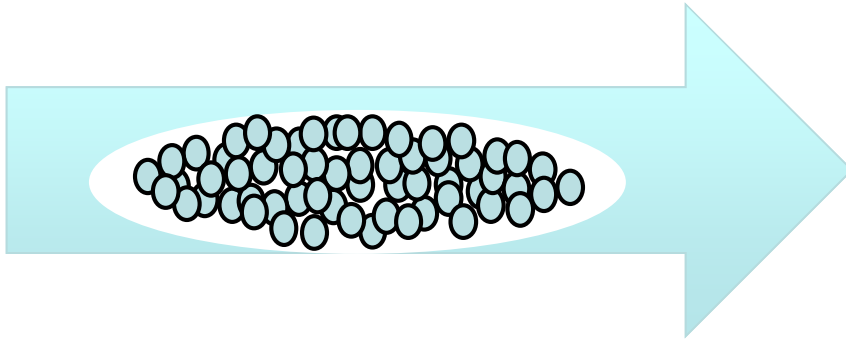
- Motional errors set a high floor on error for the original scheme.
- The Doppler-free scheme is limited by the much smaller photon scattering rate.
- Entanglement fidelity expected to be even larger

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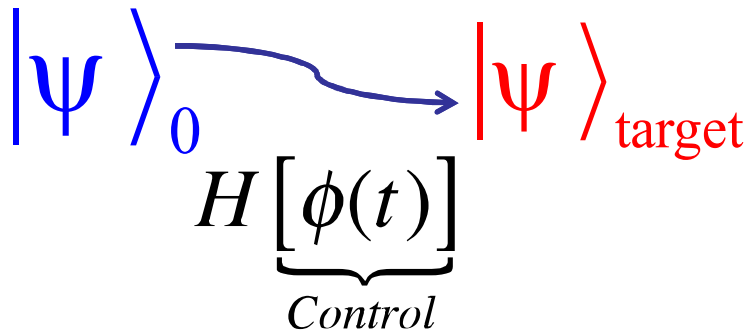


# Quantum Control of Ensembles

Symmetrically couple ensemble of atoms localized with Rydberg blockade radius



Optimal Control

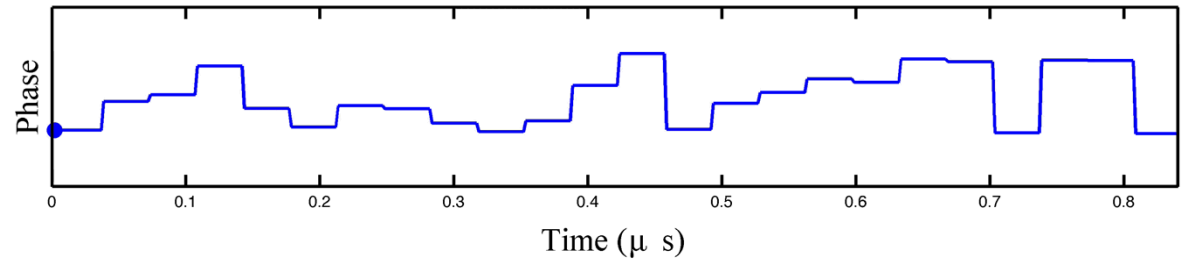


For  $n$  atoms

$$H = \sum_n \left[ \frac{\Omega_{\mu w}}{2} \left( e^{i\phi(t)} |0\rangle\langle 1| + e^{-i\phi(t)} |1\rangle\langle 0| \right)^{(n)} + \frac{\Omega_R}{2} (|1\rangle\langle r| + |r\rangle\langle 1|)^{(n)} + \Delta |r\rangle\langle r|^{(n)} \right] + V_{dd} \sum_{n \neq m} |r\rangle\langle r|^{(n)} |r\rangle\langle r|^{(m)}$$

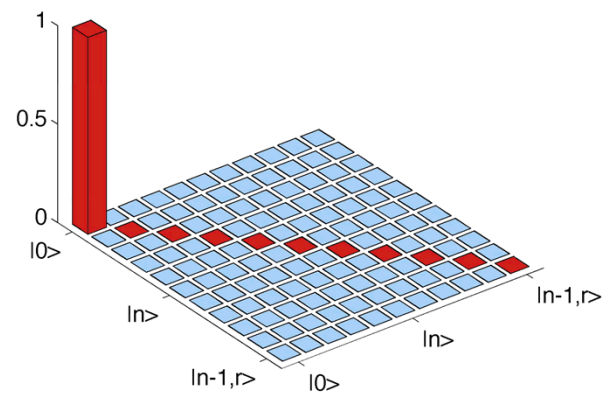
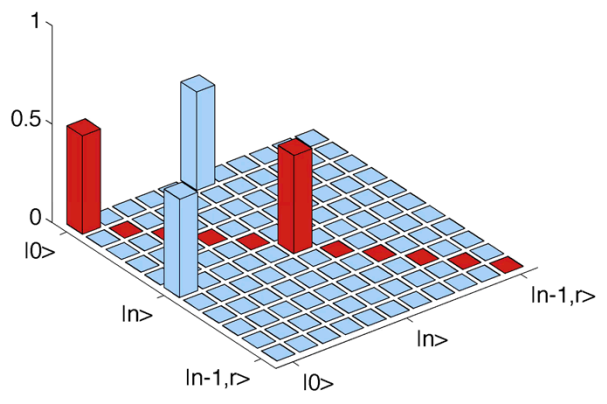


# Example: A 5-atom "Cat State"



$\rho$  target

$\rho$  evolved



$$|\psi_{cat}\rangle = \frac{1}{\sqrt{2}} (|0\rangle|0\rangle|0\rangle|0\rangle|0\rangle + |1\rangle|1\rangle|1\rangle|1\rangle|1\rangle)$$

$$|\psi(t)\rangle$$



# Summary and outlook

- Ensemble exchange technique potentially useful for deployed inertial sensors and Gradiometer survey pathfinder facility
- We have demonstrated an effective ground-state interaction  $J/h \sim 1$  MHz via the Rydberg dressing technique
- We have shown neutral atom entanglement with a fidelity  $\geq 81(2)\%$
- With two-atom survival of 74% and  $10 \text{ s}^{-1}$  data rate, we produce 6 entangled pairs per second
- Multi-atom entanglement can be achieved based a similar approach or with optimal control
- We are investigating atom interferometry with cat states and  $N > 2$

Team Members:

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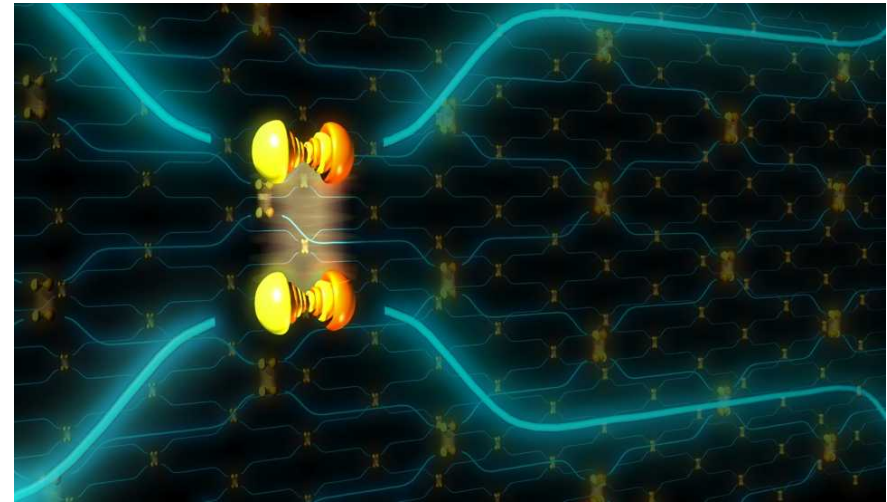
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Aaron Hankin (Sandia, currently at NIST)

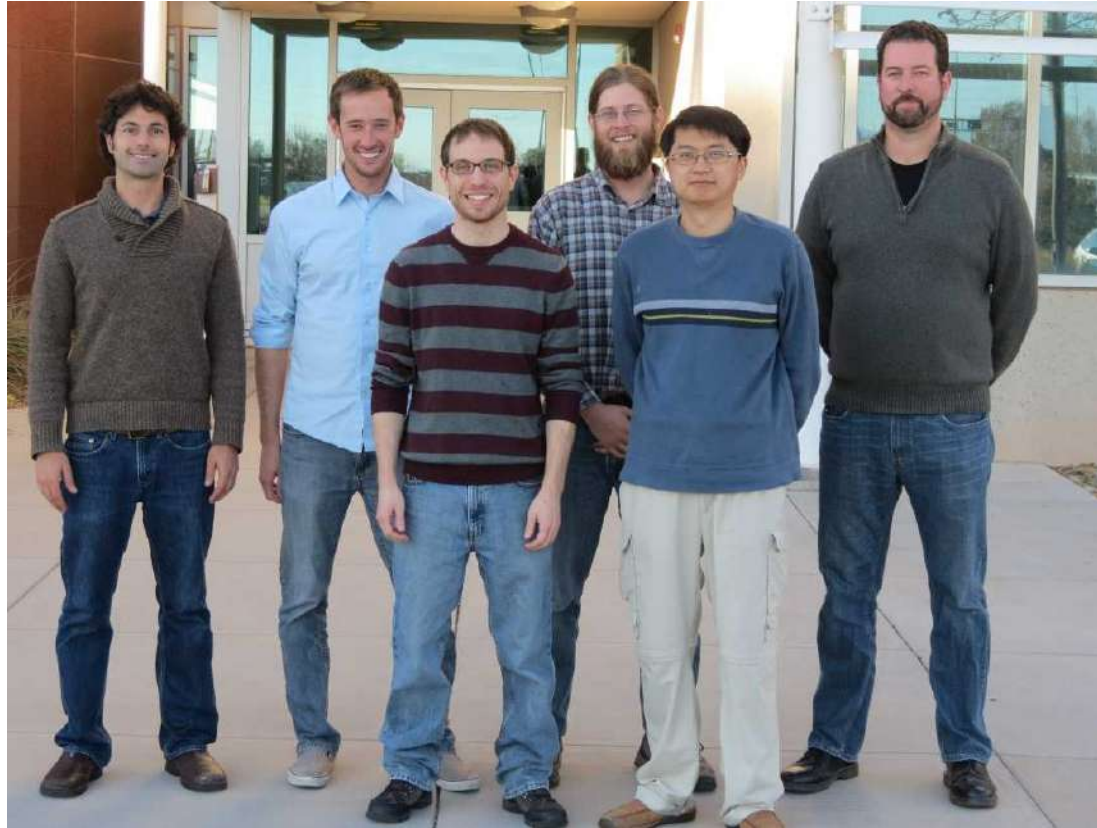
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