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CERN Theory Division, PSI & UZH

## Heavy Flavours -- Theory

LHCP, Paris, 10.06.2021 (remote)

# Outline

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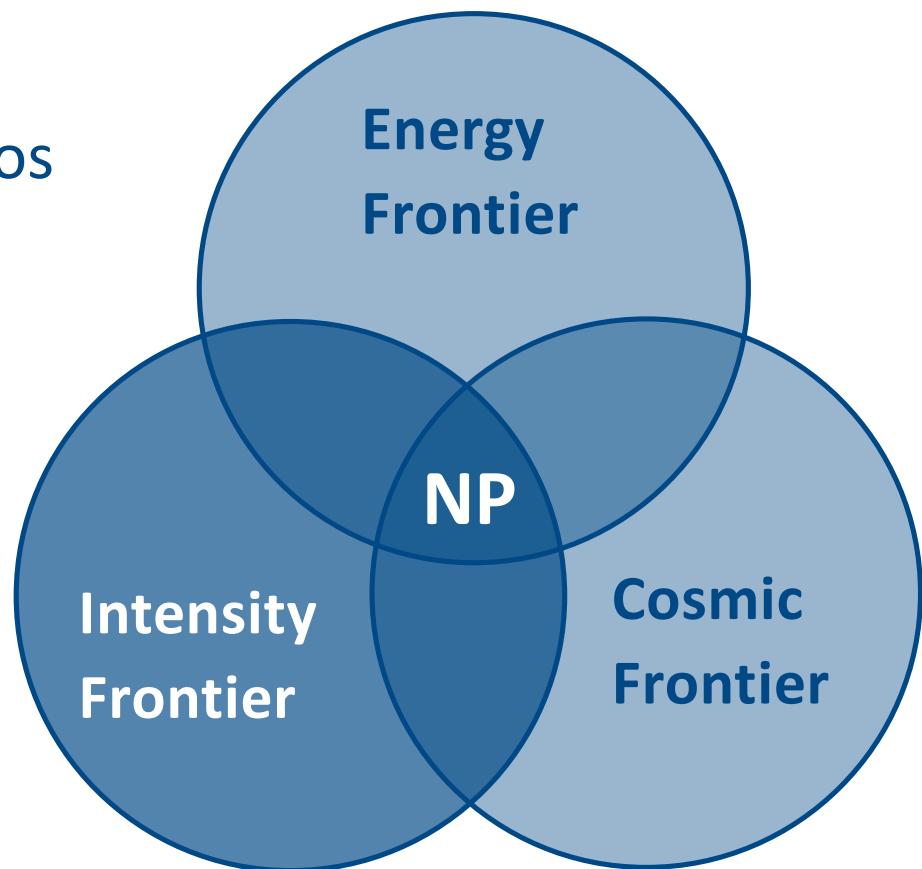
- Introduction
- Hints for Lepton Flavour Universality Violation
  - Semi-leptonic B decays
  - Anomalous magnetic moment of the muon
  - Cabibbo Angle Anomaly
- Explanations of the Anomalies
- Common explanations
- Conclusions and outlook

# Introduction

# Discovering New Physics

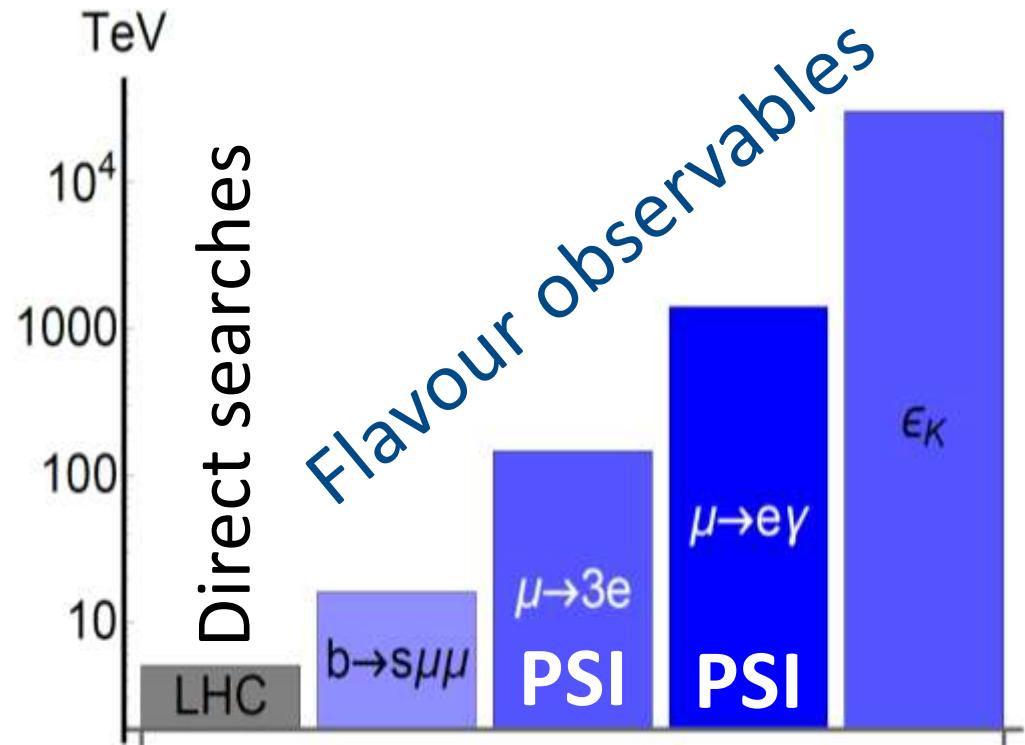
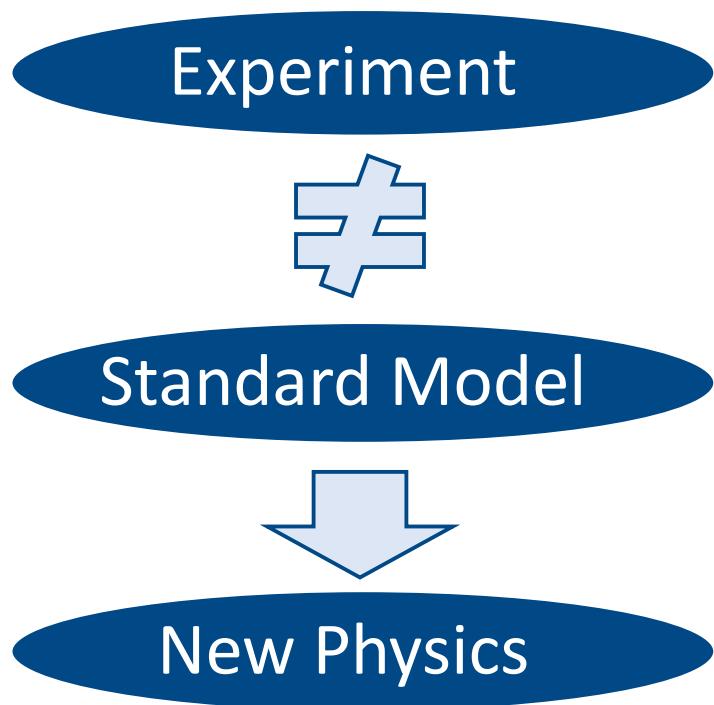
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- Cosmic Frontier
  - Cosmic rays and neutrinos
  - Dark Matter
  - Dark Energy
- Energy Frontier
  - LHC
  - Future colliders
- Intensity Frontier
  - Flavour
  - Neutrino-less double- $\beta$  decay
  - Test of fundamental symmetries
  - Proton decay



# Finding New Physics with Flavour

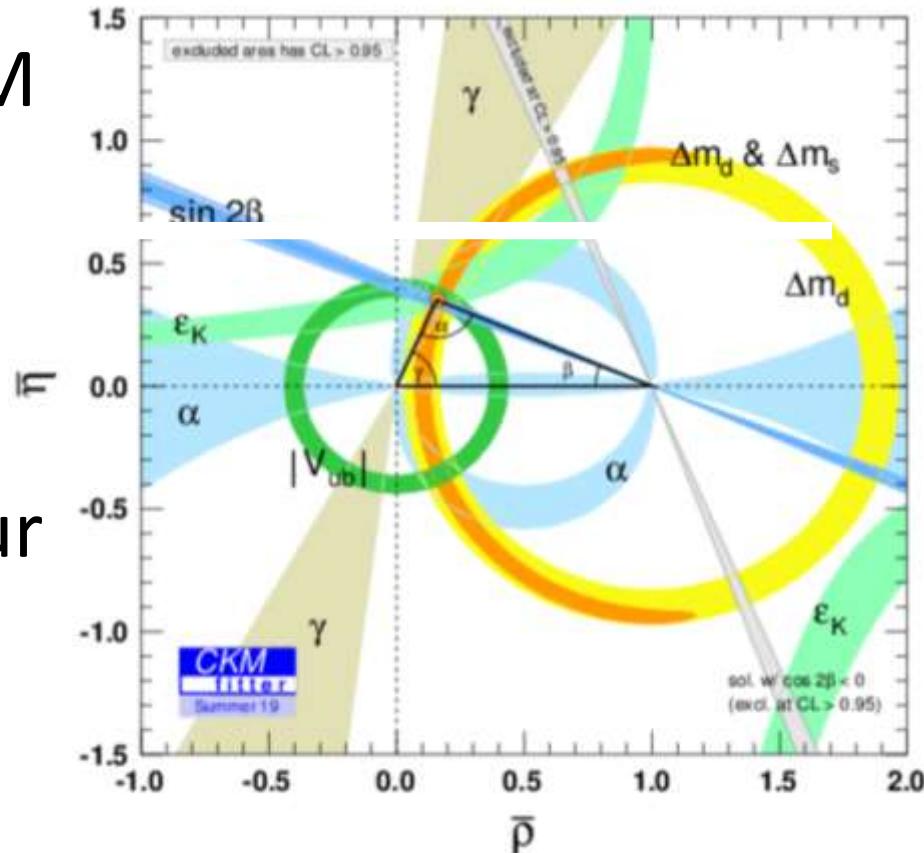
- At colliders one produces many (up to  $10^{14}$ ) heavy quarks or leptons and measures their decays into light flavours



Flavour observables probe higher energy scales than collider searches

# Global Fit to the CKM Matrix

- Tree-level determinations of CKM elements (with light leptons) agree with  $\Delta F=2$  processes
- Picture of CKM Flavour violation established, but sub-leading NP possible



Still room for New Physics effects of  $O(10\%)$

# Lepton Flavour (Universality) Violation

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In the Standard Model accidental symmetry:

- Lepton Flavour is conserved  
(for vanishing neutrino masses)
  - Excellent approximation: branching ratios smaller than  $10^{-45}$ 
    - ➡ Any observation proves **new physics**
- Gauge Interactions are Lepton Flavour Universal
- Only Yukawa couplings distinguish flavors
  - ➡ Very small effect (except for phase space)

LFUV is an excellent probe of the SM

# Overview on hints for Lepton Flavour Universality Violation

# LFUV in $b \rightarrow s\ell^+ \ell^-$

$$R(K) = \frac{B \rightarrow K \mu^+ \mu^-}{B \rightarrow K e^+ e^-}$$

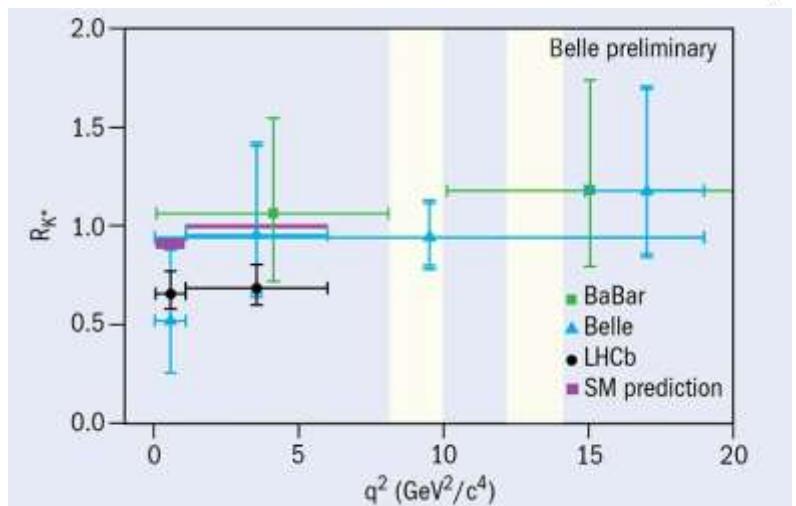
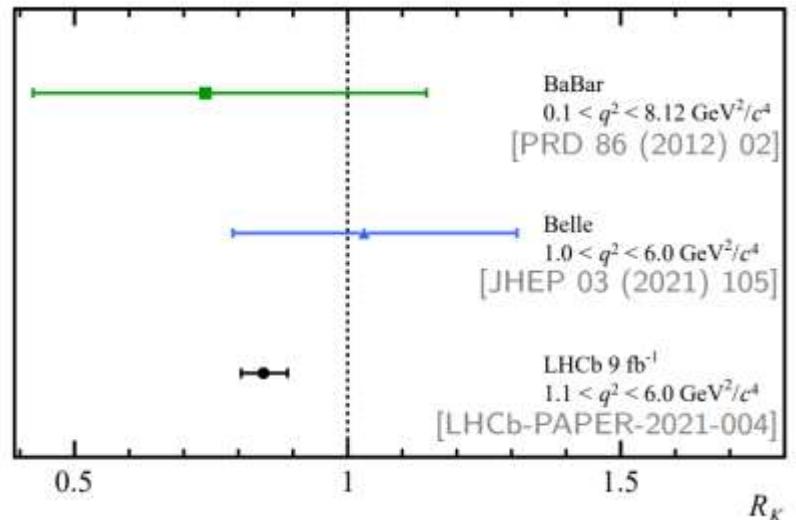
$$R(K^*) = \frac{B \rightarrow K^* \mu^+ \mu^-}{B \rightarrow K^* e^+ e^-}$$

- Muon and electron masses can be neglected

 **Clean prediction**

- Supported by

$$\frac{\Lambda_b \rightarrow K p \mu^+ \mu^-}{\Lambda_b \rightarrow K p e^+ e^-} = 0.86^{+0.14}_{-0.11} \pm 0.05$$



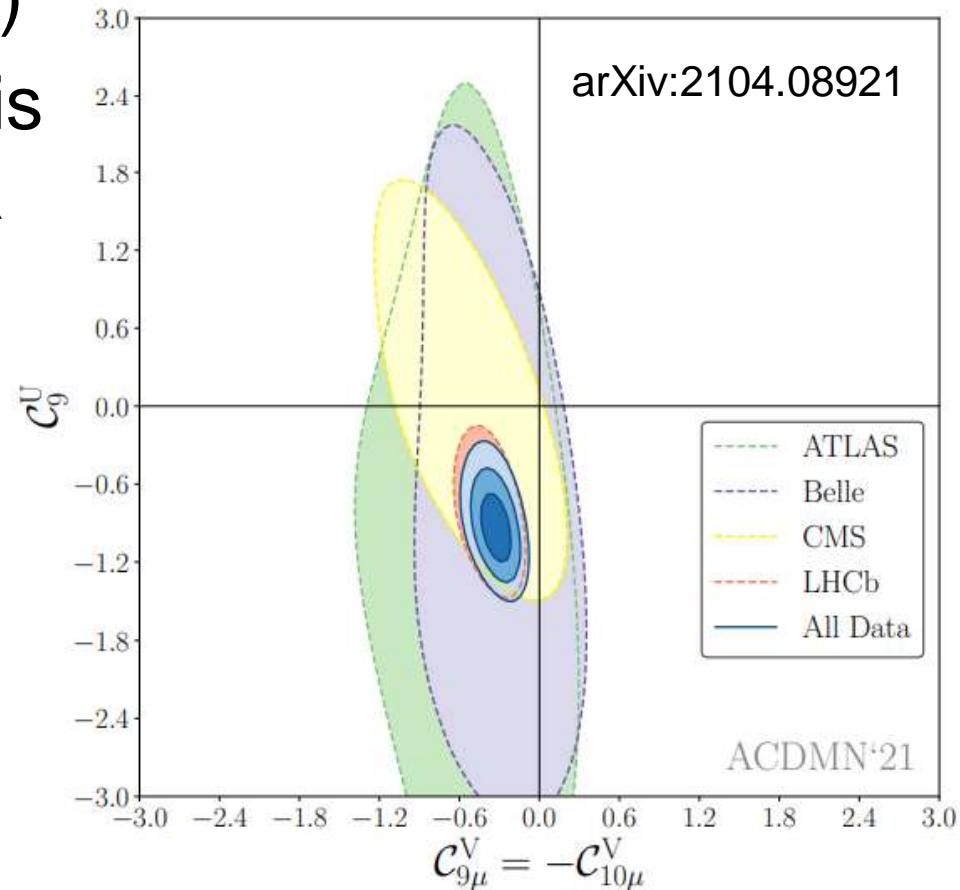
LFUV in B decays  $>4\sigma$

# Global Fit to $b \rightarrow s\mu^+\mu^-$ Data

- Perform global model independent fit to include all observables ( $\approx 180$ )
- Several NP hypothesis give a good fit to data significantly preferred over the SM hypothesis

$$O_9 = \bar{s} \gamma^\mu P_L b \bar{l} \gamma_\mu l$$

$$O_{10} = \bar{s} \gamma^\mu P_L b \bar{l} \gamma_\mu \gamma^5 l$$

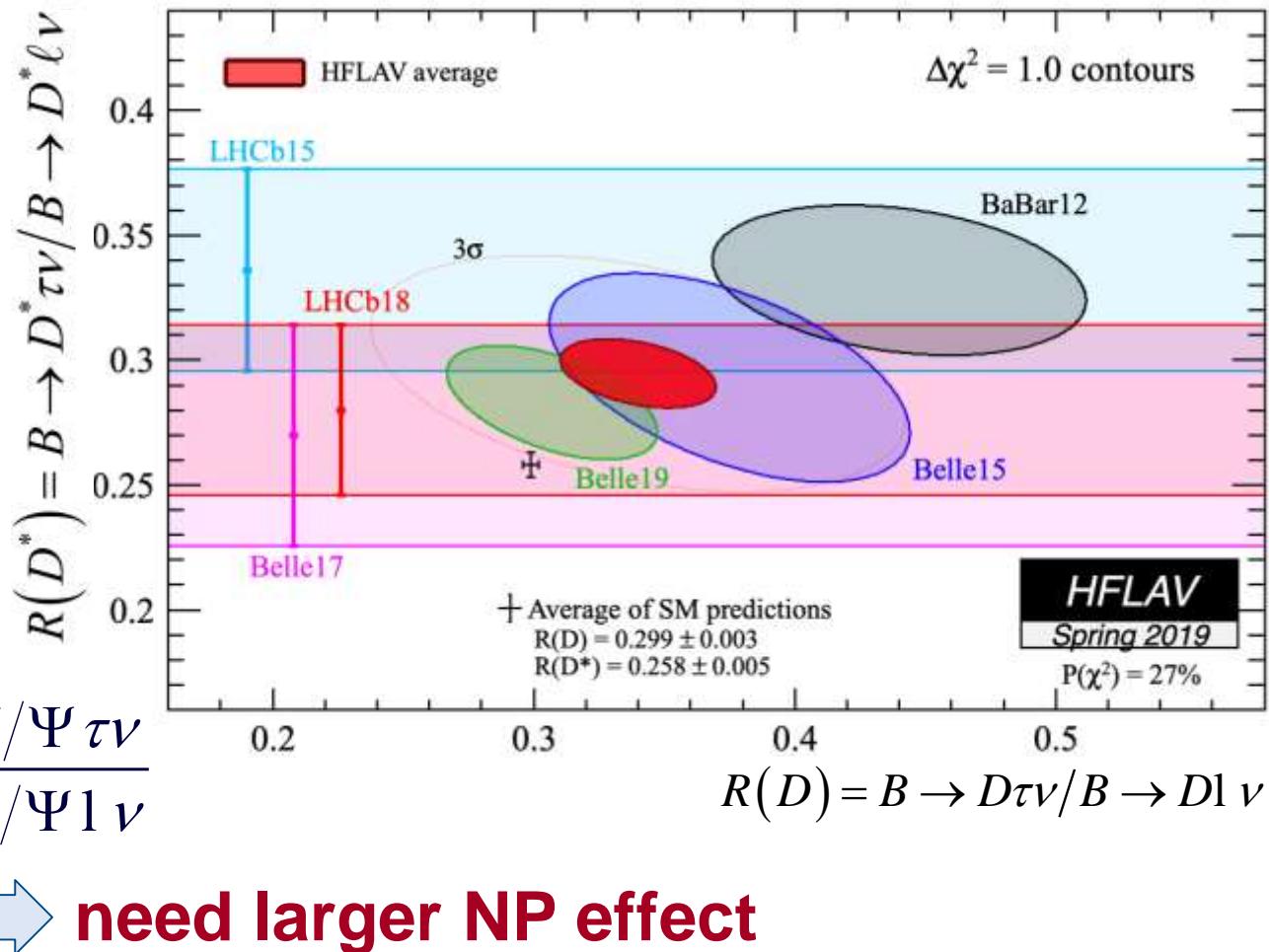


Fit is  $>7 \sigma$  better than the SM

# b $\rightarrow$ c $\tau\nu$ Transitions

- LFU test of the charged current
- Tau mode consistently enhanced
- Supported by

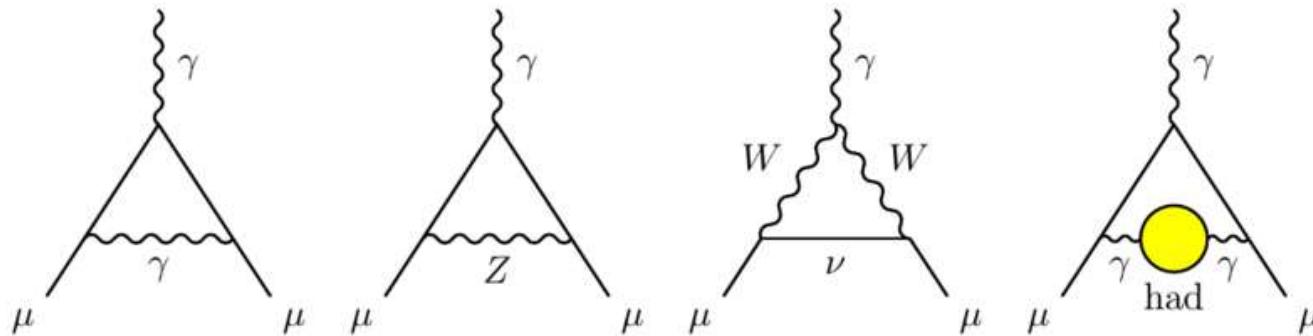
$$R(J/\Psi) = \frac{B_c \rightarrow J/\Psi \tau\nu}{B_c \rightarrow J/\Psi l\nu}$$



- Tree-level **need larger NP effect**

O(10%) constructive preferred effect at 3 $\sigma$

# Muon Anomalous Magnetic Moment



- Theory prediction intricate (hadronic effects)  
 $\Delta a_\mu = (251 \pm 49) \times 10^{-11}$  T. Aoyama et al., arXiv:2006.04822
- Need NP of the order of the SM EW contribution
- Chiral enhancement necessary for heavy NP
- Soon more experimental results from Fermilab
- Vanishes for  $m_\mu \rightarrow 0$  **measure of LFUV**

4.2 $\sigma$  deviation from the SM prediction

# Cabibbo Angle Anomaly (CAA)

- Deficit in first row and first column CKM unitarity

$$|V_{ud}^2| + |V_{us}^2| + |V_{ub}^2| = 0.9985 \pm 0.0005$$

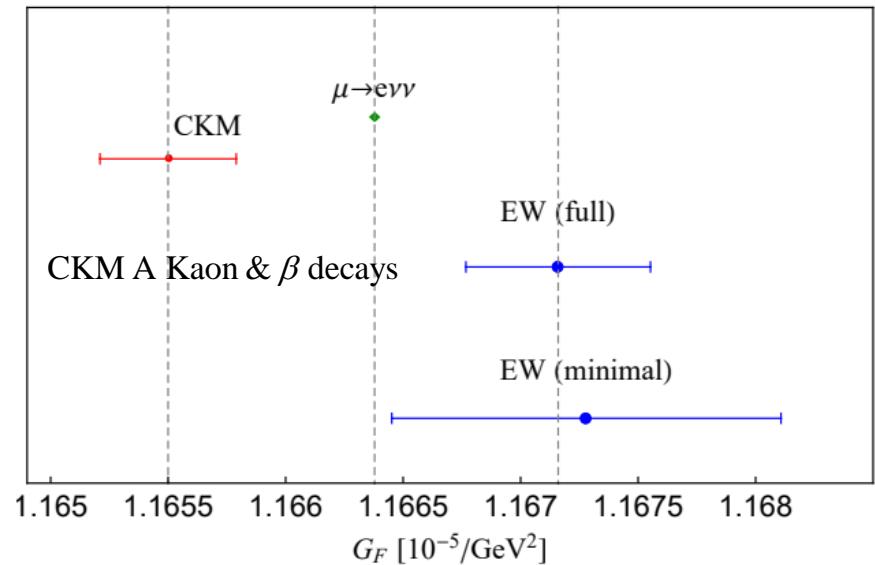
$$|V_{ud}^2| + |V_{cd}^2| + |V_{td}^2| = 0.9970 \pm 0.0018$$

(PDG)

AC, Hoferichter, Manzari, 2102.02825

- NP in the determination of  $V_{ud}$  from beta decays needed

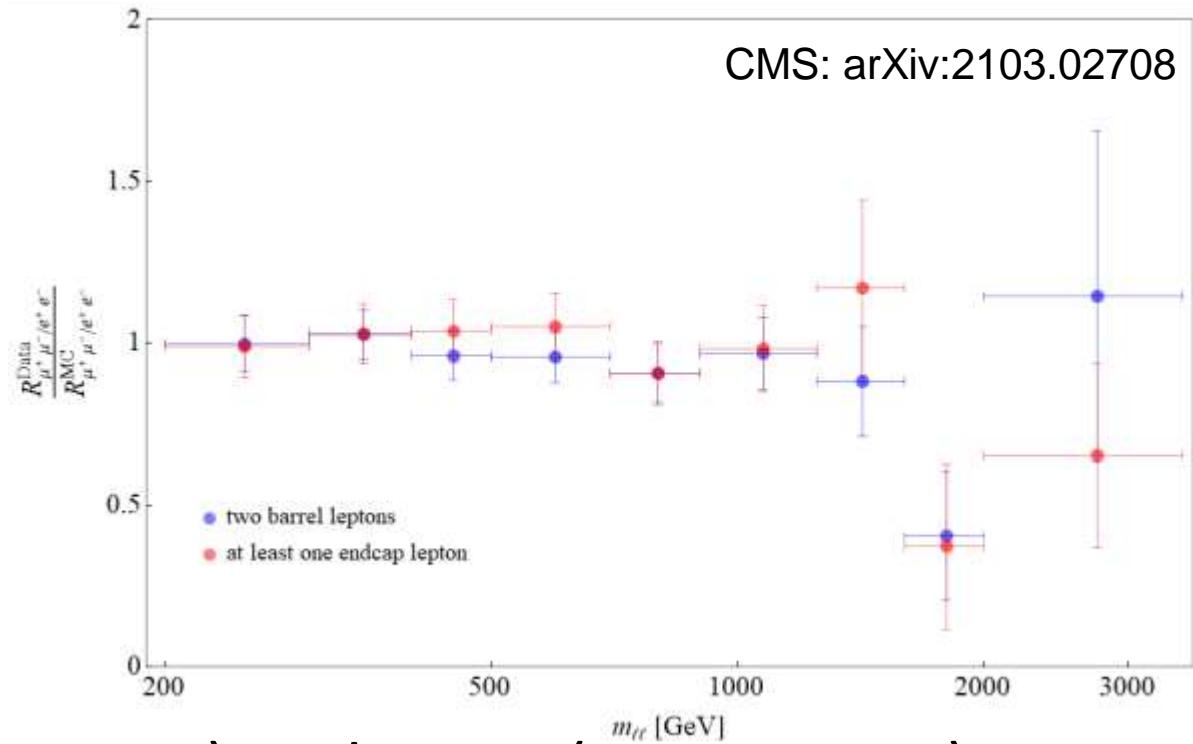
- Can be interpreted as
  - NP in beta decays
  - NP in the Fermi constant
  - LFUV (modified  $W\mu\nu$  coupling)



3 $\sigma$  tension

# Non-Resonant Di-Leptons

- Excess in di-electrons at  $m_{ee} > 1800\text{GeV}$
- Observed: 44 events
- Expected  $29.2 \pm 3.6$  events

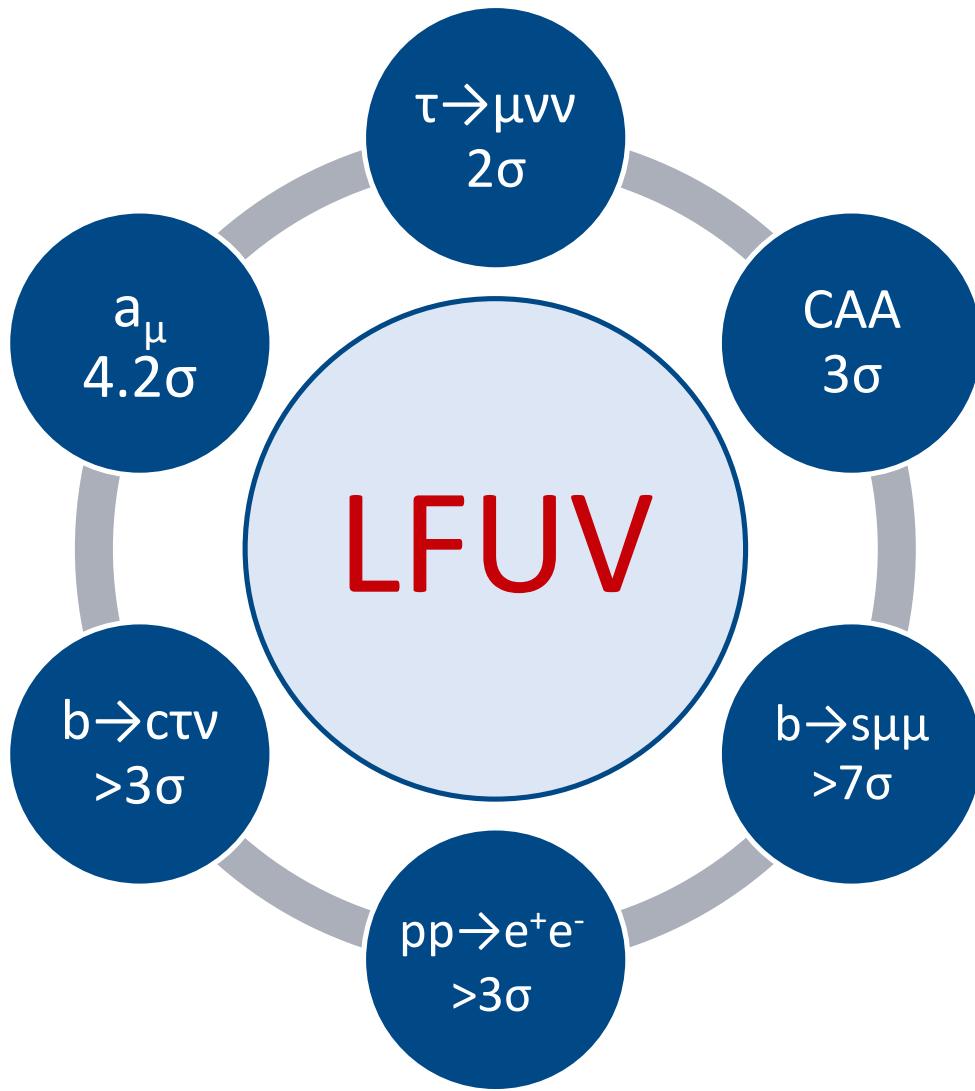


- Also ATLAS (2006.12946) and HERA (1902.03048) observe slightly more electrons than expected.
- No excess in muon data

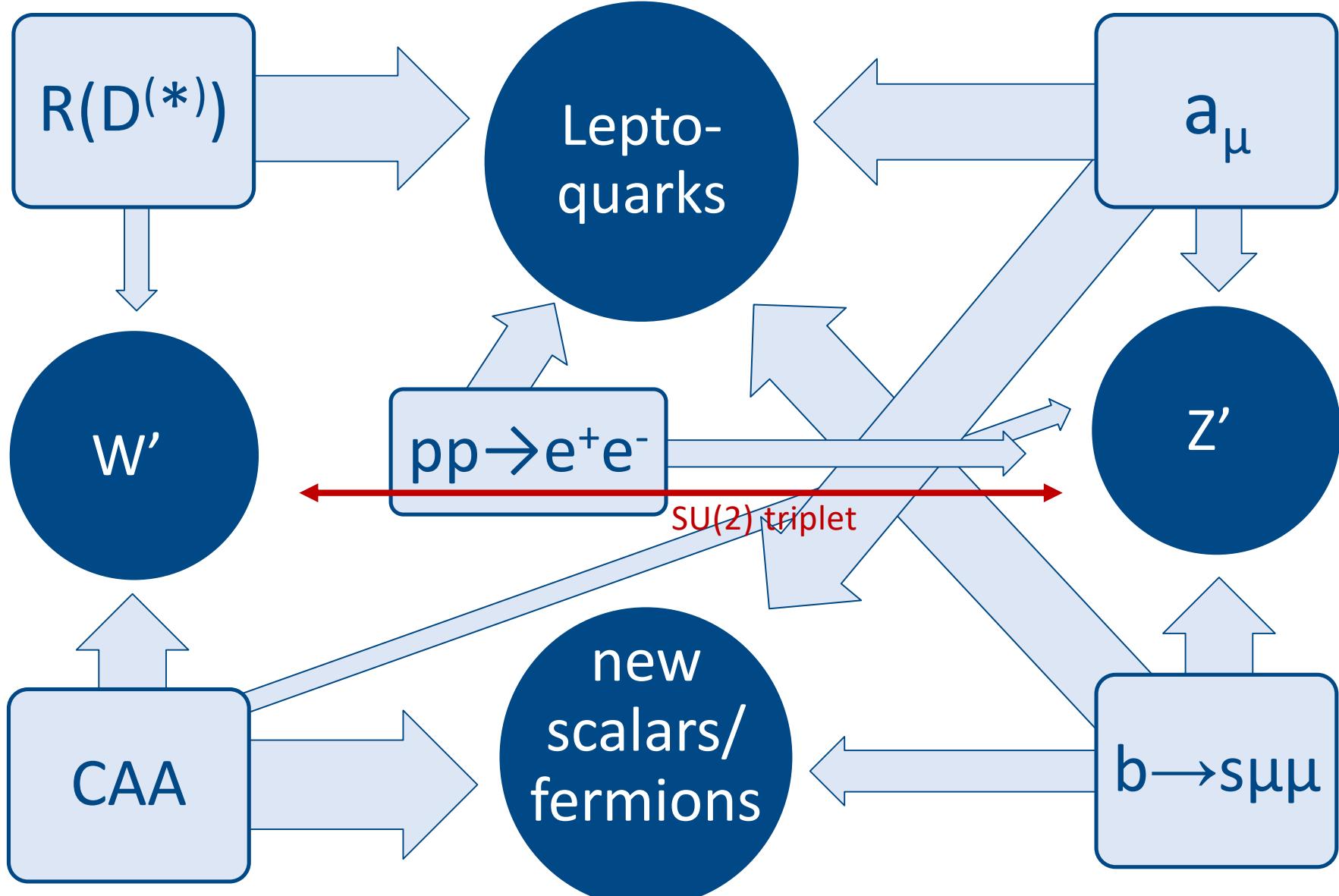
≈ $3\sigma$  hint for LFUV

# Hints for New Physics

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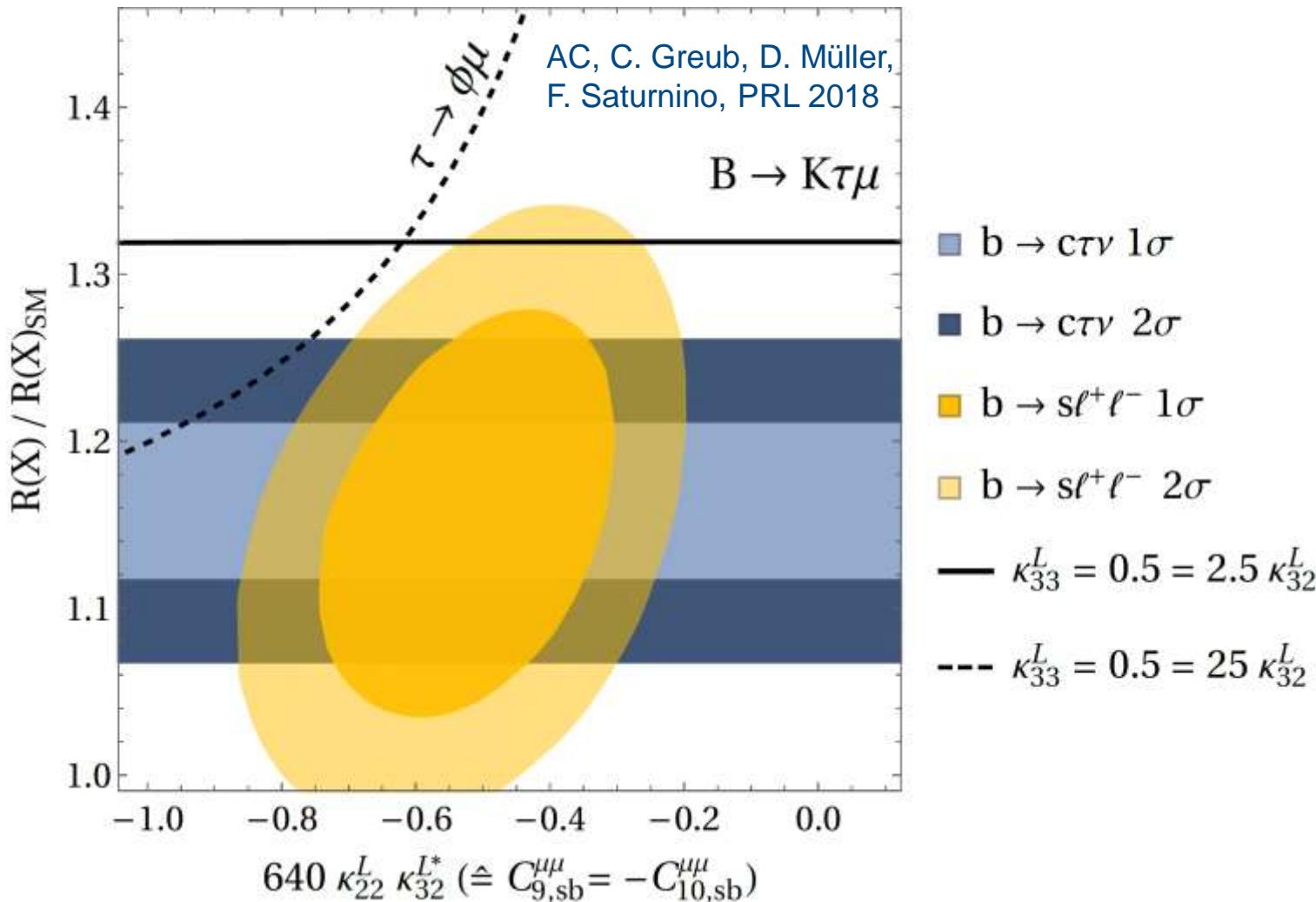


# New Physics Explanations



# Simultaneous Explanations

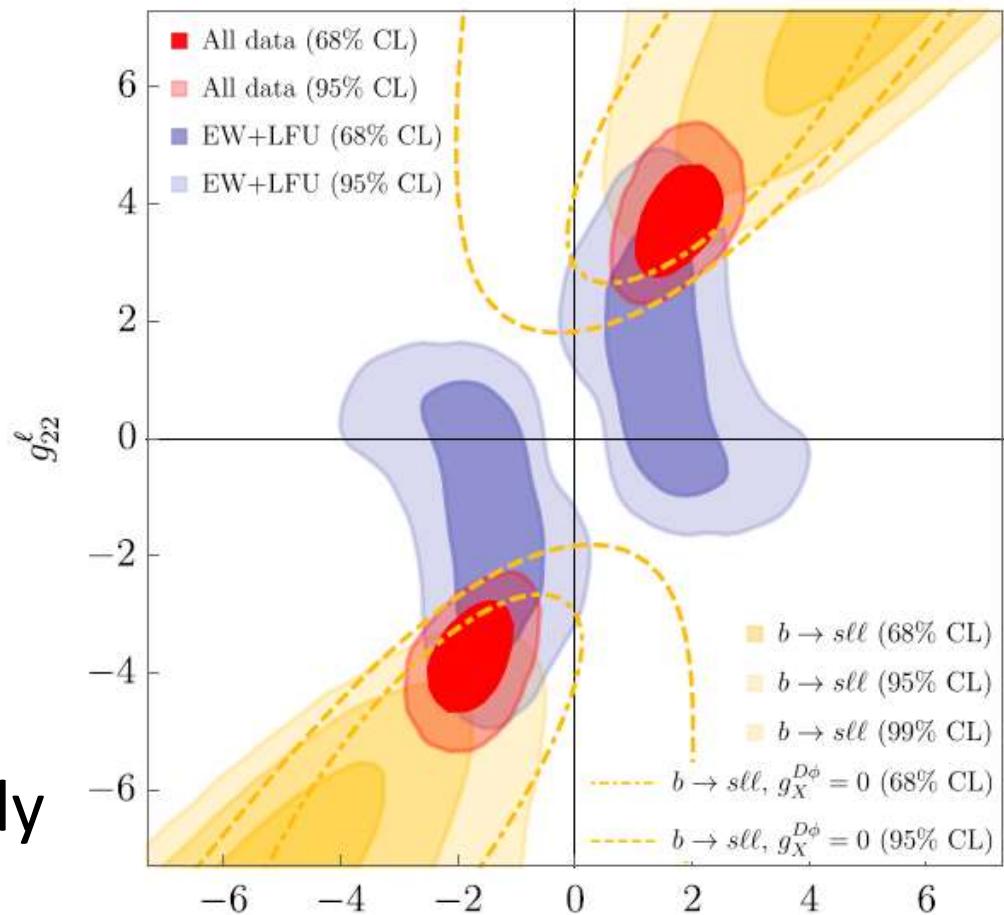
# $b \rightarrow s\ell\ell$ and $b \rightarrow c\tau\nu$ with a Vector Leptoquark



Pati-Salam LQ can explain the flavour anomalies

# Vector Triplet in the CAA & $b \rightarrow s\ell\ell$

- Region from EW fit overlaps with  $b \rightarrow s\ell\ell$  region
- Correlations between e.g.  $\pi \rightarrow \mu\nu/\pi \rightarrow e\nu$  and  $R(K^{(*)})$  are predicted
- Global fit significantly improved

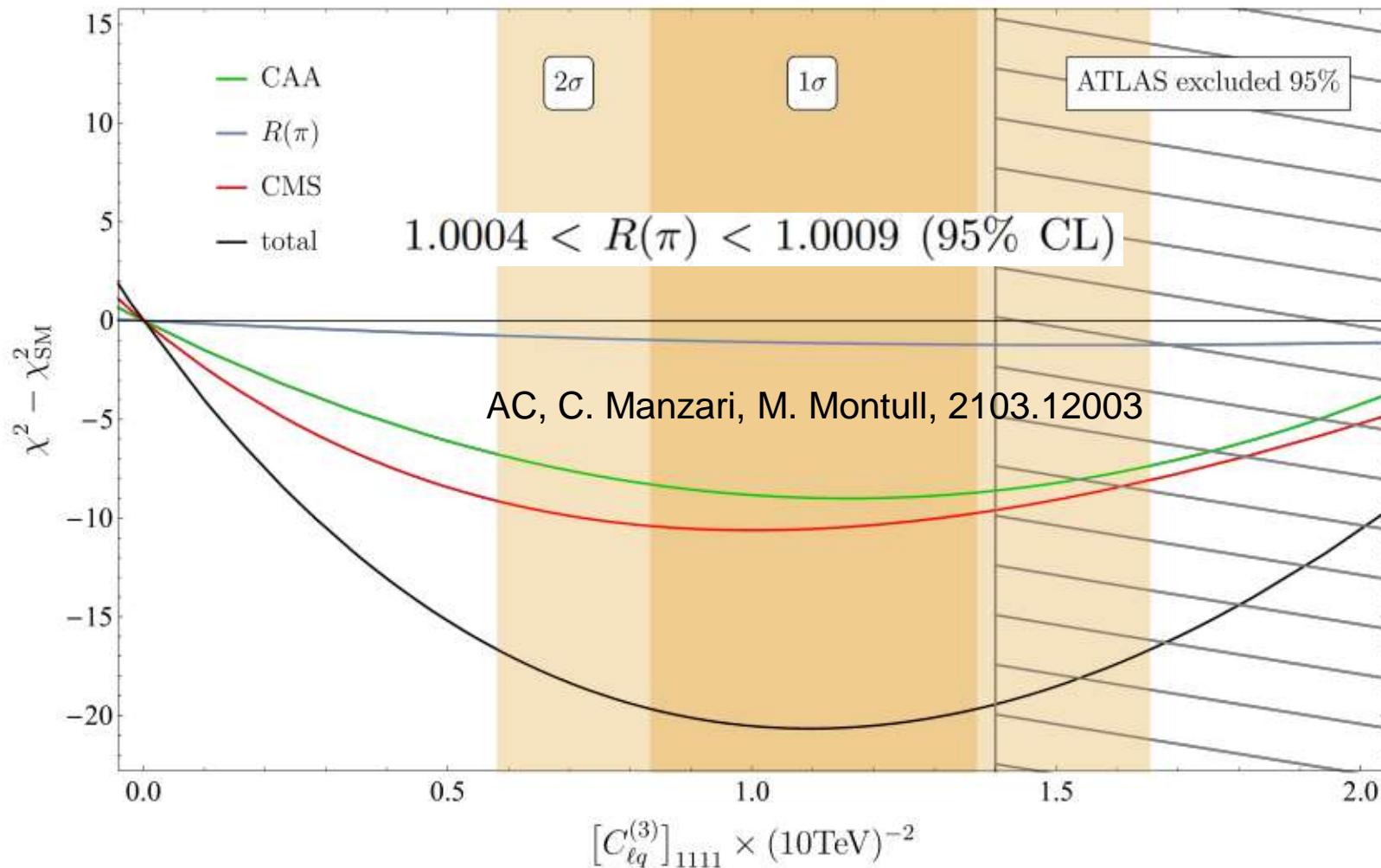


B. Capdevilla, AC, C. Manzari,  
M. Montull, PRD 2020

$g_{11}^{\ell}$

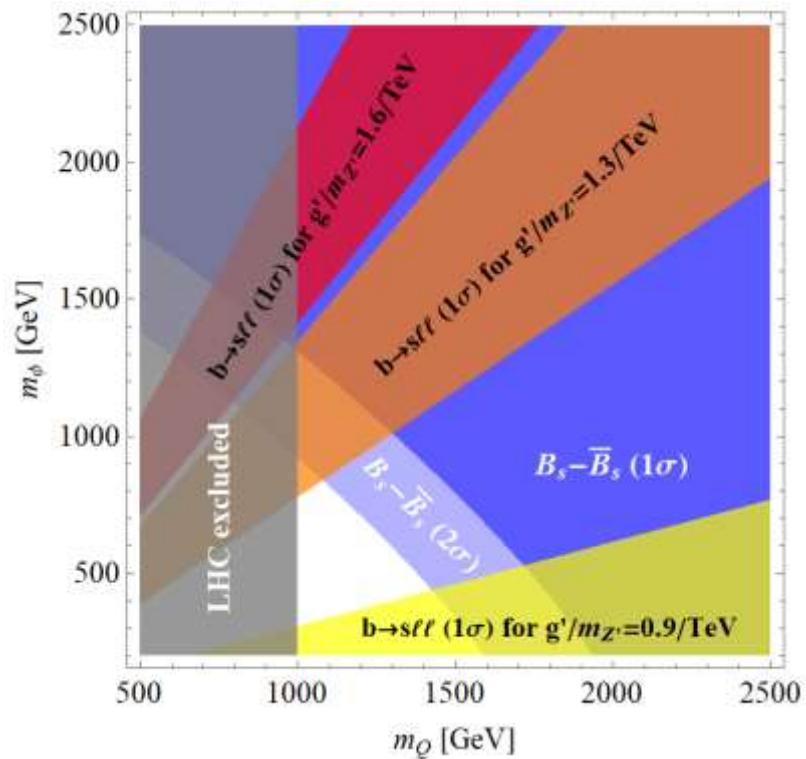
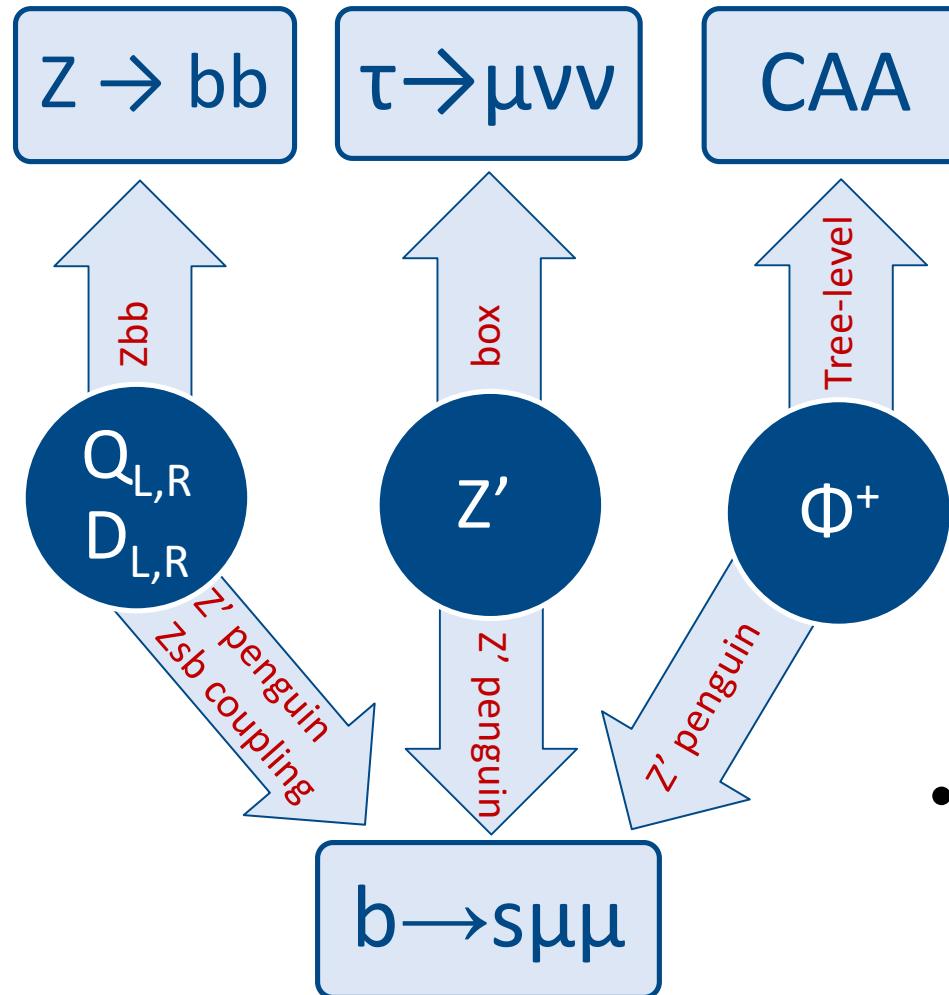
Common explanation possible

# CAA and Non-Resonant Di-Leptons



4.5 $\sigma$  better than SM, prediction for  $R(\pi)$

# Model for $b \rightarrow s\ell\ell$ , CAA, $Z \rightarrow bb$ and $\tau \rightarrow \mu\nu\nu$

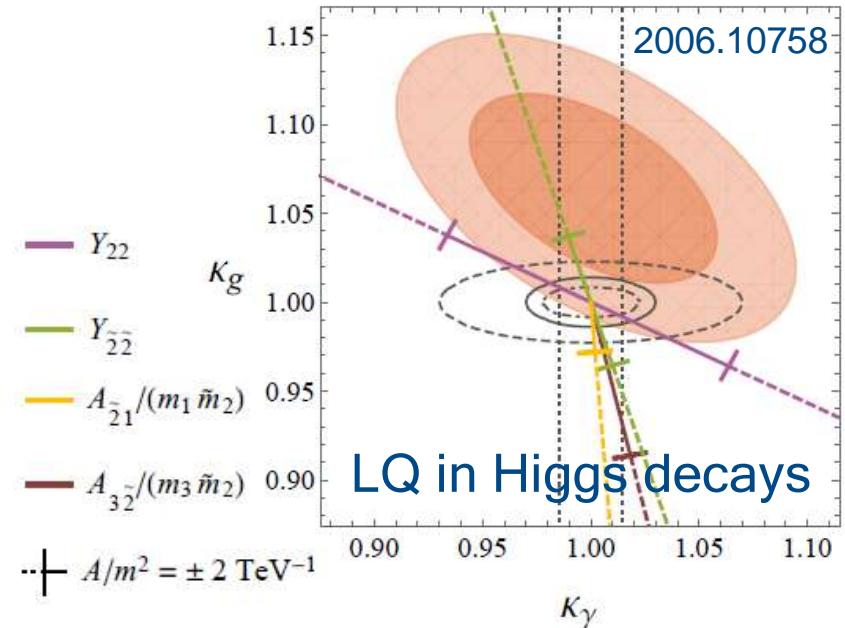


- $Z'$  penguin + modified Zsb coupling give very good fit to  $b \rightarrow s\ell\ell$  data

Simple model provides combined explanation

# Outlook

- Flavour Anomalies require NP at the TeV scale  
→ Direct Searches at (HL-) LHC, FCC-pp
- This new particles in general also affect EW precision observables  
→ Z decays at CLIC and FCC-ee, CEPC
- Flavour is directly linked to the Higgs boson  
→ CLIC, FCC

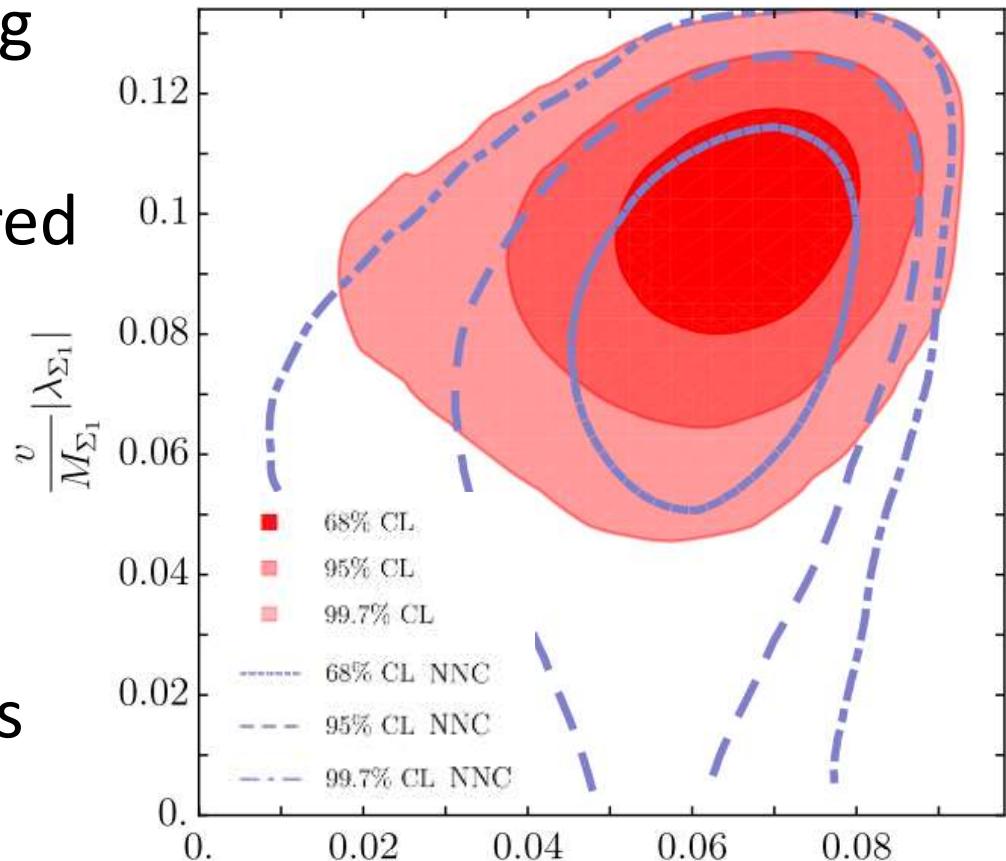


The flavour anomalies strengthen the physics case for future colliders significantly

# Backup

# Cabibbo Angle Anomaly and EW Fit

- Modified  $W_{ud}$  coupling
- Tree-level effects in beta decays disfavoured by LHC searches
- $W-W'$  mixing
- Vector-like leptons
  - $SU(2)_L$  singlet  $N$  coupling to electrons
  - $SU(2)_L$  triplet  $\Sigma$  coupling to muon

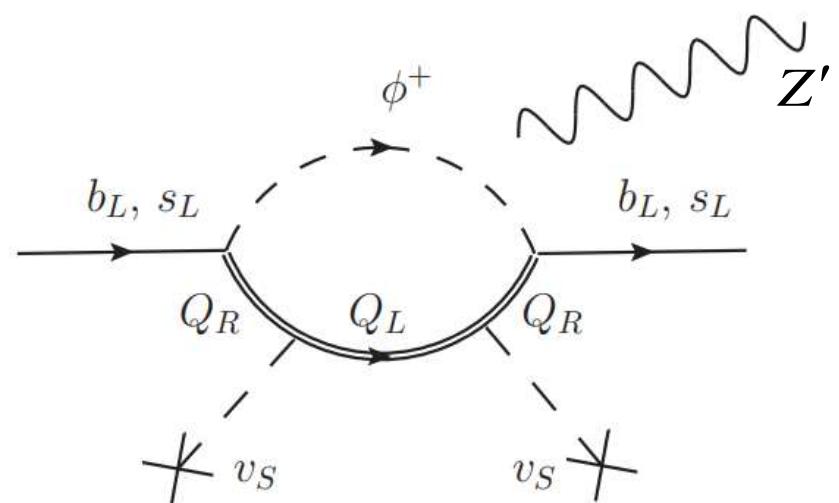
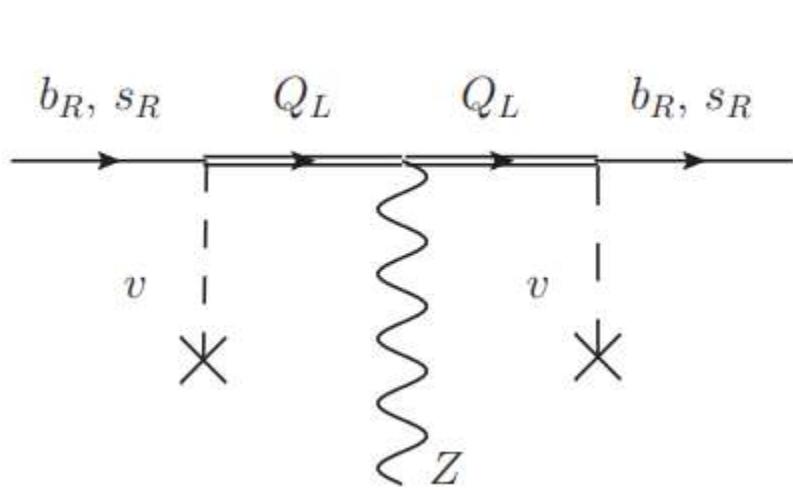


AC, F. Kirk, C. Manzari,  
M. Montull JHEP, 2008.01113  $\frac{v}{M_N} |\lambda_N|$

>5 $\sigma$  improvement over SM hypothesis

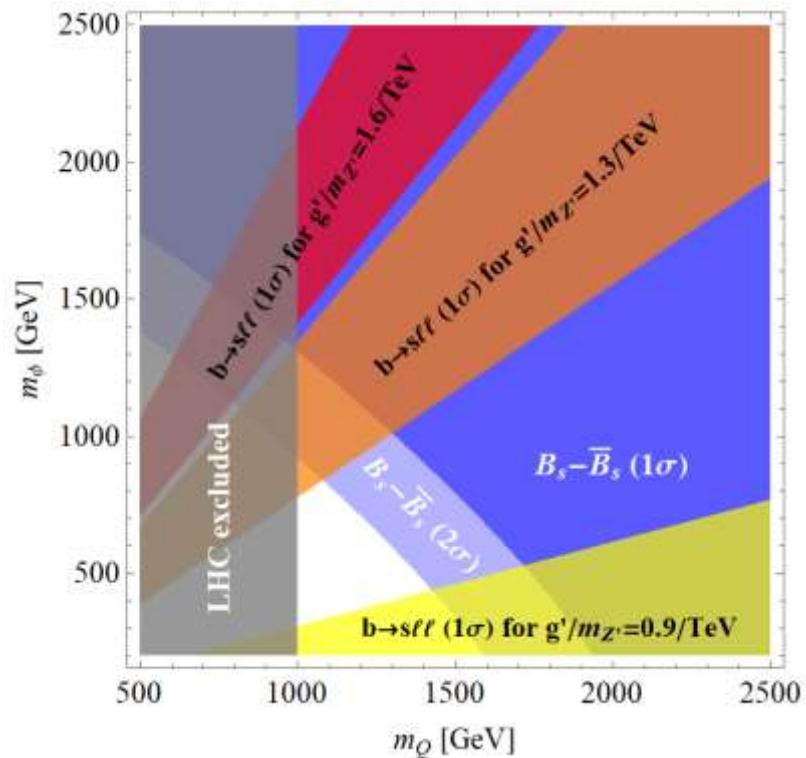
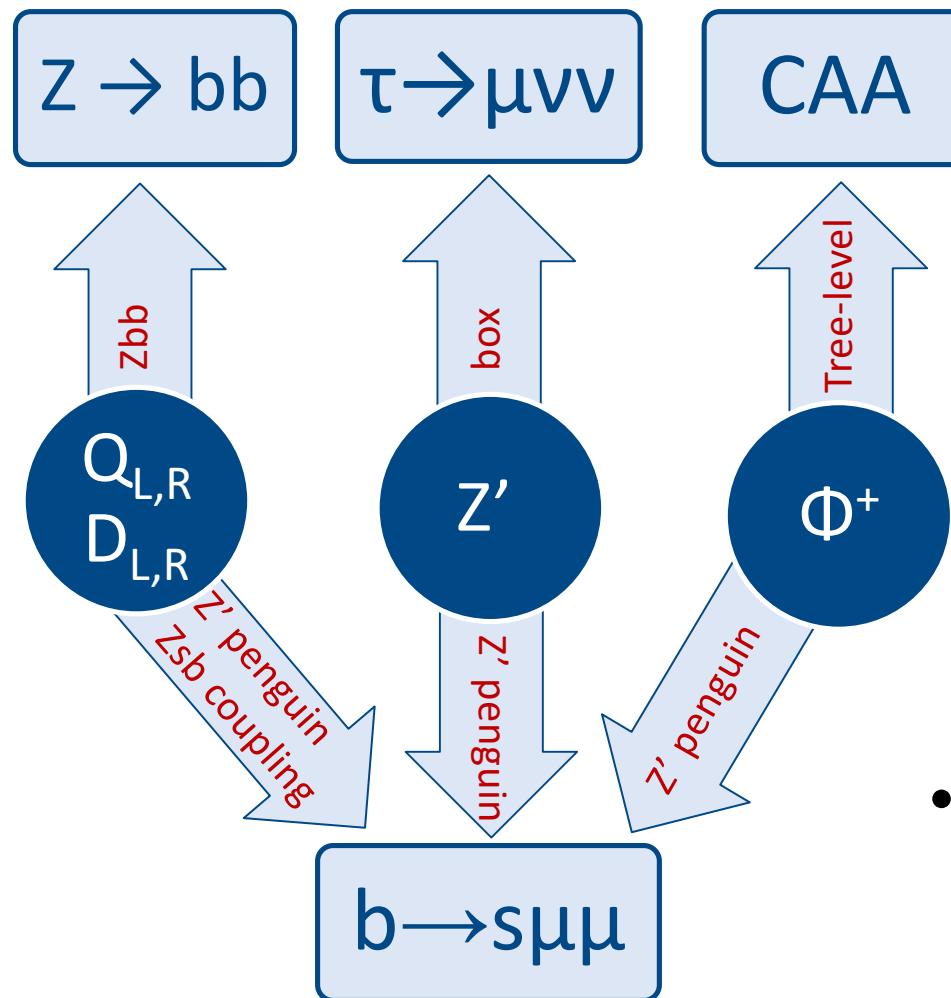
# Model for $b \rightarrow s\ell\ell$ , CAA, $Z \rightarrow bb$ and $\tau \rightarrow \mu\nu\nu$

	$q_L$	$d_R$	$u_R$	$H$	$\ell_L$	$e_R$	$Q_L$	$Q_R$	$D_L$	$D_R$	$\phi^+$	$S$
$SU(3)_c$	3	3	3	1	1	1	3	3	3	3	1	1
$SU(2)_L$	2	1	1	2	2	1	2	2	1	1	1	1
$U(1)_Y$	$\frac{1}{6}$	$-\frac{1}{3}$	$\frac{2}{3}$	$\frac{1}{2}$	$-\frac{1}{2}$	-1	$-\frac{5}{6}$	$-\frac{5}{6}$	$-\frac{1}{3}$	$-\frac{1}{3}$	1	0
$U(1)'$	0	0	0	0	(0, 1, -1)		0	1	1	0	-1	-1



Tree effect in  $Zbb$  and loop in  $Z'sb$

# Model for $b \rightarrow s\ell\ell$ , CAA, $Z \rightarrow bb$ and $\tau \rightarrow \mu\nu\nu$

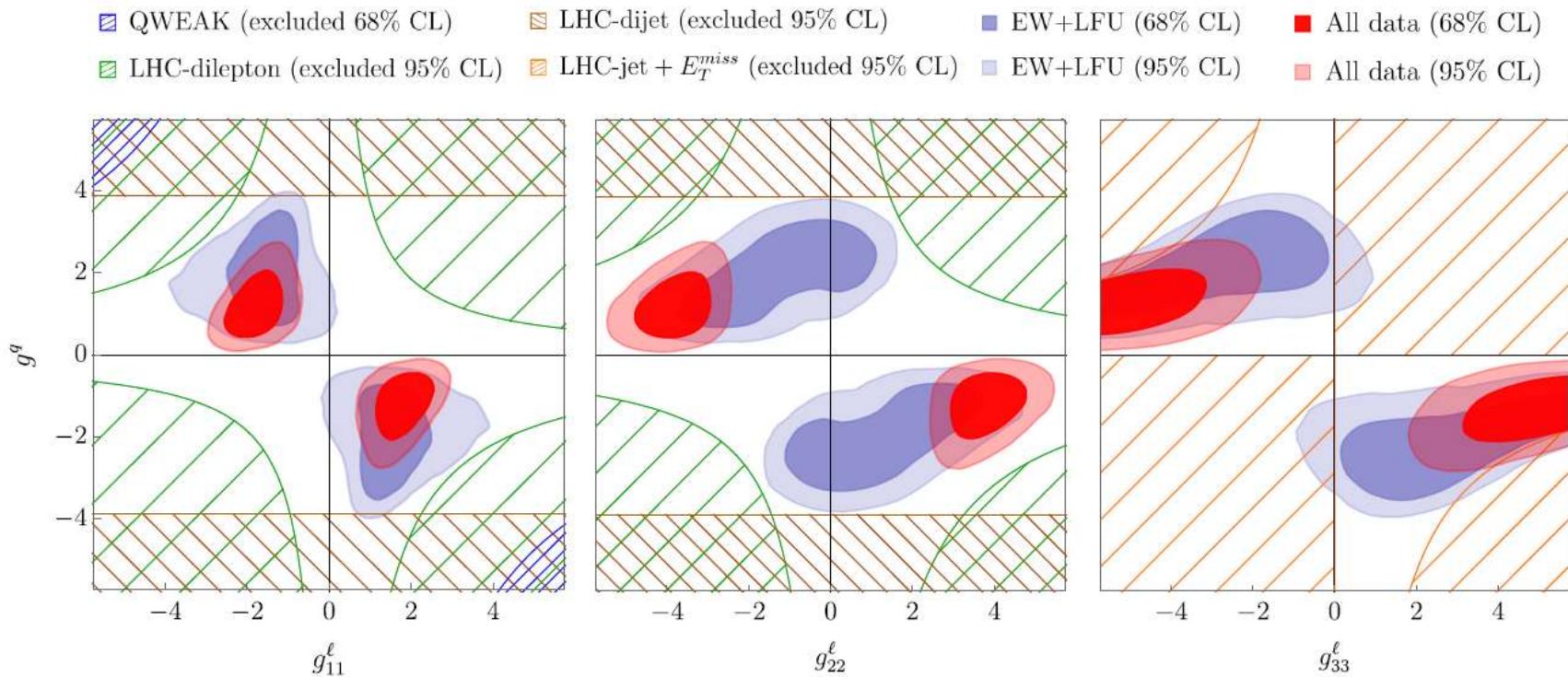


- $Z'$  penguin + modified Zsb coupling give very good fit to  $b \rightarrow s\ell\ell$  data

Simple model provides combined explanation

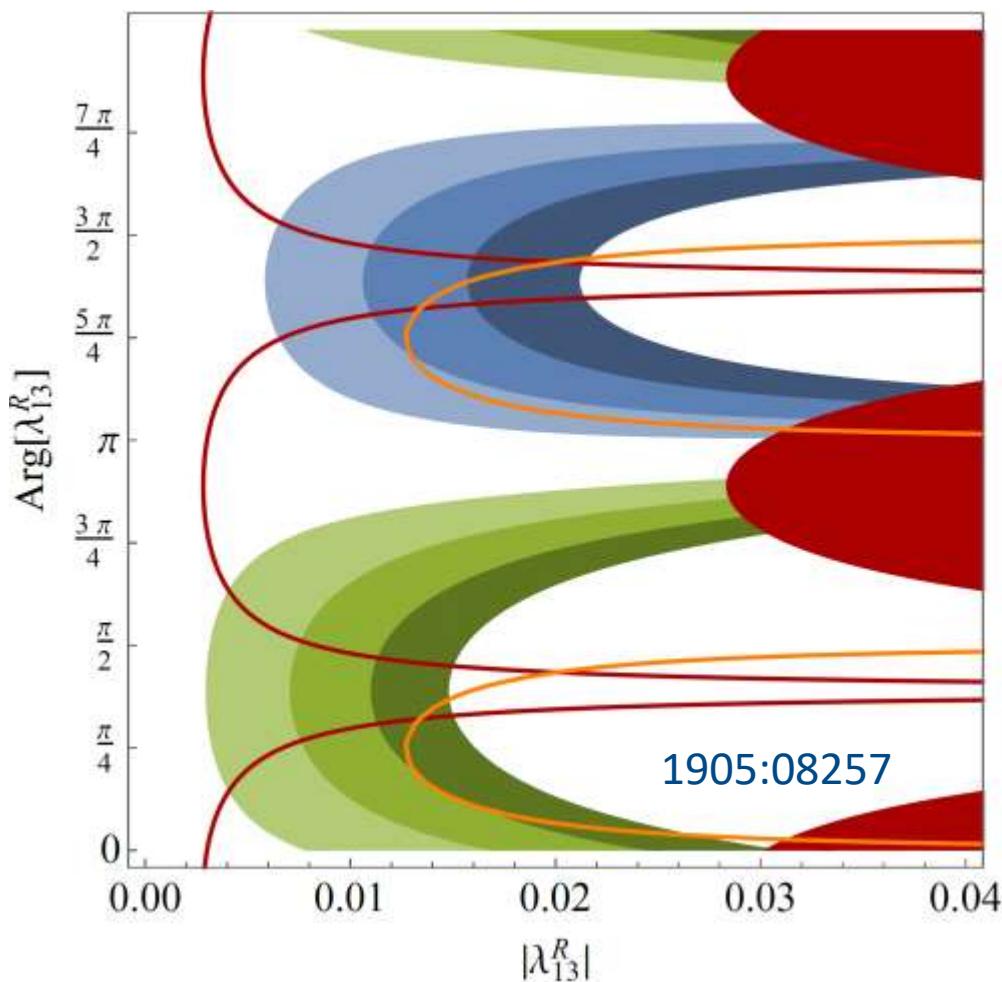
# $W'$ Explanation of $R(V_{us})$

- $W'$  effects in LFU and EW observables
- $Z'$  effects in LHC di-jet and di-lepton tail searches



$R(V_{us})$  can be explained by a left-handed  $W'$

# Correlations the neutron EDM with S1

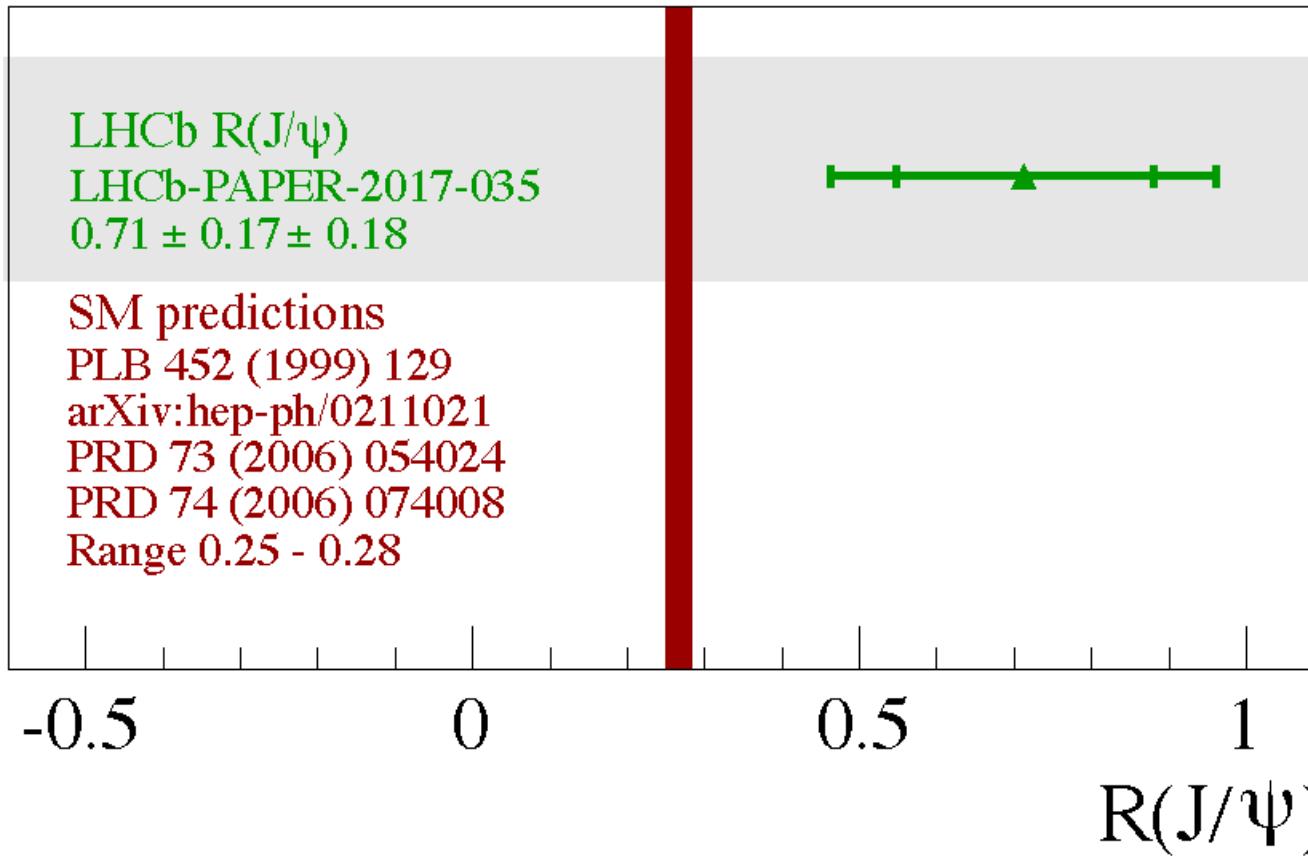


W. Dekens, J. de Vries, M. Jung,  
K. K. Vos, arXiv:1809.09114  
AC, F. Saturnino  
arxiv:1905:08257

Effect in B predicts measurable nEDM effect

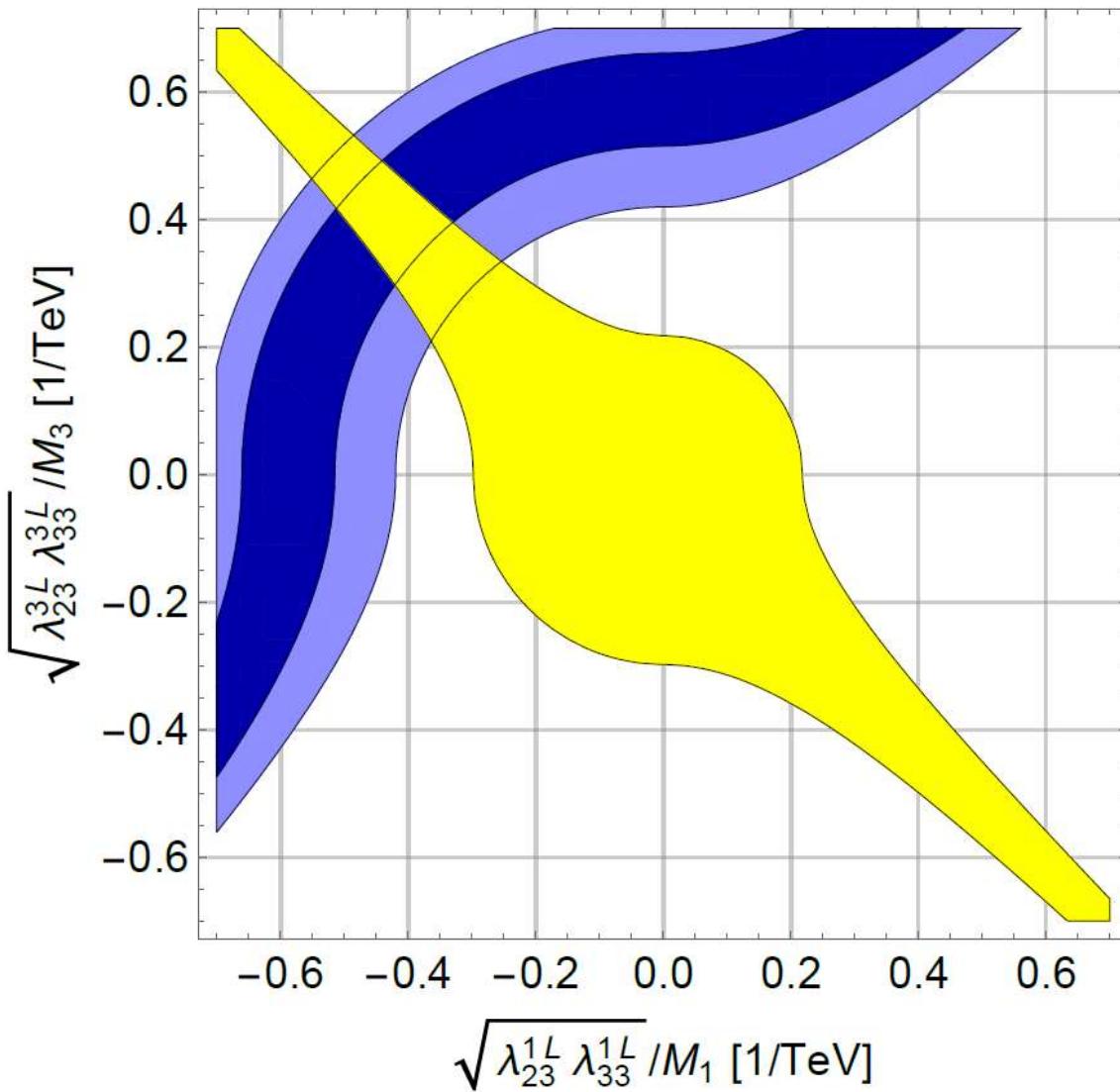
# $b \rightarrow c\tau\nu$ Measurements

$$R(J/\Psi) = B_c \rightarrow J/\Psi \tau\nu / B_c \rightarrow J/\Psi 1\nu$$



Supports  $R(D)$  &  $R(D^*)$

# $R(D^{(*)})$ , $b \rightarrow svv$ with 2 Scalar LQs

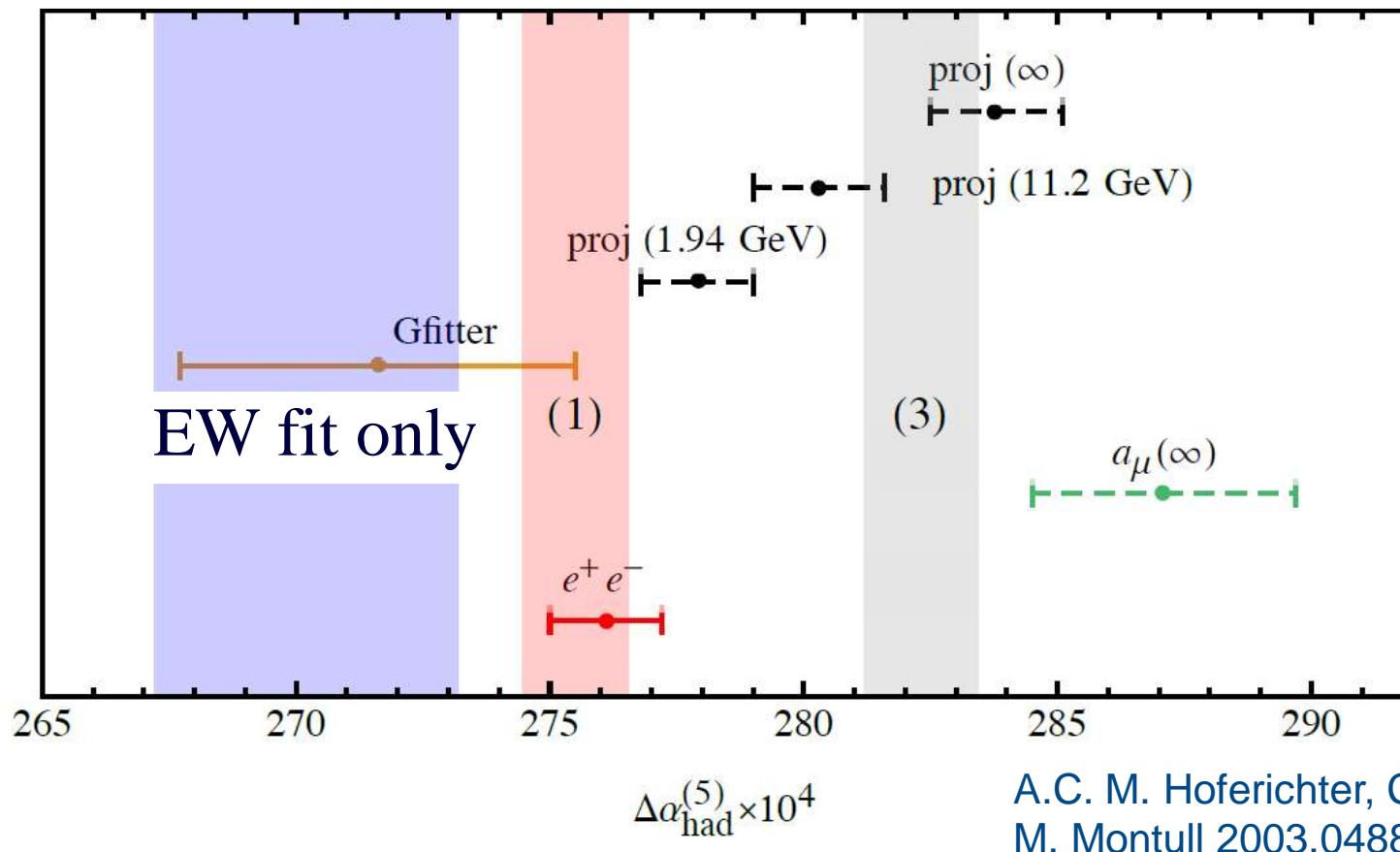


- $R(D^{(*)}) 2\sigma$
- $R(D^{(*)}) 1\sigma$
- $b \rightarrow svv$  allowed

$$\lambda_{jk}^L \equiv \lambda_{jk}^{1L}$$
$$\lambda_{jk}^{3L} = e^{i\pi j} \lambda_{jk}^L$$

# Hadronic Vacuum Polarization

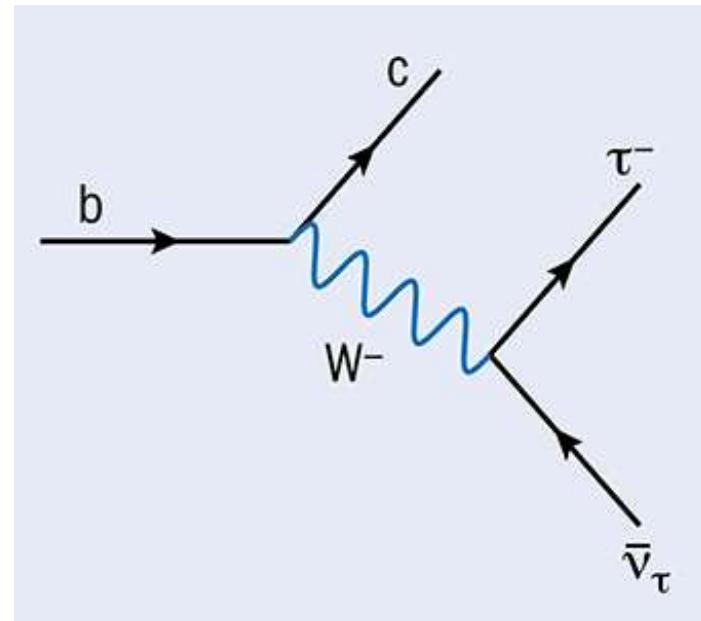
- New BMWc lattice QCD result



Up to  $4\sigma$  tension in EW fit

# $b \rightarrow c \tau \bar{\nu}_\tau$ Transitions

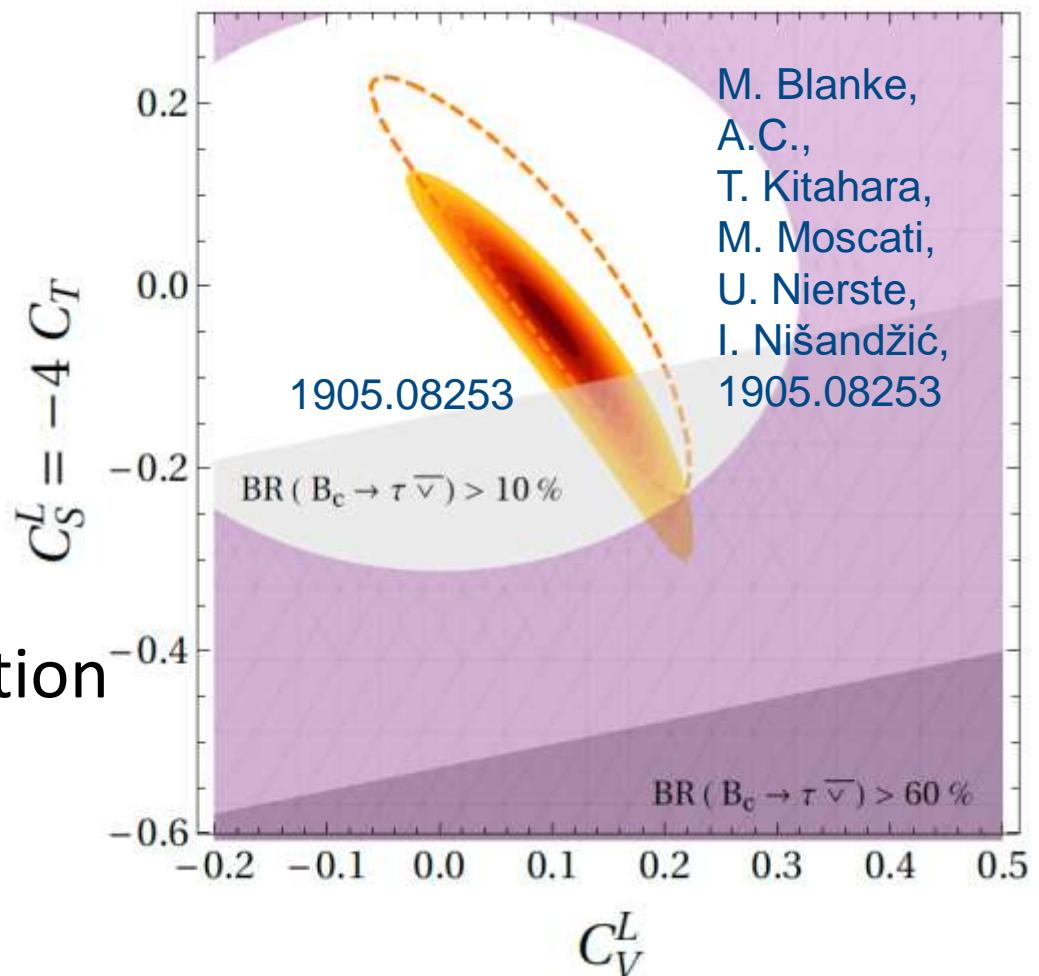
- $B \rightarrow D\tau\nu$ ,  $B \rightarrow D^*\tau\nu$ ,  $\Lambda_b \rightarrow \Lambda_c\tau\nu$
- Tree-level decays in the SM
- Form factors needed
- With light leptons ( $\mu$ ,  $e$ ) used to determine the CKM elements
- CKM fit works very well, i.e. tree-level in agreement with  $\Delta F=2$  processes



Largest B branching ratios, used to determine the CKM elements, usually assumed to be free of NP

# $b \rightarrow c\tau\nu$ Global Fit

- Pure scalar-tensor explanations in tension with the  $B_c$  lifetime
- Pure left-handed vector, i.e. contribution to the SM operator gives good fit

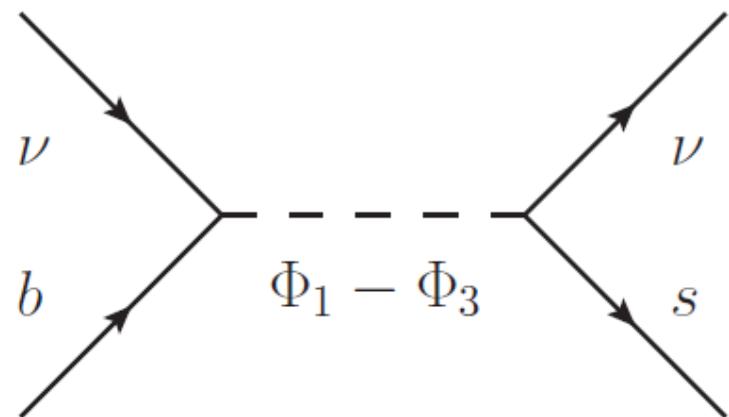
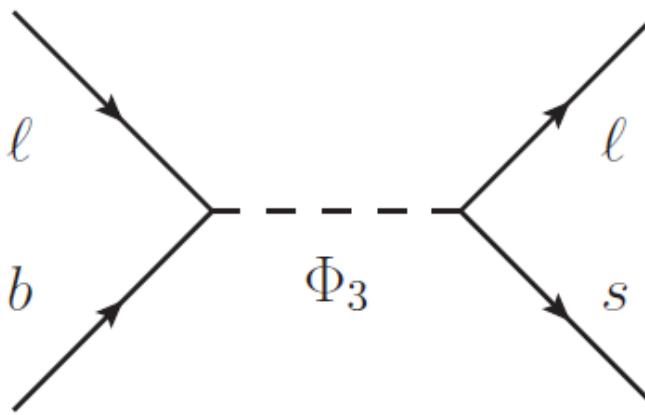
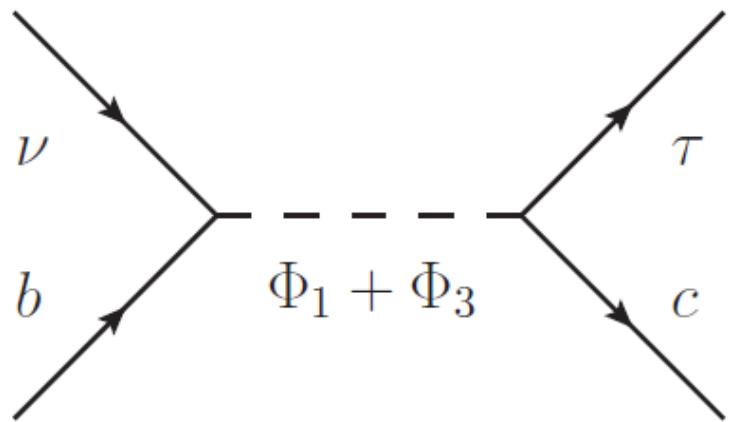


Global fit give up to  $4\sigma$  preference for NP

# Two Scalar Leptoquarks

AC, D. Mueller, T. Ota  
arxiv:1703.09226

- $\Phi_1$  scalar leptoquark singlet with  $Y=-2/3$
- $\Phi_3$  scalar leptoquark triplet with  $Y=-2/3$



Constructive in  $R(D^{(*)})$   
Destructive in  $b \rightarrow s \mu \mu$

# R(D<sup>(\*)</sup>), b→sll and a<sub>μ</sub>

## ■ 4 benchmark points

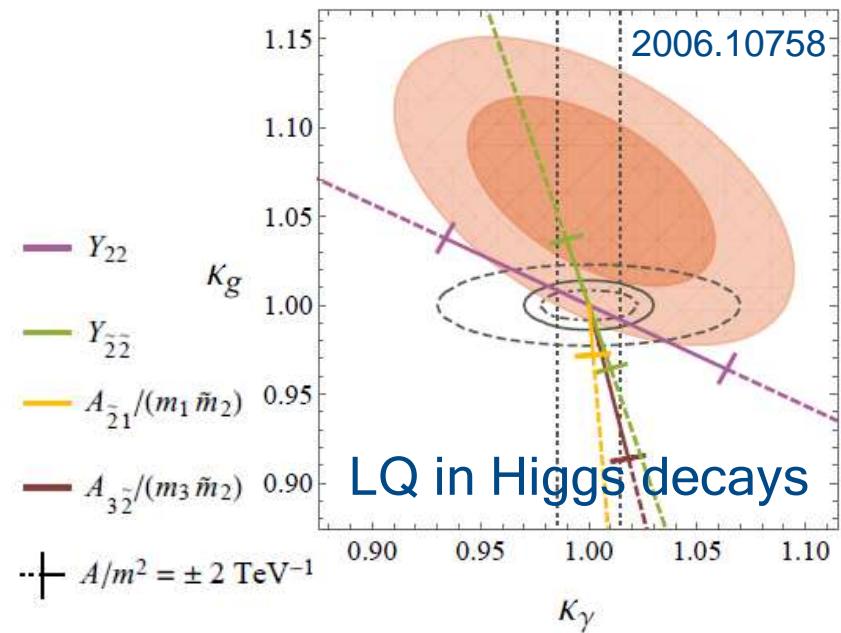
AC, D. Mueller, F. Saturnino  
arxiv:1912.04224

	$\kappa_{22}$	$\kappa_{32}$	$\kappa_{23}$	$\kappa_{33}$	$\lambda_{22}$	$\lambda_{32}$	$\lambda_{23}$	$\lambda_{33}$	$\hat{\lambda}_{32}$	$\hat{\lambda}_{23}$
● $p_1$	-0.019	-0.059	0.58	-0.11	-0.0082	-0.016	-1.46	-0.064	-0.19	1.34
● $p_2$	-0.017	-0.070	-1.23	0.066	0.0078	-0.055	1.36	0.052	-0.053	-1.47
● $p_3$	0.0080	0.081	1.18	-0.073	-0.0017	0.16	-0.76	-0.068	0.023	1.23
● $p_4$	-0.0032	-0.21	0.44	-0.20	0.014	-0.10	-1.38	-0.068	-0.032	0.57
	$C_9^{\mu\mu} = -C_{10}^{\mu\mu}$	$C_9^{\ell\ell}$	$\frac{R(D)}{R(D)_{\text{SM}}}$	$\frac{R(D^*)}{R(D^*)_{\text{SM}}}$	$\frac{B_s \rightarrow \tau\tau}{B_s \rightarrow \tau\tau _{\text{SM}}}$	$\tau \rightarrow \mu\gamma$ $\times 10^8$	$\delta a_\mu$ $\times 10^{11}$	$\tilde{V}_{cb}^e/\tilde{V}_{cb}^\mu - 1$ $\times 10^6$	$Z \rightarrow \tau\mu$ $\times 10^{10}$	
● $p_1$	-0.52	-0.21	1.15	1.10	59.88	4.35	207	291	0.117	
● $p_2$	-0.56	-0.28	1.14	1.10	99.76	0.766	199	448	2.38	
● $p_3$	-0.31	-0.31	1.14	1.09	112.5	3.62	255	17	0.129	
● $p_4$	-0.31	-0.31	1.13	1.11	112.5	0.734	230	934	45.6	
	$C_{SL}^{\tau\tau} = -4C_{TL}^{\tau\tau}$	$C_{VL}^{\tau\tau}$	$R_{\nu\nu}^{K(*)}$	$\frac{\Delta m_{B_s}^{\text{NP}}}{\Delta m_{B_s}^{\text{SM}}} \times 10^5$	$B \rightarrow K\tau\mu$ $\times 10^8$	$\tau \rightarrow \phi\mu$ $\times 10^8$	$\tau \rightarrow \mu ee$ $\times 10^{11}$	$ \Lambda_{33}^{\text{LQ}}(0)  \times 10^5$	$\frac{\Delta_{33}^L(m_Z^2)}{\Lambda_{\text{SM}}^{L\ell} \times 10^{-5}}$	
● $p_1$	0.023	0.040	2.33	0.1	0.512	1.27	44.94	1.11	-3.64	
● $p_2$	0.020	0.040	0.87	0.16	3.32	4.73	7.783	0.90	-3.02	
● $p_3$	0.023	0.037	1.08	0.19	4.07	1.00	37.89	0.89	-3.51	
● $p_4$	0.010	0.047	2.43	0.18	3.69	0.0021	18.60	3.12	-10.04	

Common explanation possible

# Outlook: Physics at Future Colliders

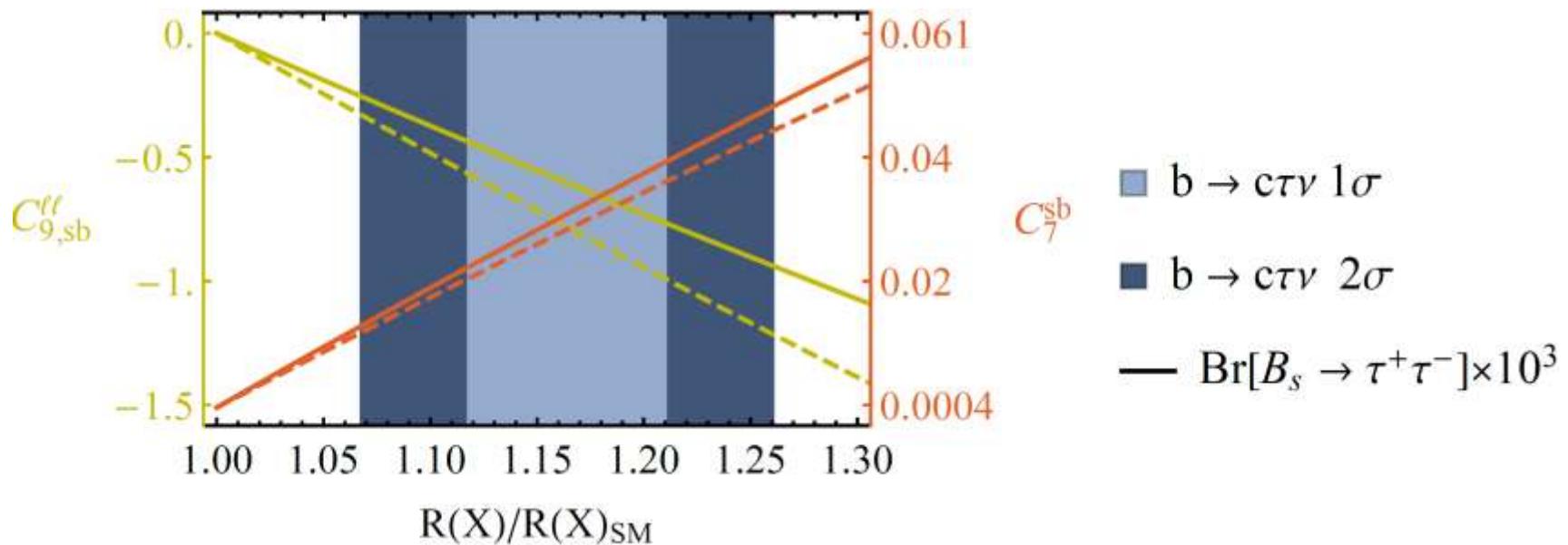
- Flavour Anomalies require NP at the TeV scale  
→ Direct Searches at HL-LHC, HE-LHC, FCC-pp
- This new particles in general also affect EW precision observables  
→ Z decays at CLIC and FCC-ee
- Flavour is directly linked to the Higgs boson  
→ CLIC, FCC



Flavour Anomalies (if confirmed) strengthen the physics case for future colliders significantly

# Important Loop-Effects

- Explanation of  $b \rightarrow c\tau\nu$  requires large  $b\tau$  and  $s\tau$  couplings (follows from SU(2) invariance)

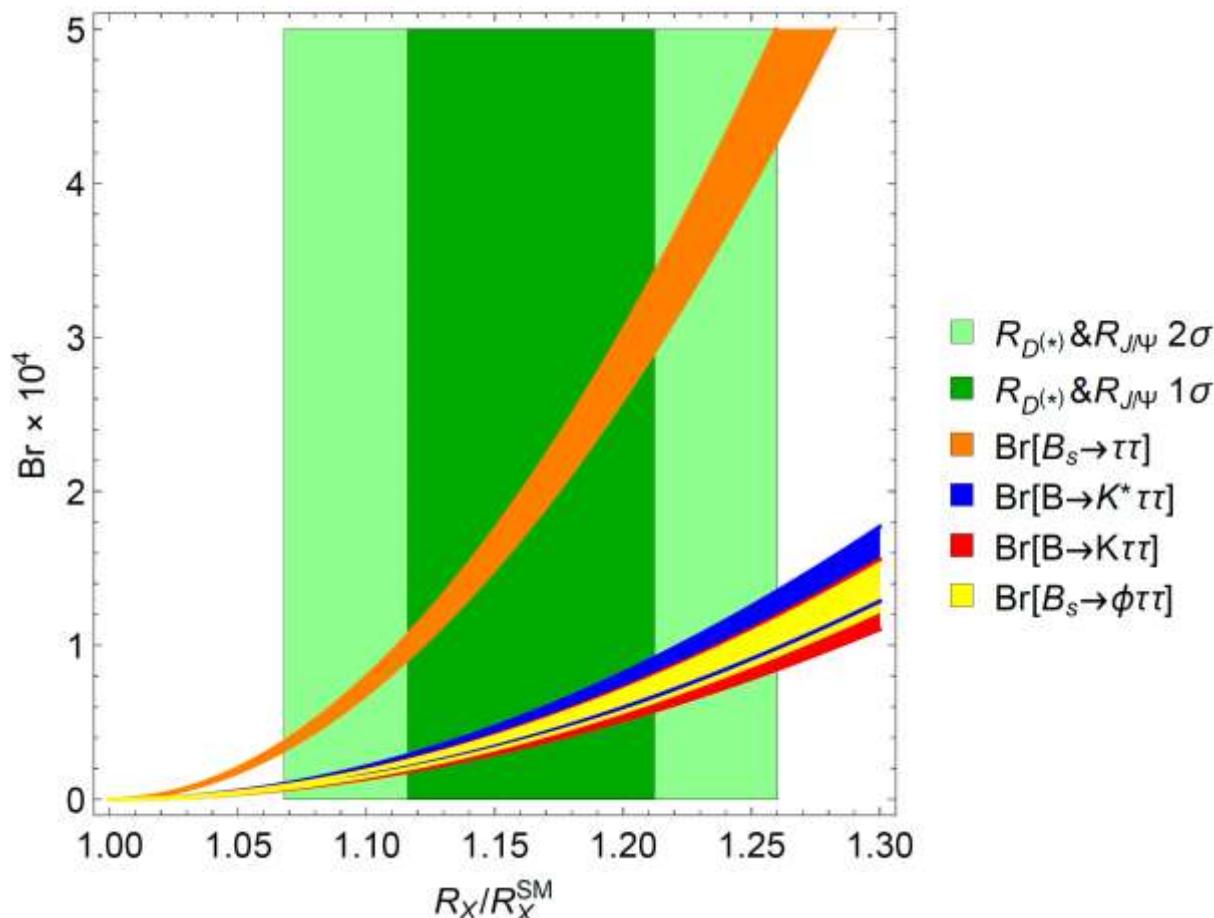


AC, C. Greub, D. Müller,  
F. Saturnino, PRL 2018

Large loop effects in  $b \rightarrow s\mu\mu$

# $R(D^{(*)})$ and $b \rightarrow s\tau\tau$

- Large couplings to the second generation



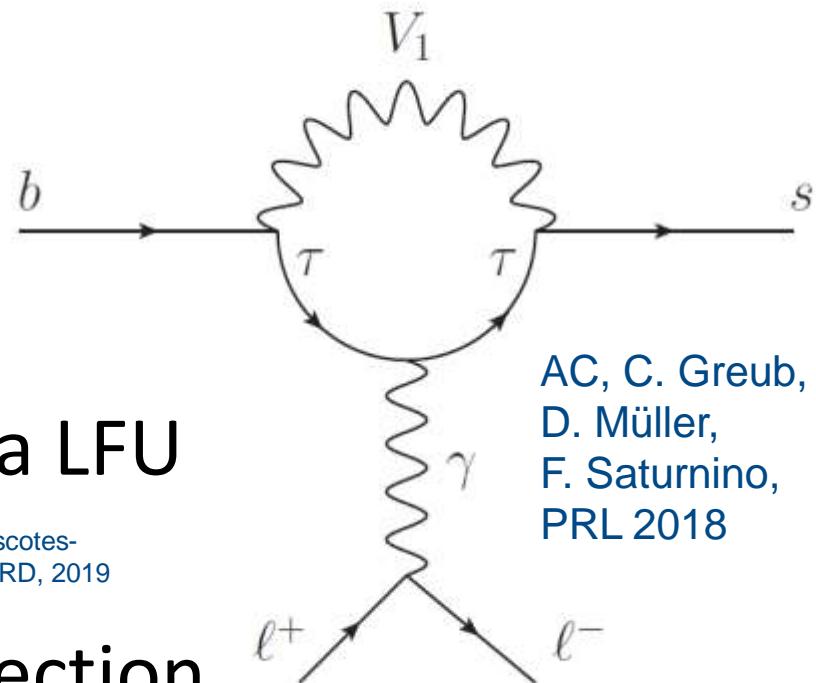
$b \rightarrow s\tau\tau$   
very  
strongly  
enhanced

B. Capdevila, AC, S. Descotes-Genon, L. Hofer and J. Matias, PRL.120.181802

# Important Loop-Effects

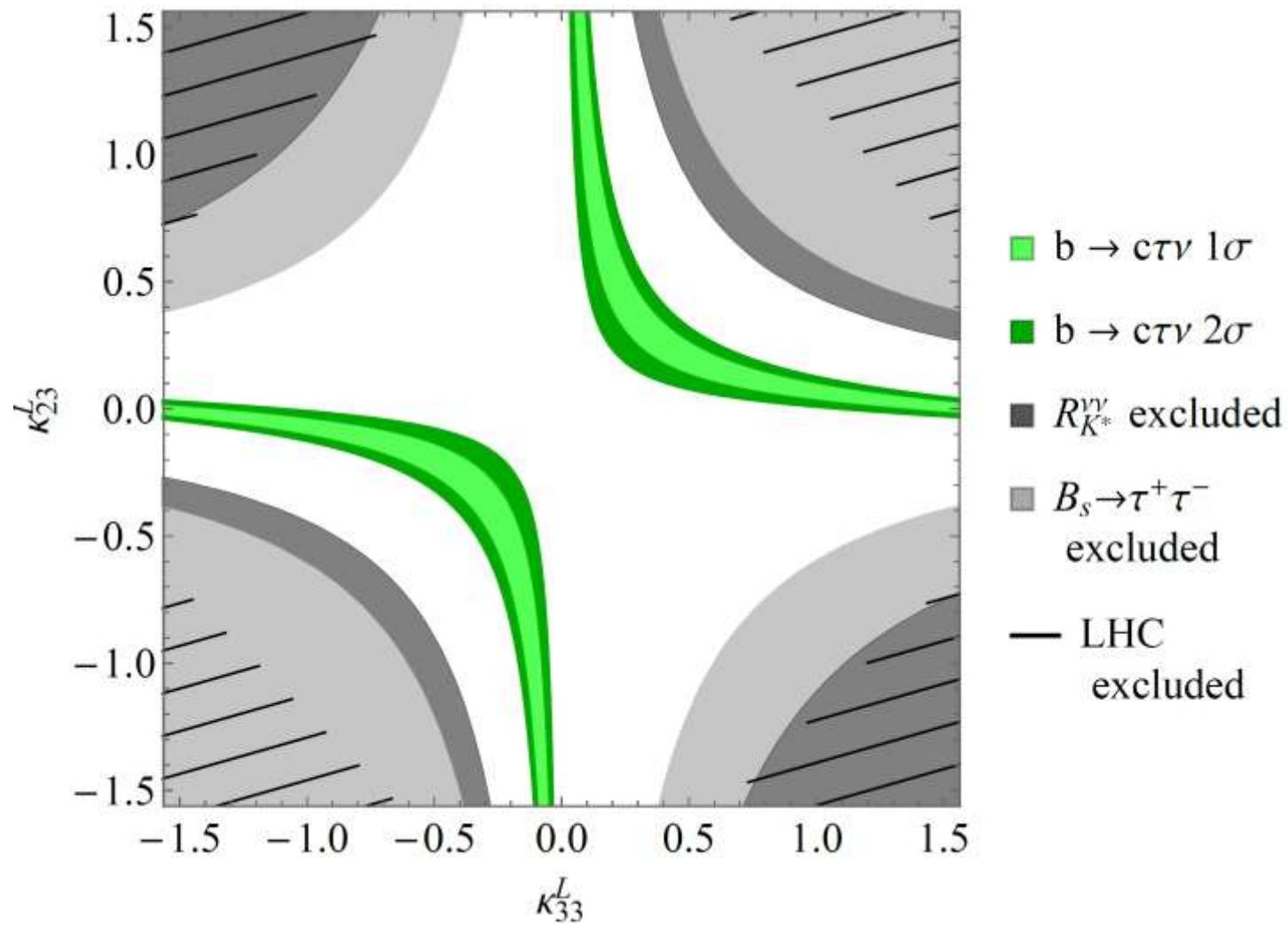
- Explanation of  $b \rightarrow c\tau\nu$  requires large LQ- $b\tau$  and LQ- $c-\nu_\tau$  couplings
- Via SU(2) invariance this leads to large effects in  $b \rightarrow s\tau\tau$  processes
- Closing the tau-loop gives a LFU effect in  $b \rightarrow sll$
- Effect goes in the right direction

M. Algueró, B. Capdevila, S. Descotes-Genon, P. Masjuan, J. Matias, PRD, 2019



Explanation of  $b \rightarrow c\tau\nu$  leads to  
loop effects in  $b \rightarrow s\mu\mu$

# Vector LQ Phenomenology



Compatible with constraints for generic couplings

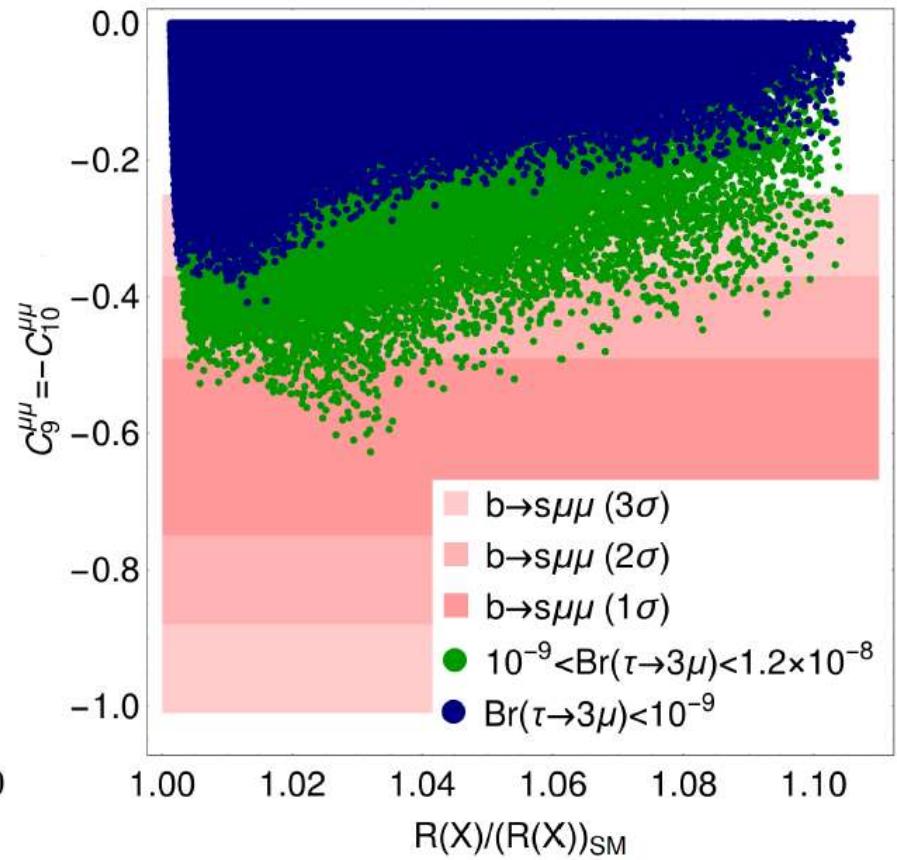
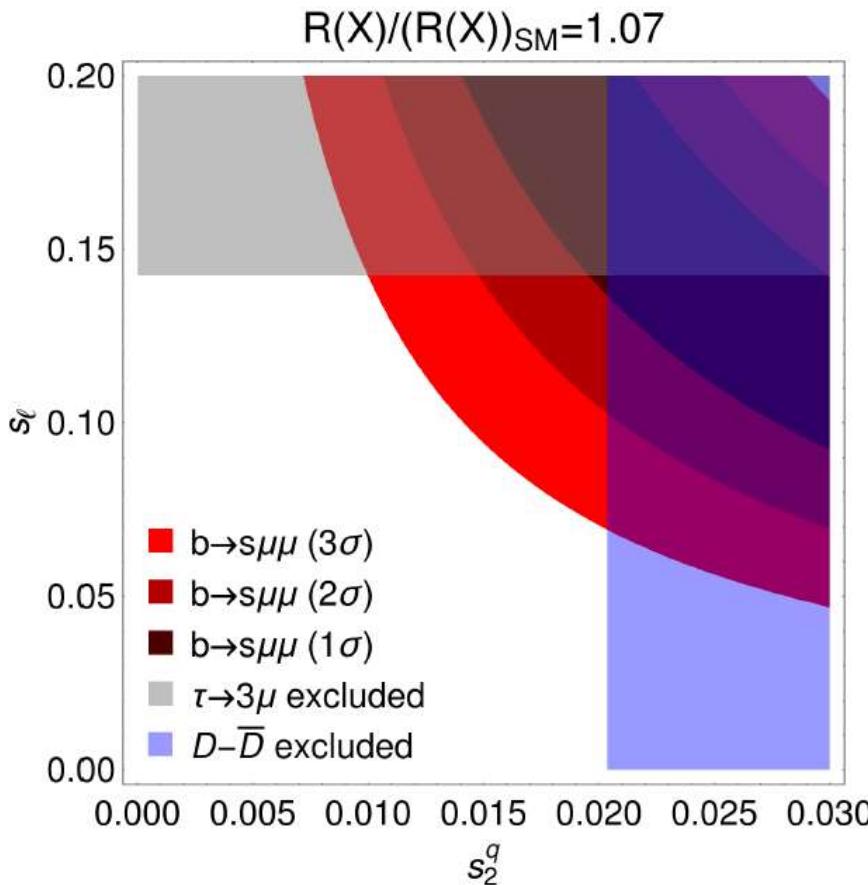
# Possible UV completions

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- $SU(4) \times SU(3)' \times SU(2)_L \times U(1)_Y +$  Vector-like fermions  
L. Di Luzio, A. Greljo, M. Nardecchia, arXiv:1708.08450
- $SU(4) \times U(2)_L \times SU(2)_R +$  Vector-like fermions  
L. Calibbi, AC, T. Li, arXiv:1709.00692
- $SU(4) \times SU(4) \times SU(4)$   
M. Bordone, C. Cornella, J. Fuentes-Martin, G. Isidori, arXiv:1712.01368
- $SU(4) \times U(2)_L \times SU(2)_R$  including scalar LQs and  
light right-handed neutrinos  
J. Heeck, D. Teresi, arXiv:1808.07492
- $SU(8)$  might even explain  $\epsilon'/\epsilon$   
S. Matsuzaki, K. Nishiwaki and K. Yamamoto, arXiv:1806.02312
- $SU(4) \times U(2) \times SU(2)_R$  in RS background  
M. Blanke, AC, arXiv:1801.07256

Good solution, but challenging UV completion

# Pati-Salam RS Phenomenology



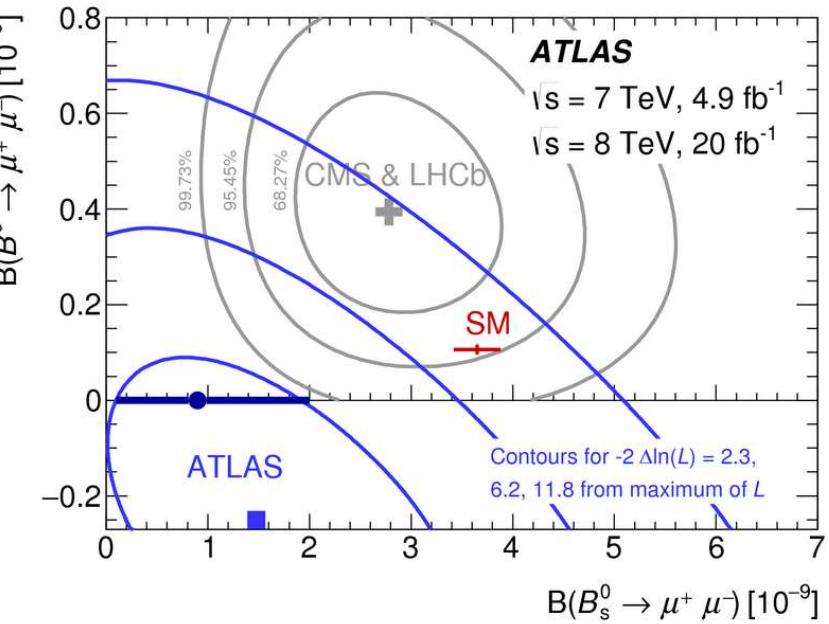
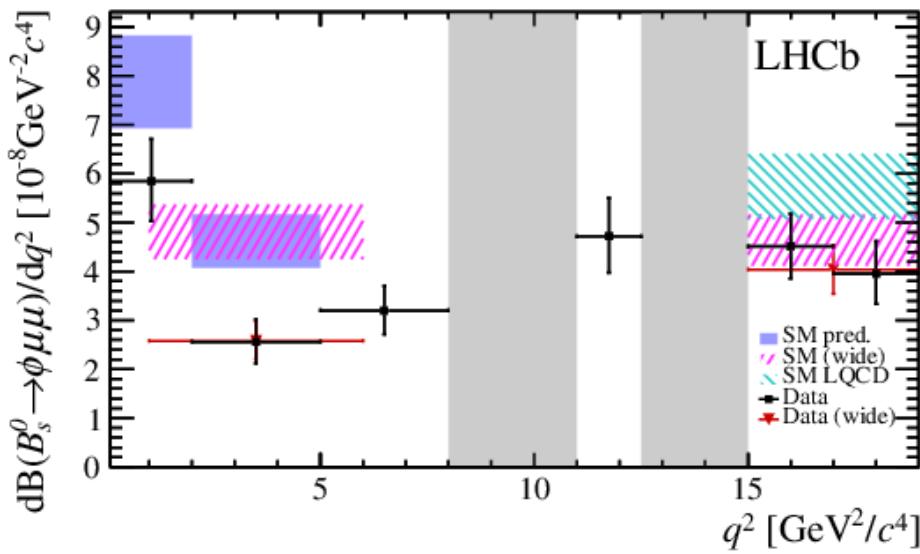
$$M = 3 \text{ TeV}, s_2^\ell = 0.2, s_3^\ell = 1/\sqrt{2} \text{ and } s_3^q = \sqrt{3}/2$$

M. Blanke, AC, PRL 2018

Model well motivated + limited but sizable effect

# $B_s \rightarrow \mu\mu$ and $B_s \rightarrow \phi\mu\mu$

- $B_s \rightarrow \mu\mu$  theoretically clean but chirality suppressed and therefore statistically limited

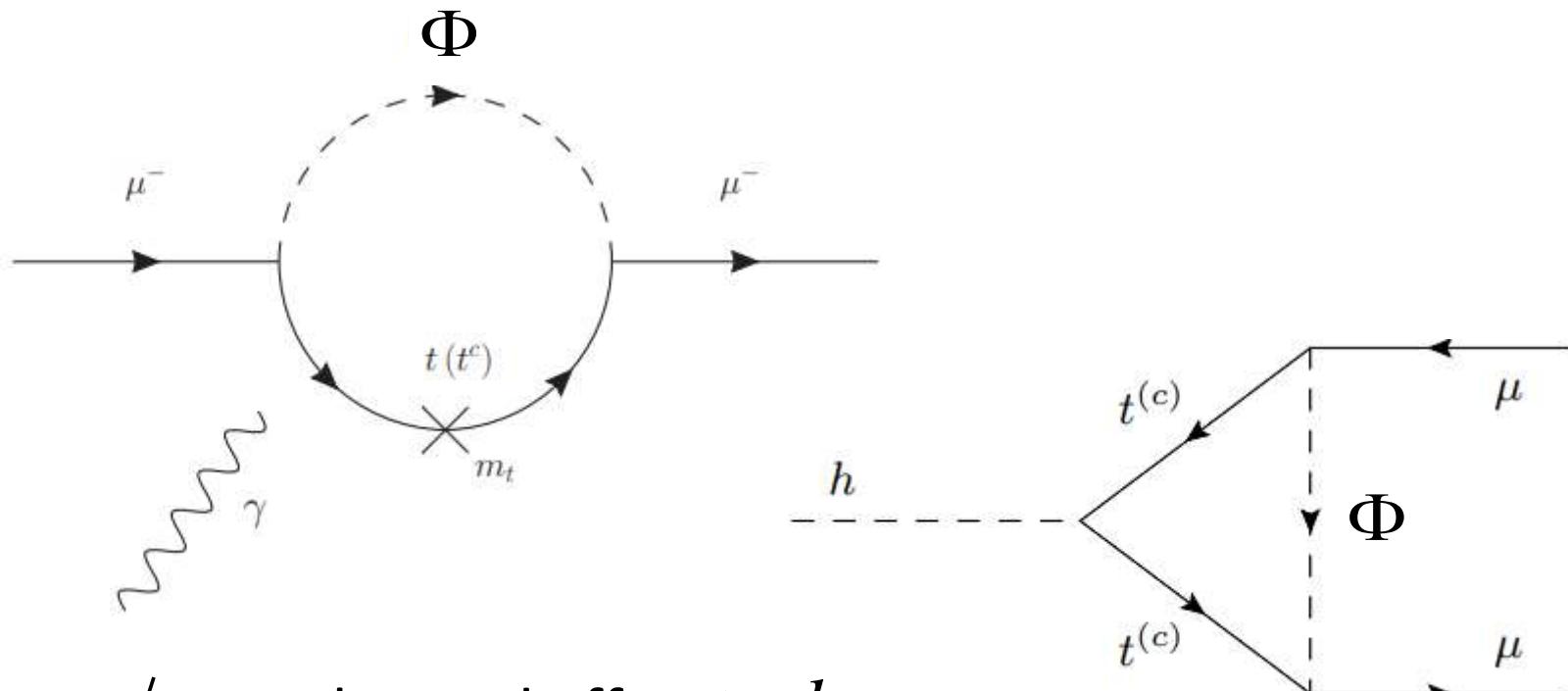


- $B_s \rightarrow \phi\mu\mu$  has a higher Br, but knowledge of the form-factor needed

Br's  $\approx 20\%$  below SM expectations

# Leptoquarks in $a_\mu$

- Chirally enhanced effects via top-loops

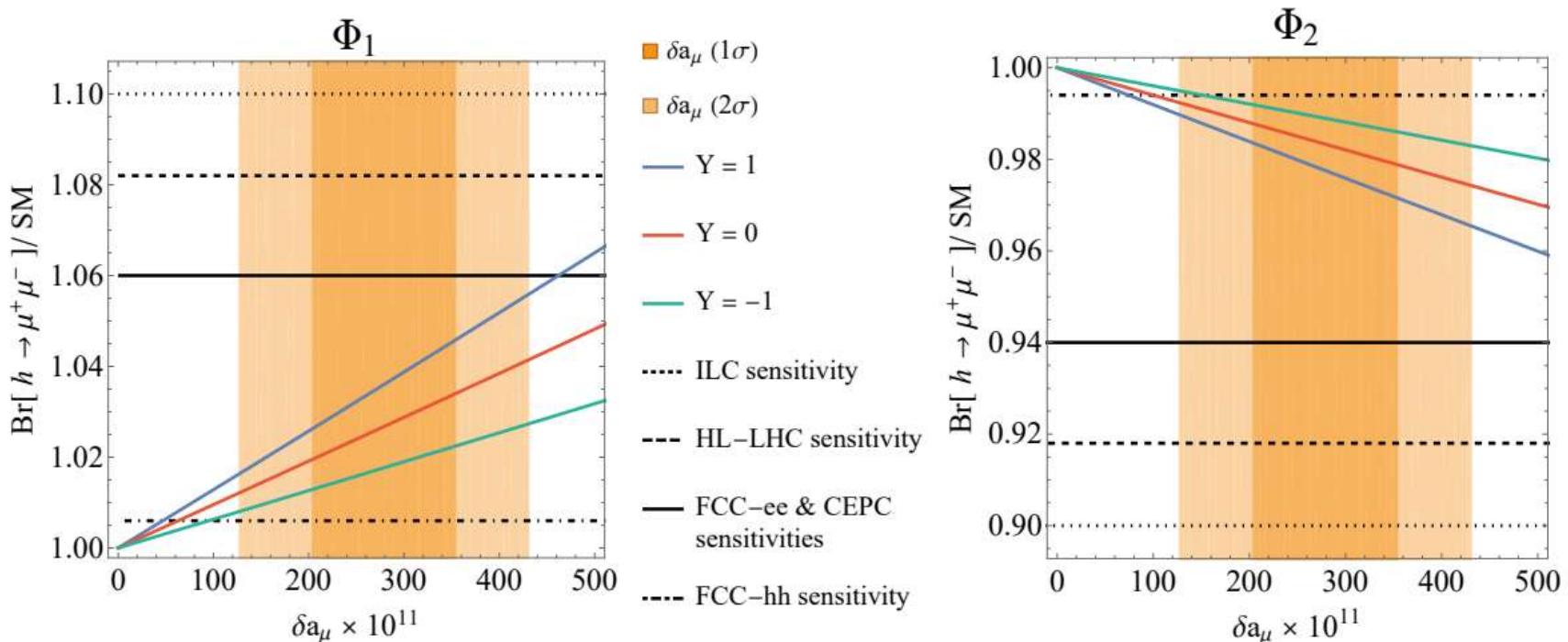


- $m_t/m_\mu$  enhanced effect  $h \rightarrow \mu\mu$
- $m_t^2/m_Z^2$  enhanced effect in  $Z \rightarrow \mu\mu$

Correlations with  $h \rightarrow \mu\mu$  and  $Z \rightarrow \mu\mu$

# $a_\mu$ vs $h \rightarrow \mu\mu$

- Chirally enhanced effects via top-loops
- Same coupling structure → direct correlation



A.C., D. Mueller, F. Saturnino, 2008.02643

$h \rightarrow \mu\mu$  at future colliders

# $\tau \rightarrow \mu \nu \bar{\nu}$ and $\tau \rightarrow e \nu \bar{\nu}$

- Ratios of leptonic tau decays

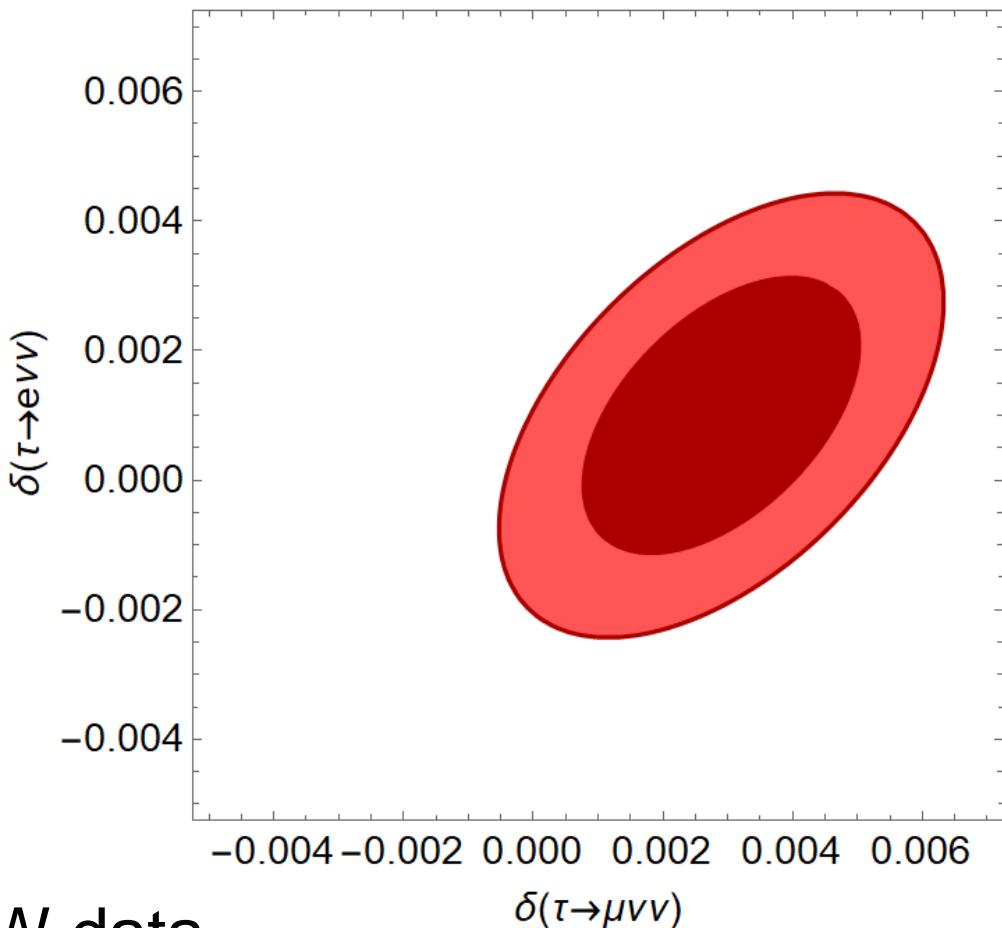
$$\frac{A_{\text{EXP}}(\tau \rightarrow \mu \nu \bar{\nu})}{A_{\text{SM}}(\mu \rightarrow e \nu \bar{\nu})} = 1.0029 \pm 0.0014$$

$$\frac{A_{\text{EXP}}(\tau \rightarrow \mu \nu \bar{\nu})}{A_{\text{SM}}(\tau \rightarrow e \nu \bar{\nu})} = 1.0018 \pm 0.0014$$

$$\frac{A_{\text{EXP}}(\tau \rightarrow e \nu \bar{\nu})}{A_{\text{SM}}(\mu \rightarrow e \nu \bar{\nu})} = 1.0010 \pm 0.0014$$

$$\rho = \begin{pmatrix} 1.00 & 0.49 & 0.51 \\ 0.49 & 1.00 & -0.49 \\ 0.51 & -0.49 & 1.00 \end{pmatrix}$$

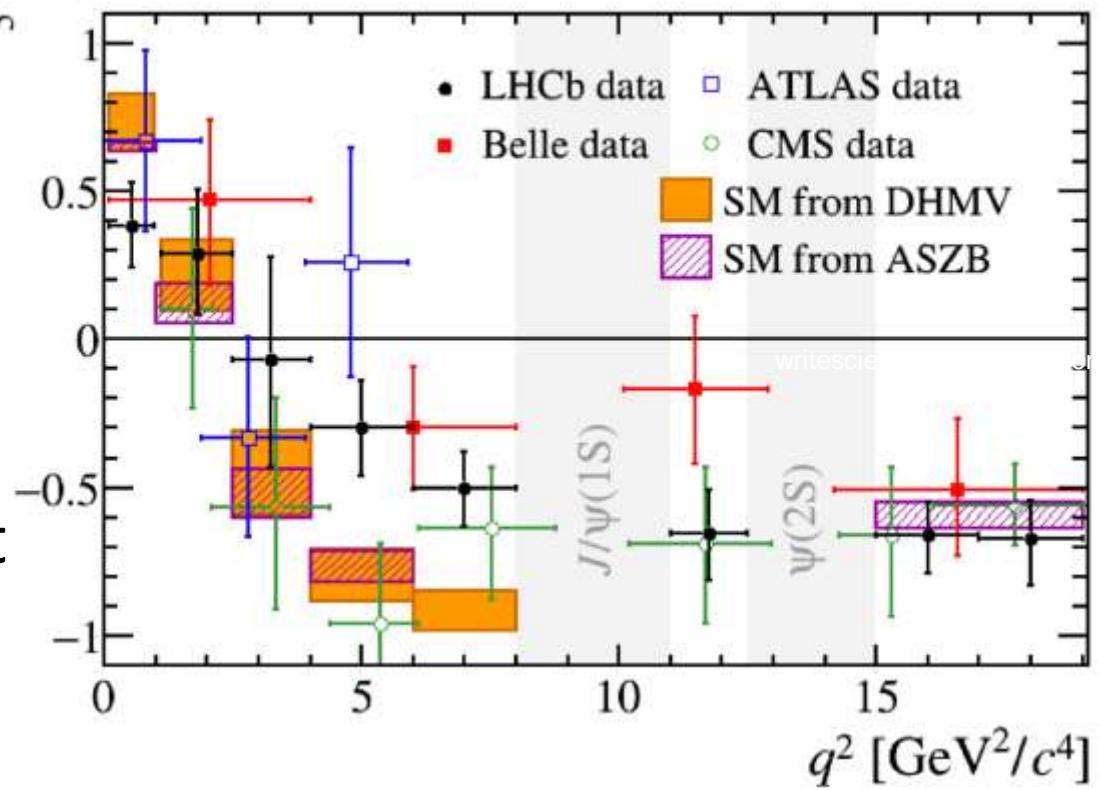
- NP in muon decay constrained from EW data



≈2σ hint for LFUV in tau decays

# The $P_5'$ Anomaly

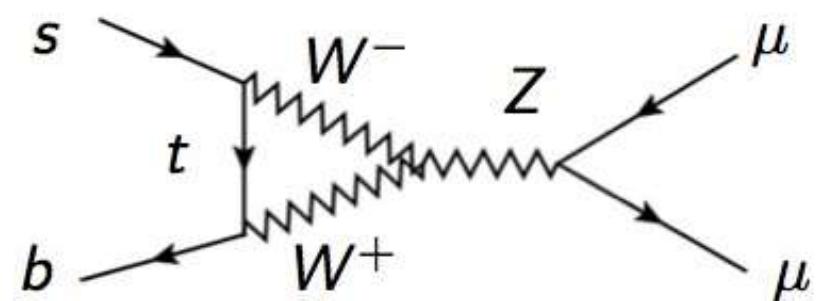
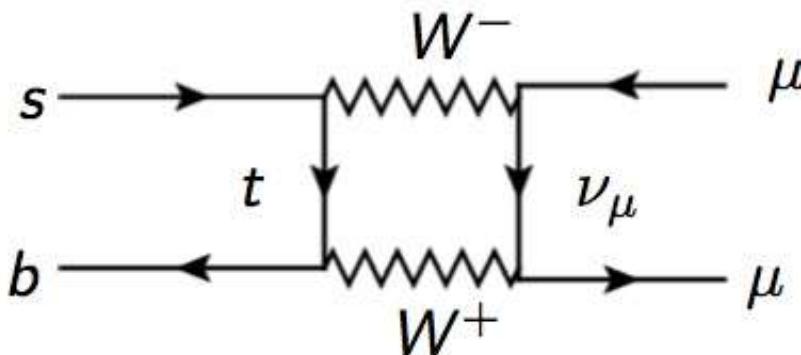
- $P_5'$  angular observables in  $B \rightarrow K^* \mu\mu$  S. Descotes-Genon, T. Hurth, J. Matias, J. Virto, JHEP 2013
- Constructed in such a way that the form factor dependence is minimized
- Confirmed by latest LHCb analysis for the charged mode



>3 $\sigma$  deviation from the SM prediction

# $b \rightarrow s \mu^+ \mu^-$ Processes

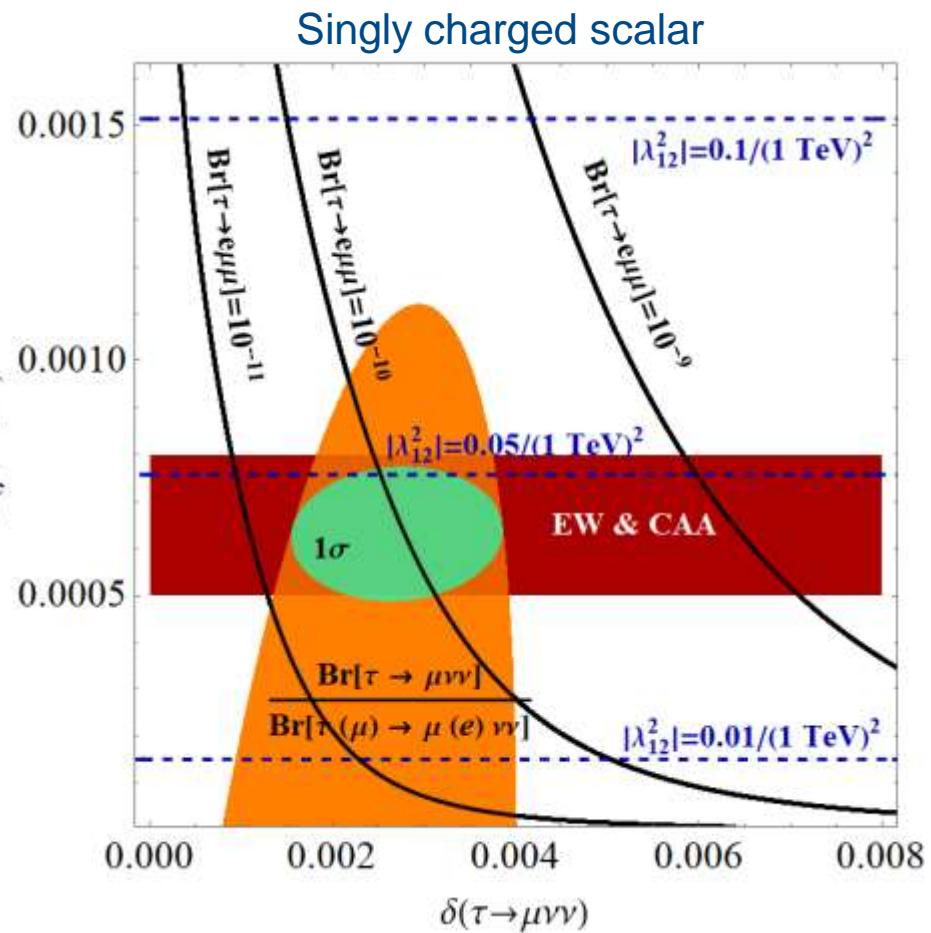
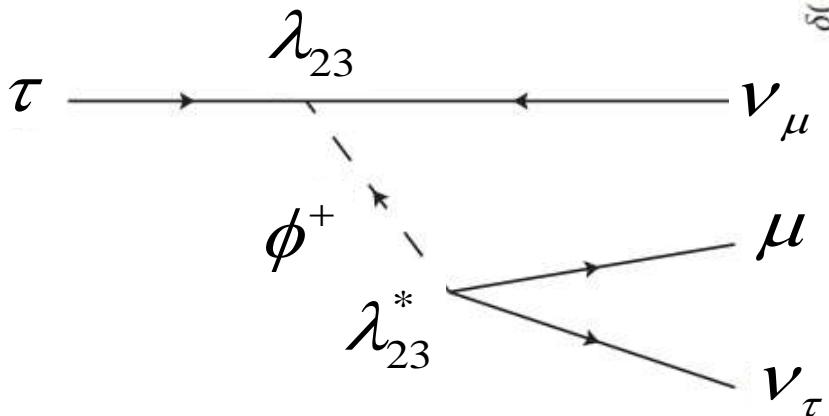
- Flavour Changing Neutral Current (FCNC)
- In the SM it is suppressed by
  - The CKM elements  $V_{cb} \approx 0.04$
  - Electroweak scale
  - Loop-factor
- Wilson coefficients precisely known Bobeth et al. PRD, 2013



Suppressed in the SM and very sensitive to NP

# $\tau \rightarrow \mu \nu \nu$

- $L_\mu$ - $L_\tau$   $Z'$  (box diagrams)
- LFV violating  $Z'$
- Modified  $W\ell\nu$  couplings
- $W'$
- Singly charged scalar



A.C., F. Kirk, C. Manzari, L. Panizzi, arXiv:2012.09845

Scenarios can be distinguished by  $\pi \rightarrow \mu \nu / \pi \rightarrow e \nu$